

2.8 ÉQUATIONS TRIGONOMETRIQUES

cours 20

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Sont des équations trigonométriques

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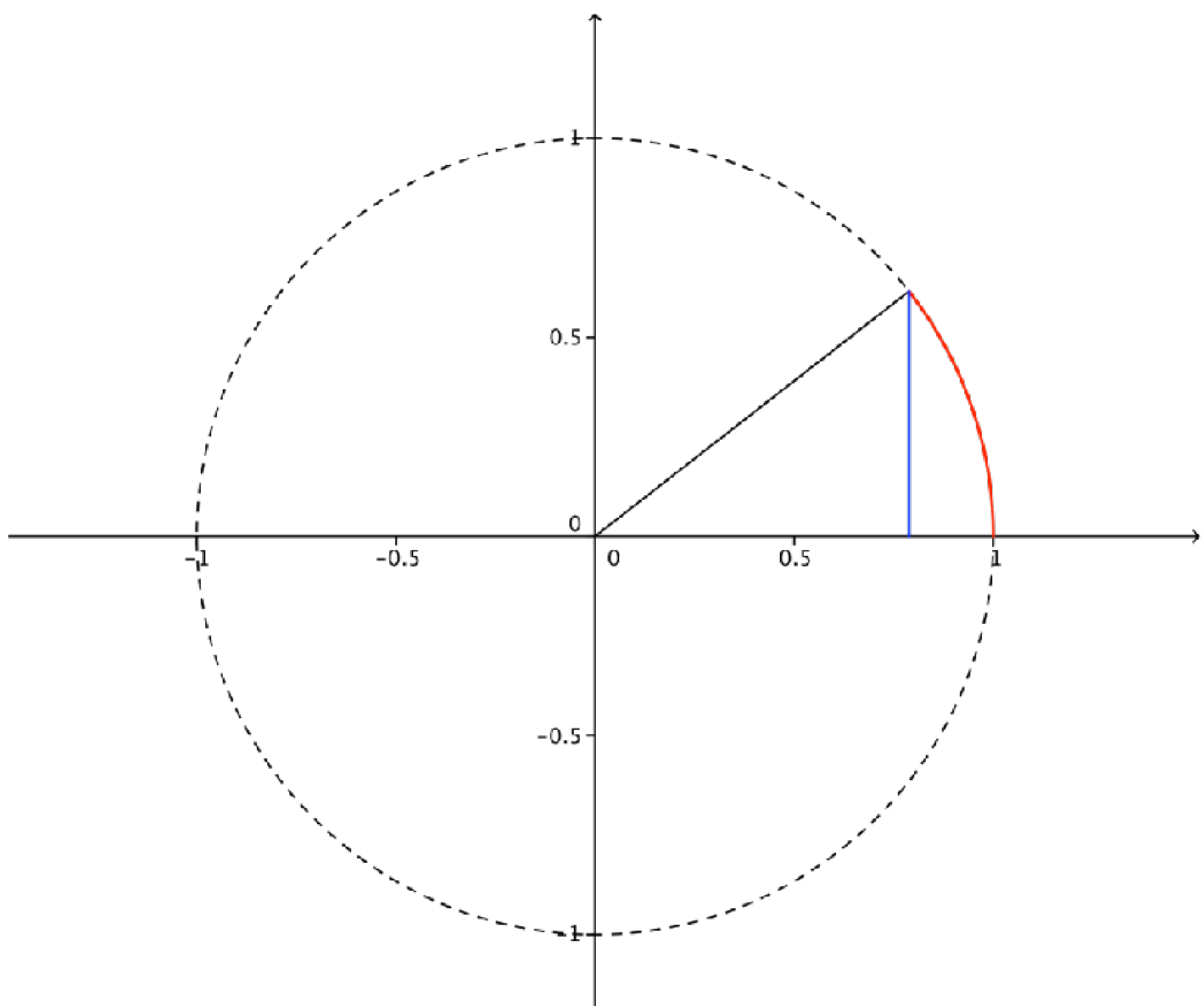
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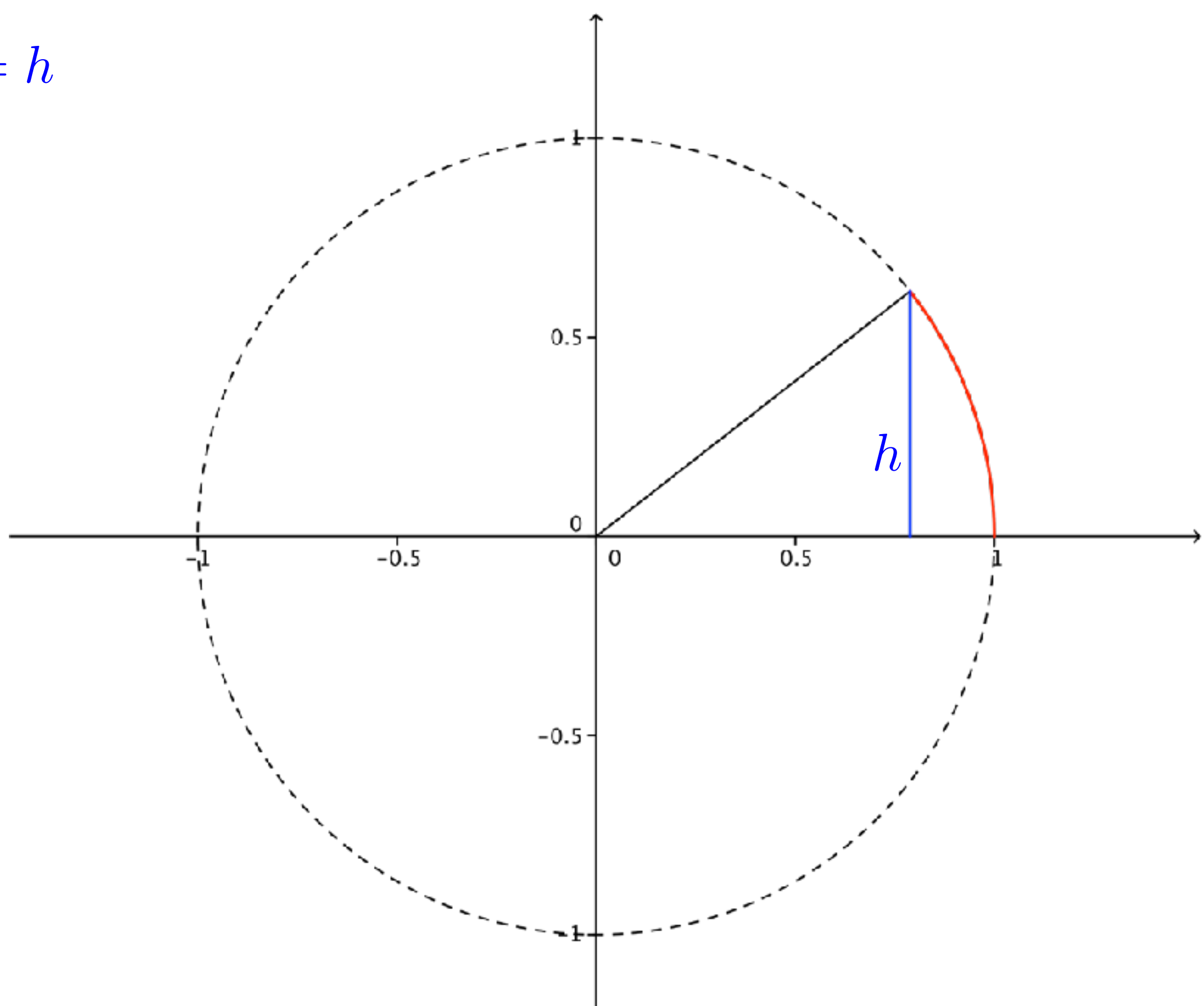
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On doit donc essayer de comprendre comment inverser le processus nous permettant de trouver les rapports trigonométriques.

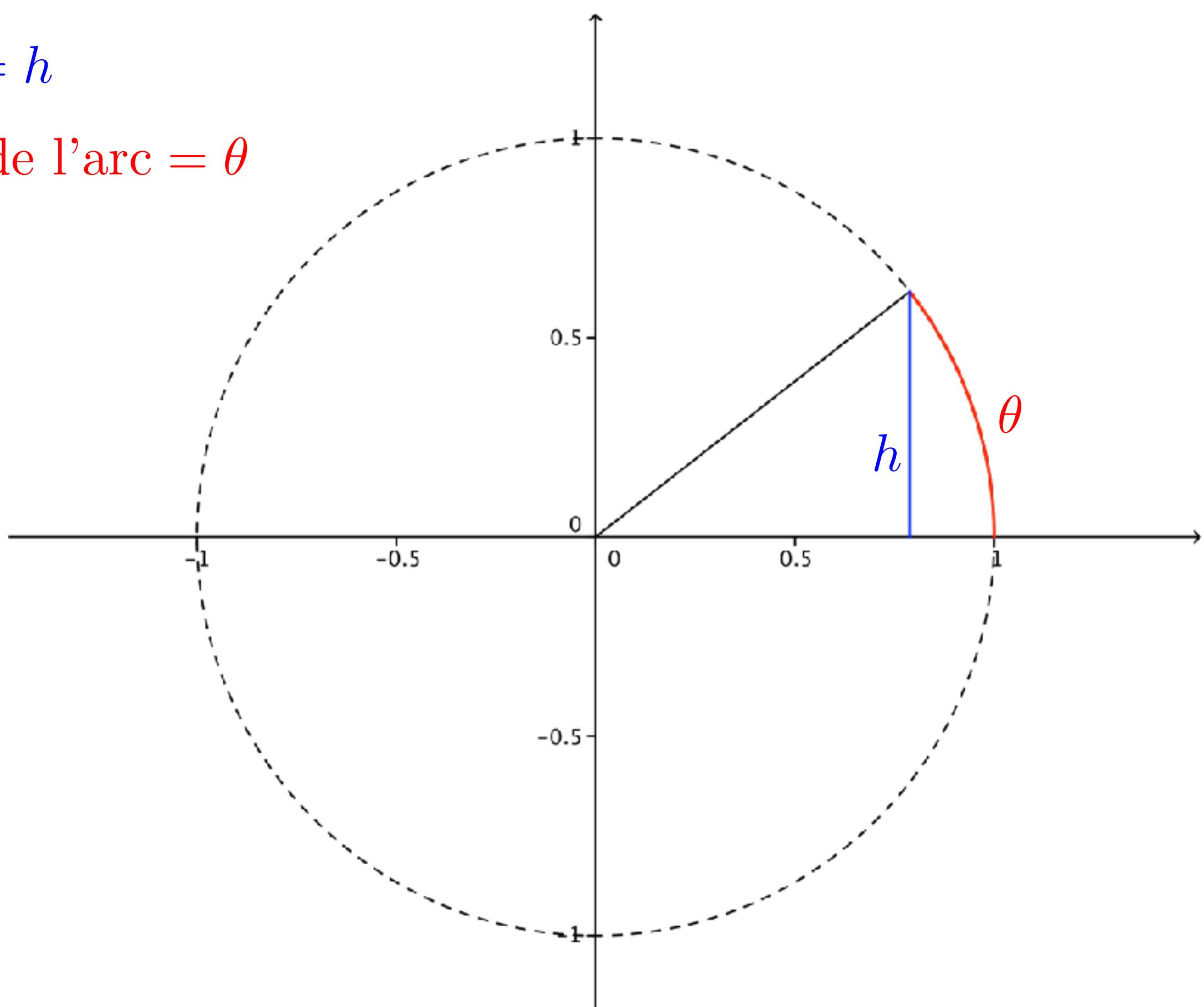


hauteur = h



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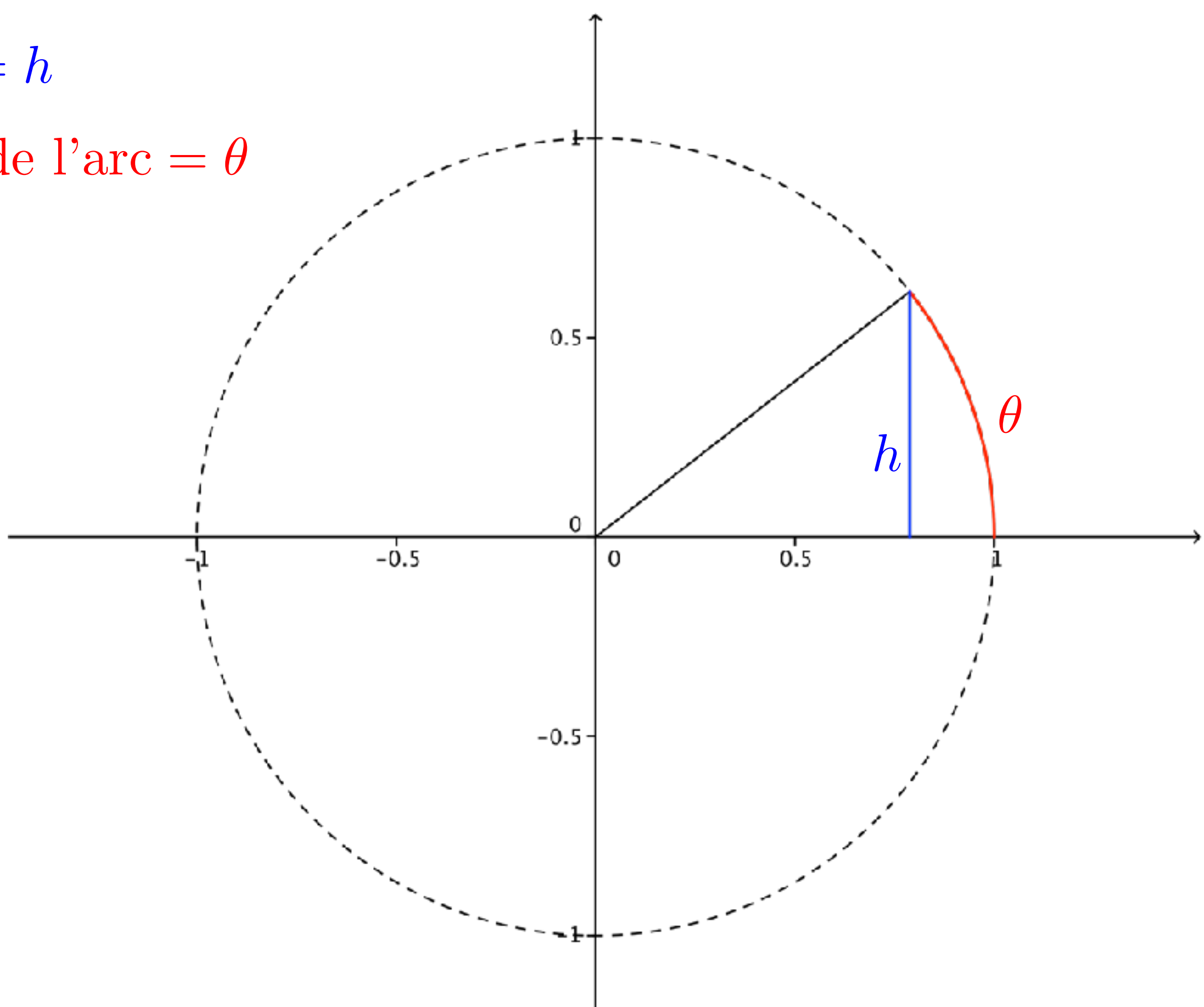
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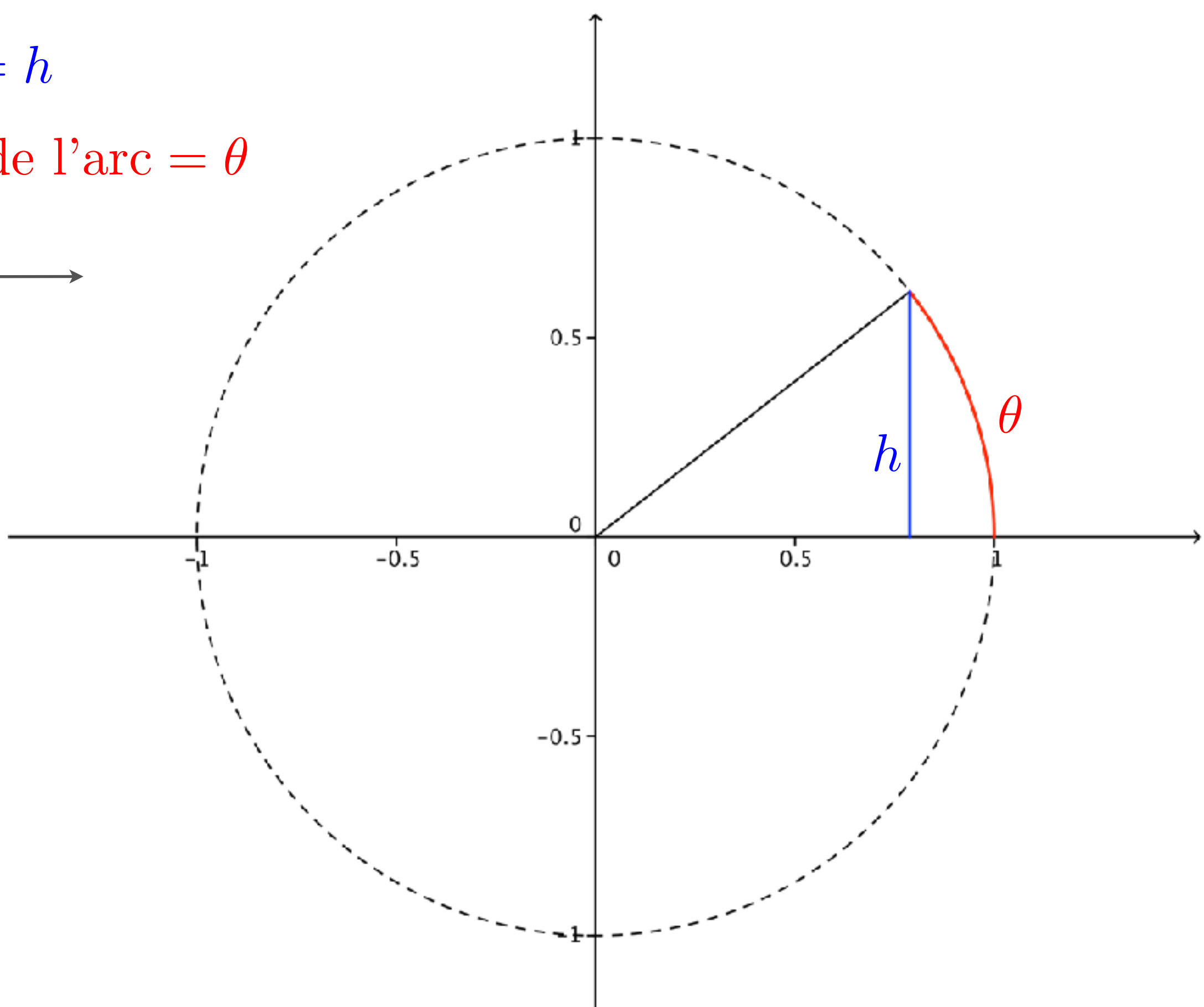
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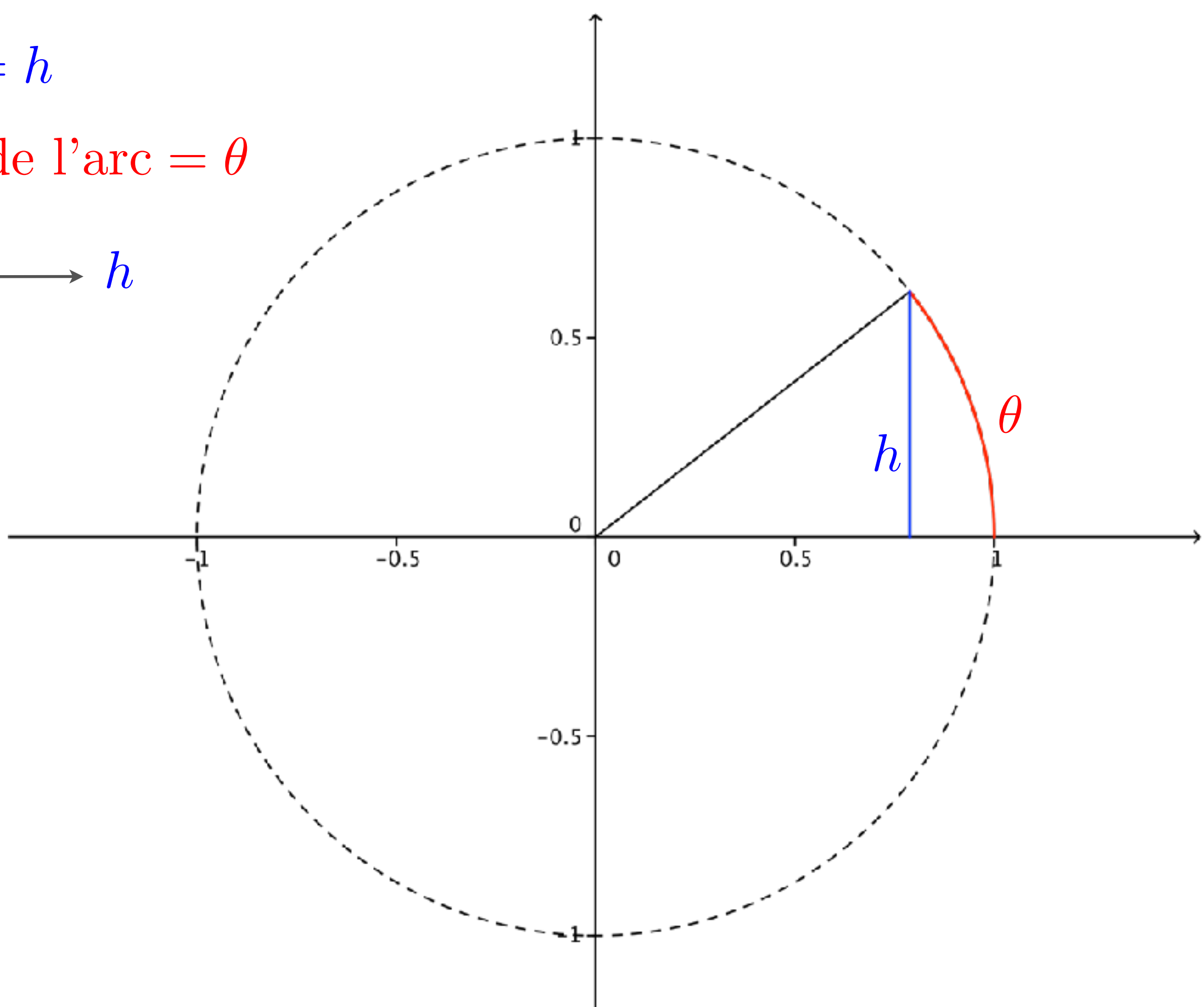
θ $\xrightarrow{\text{sin}}$



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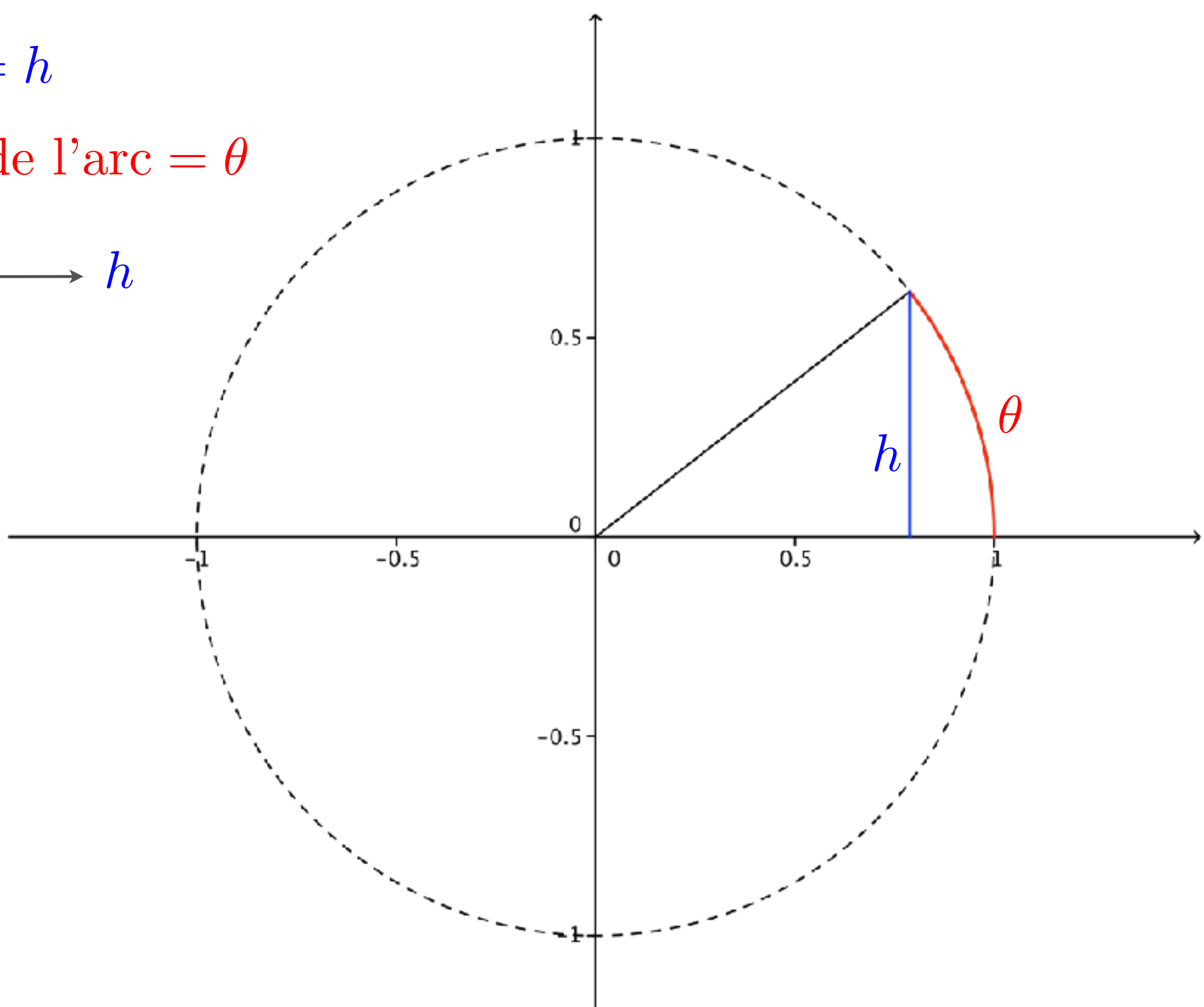


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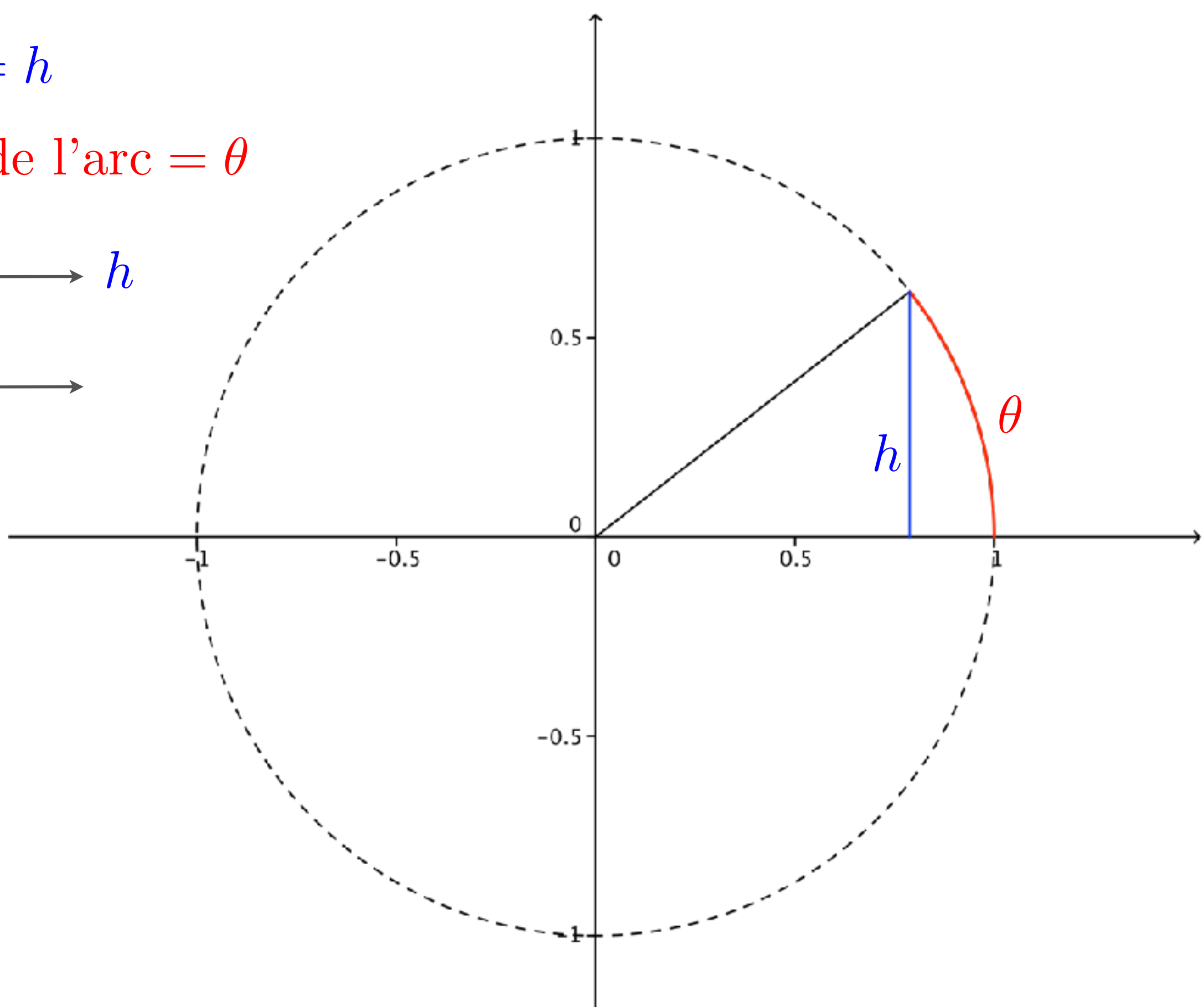


hauteur = h

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θ $\xrightarrow{\text{sin}}$ h

h $\xrightarrow{\text{arcsin}}$

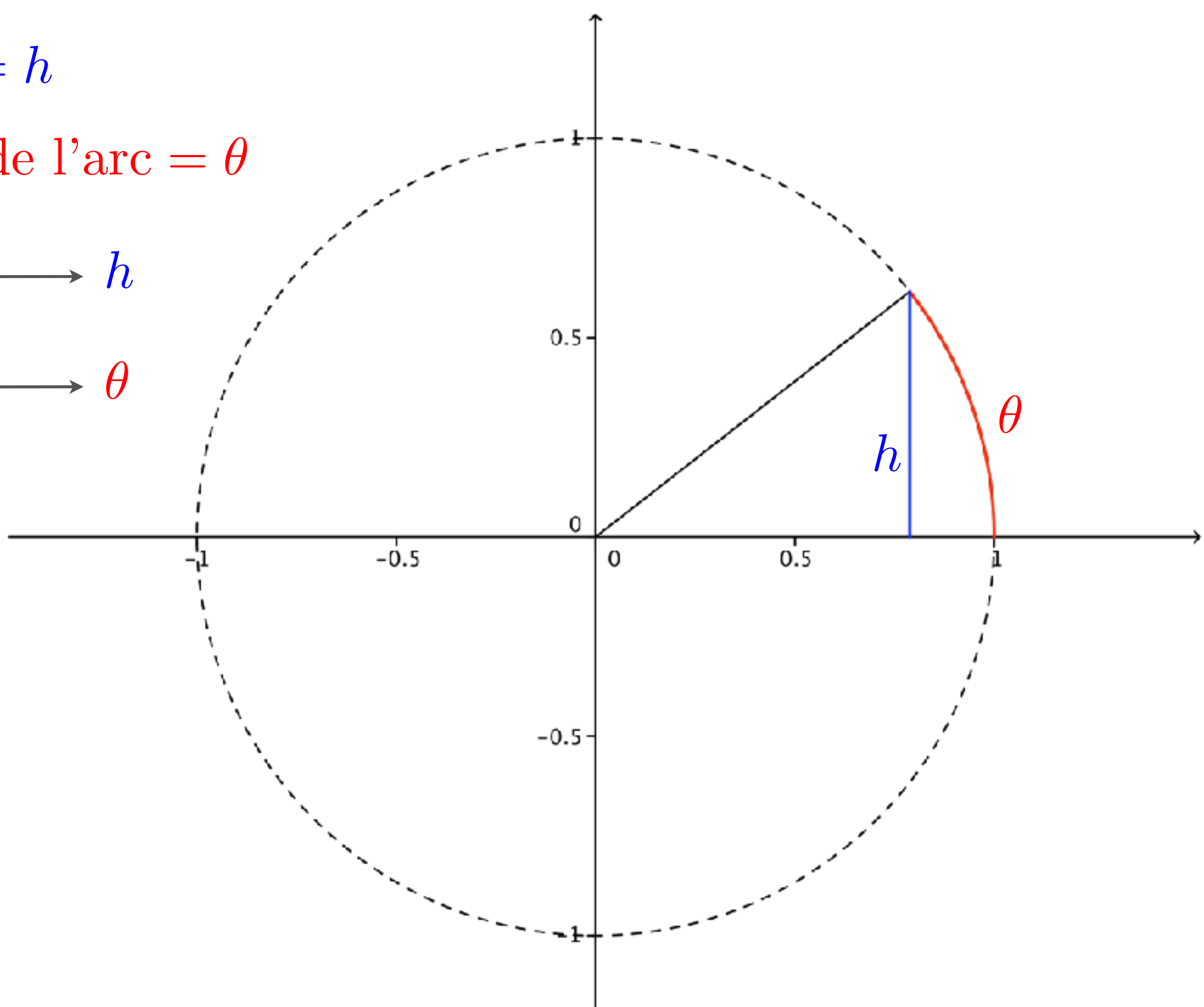


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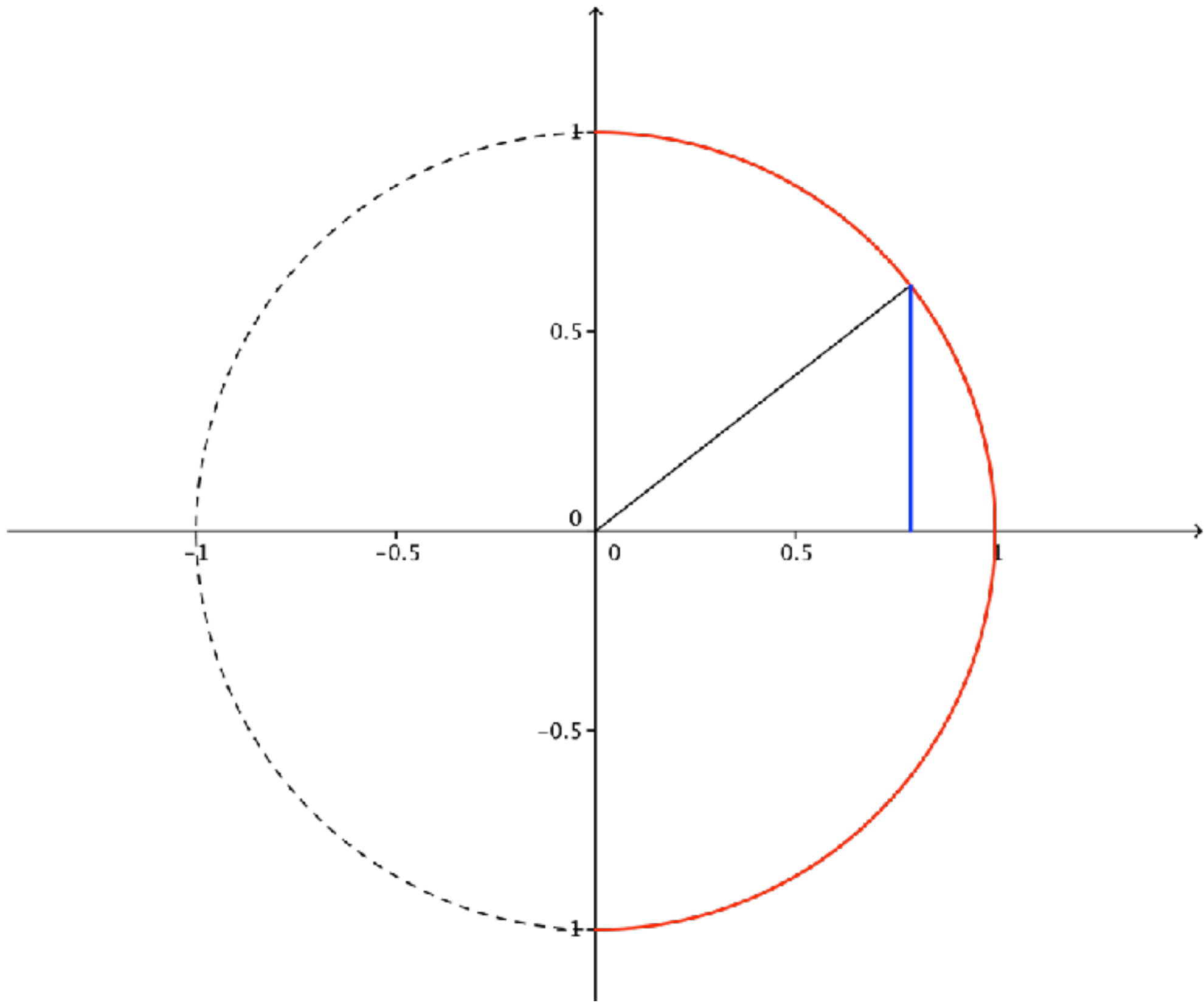
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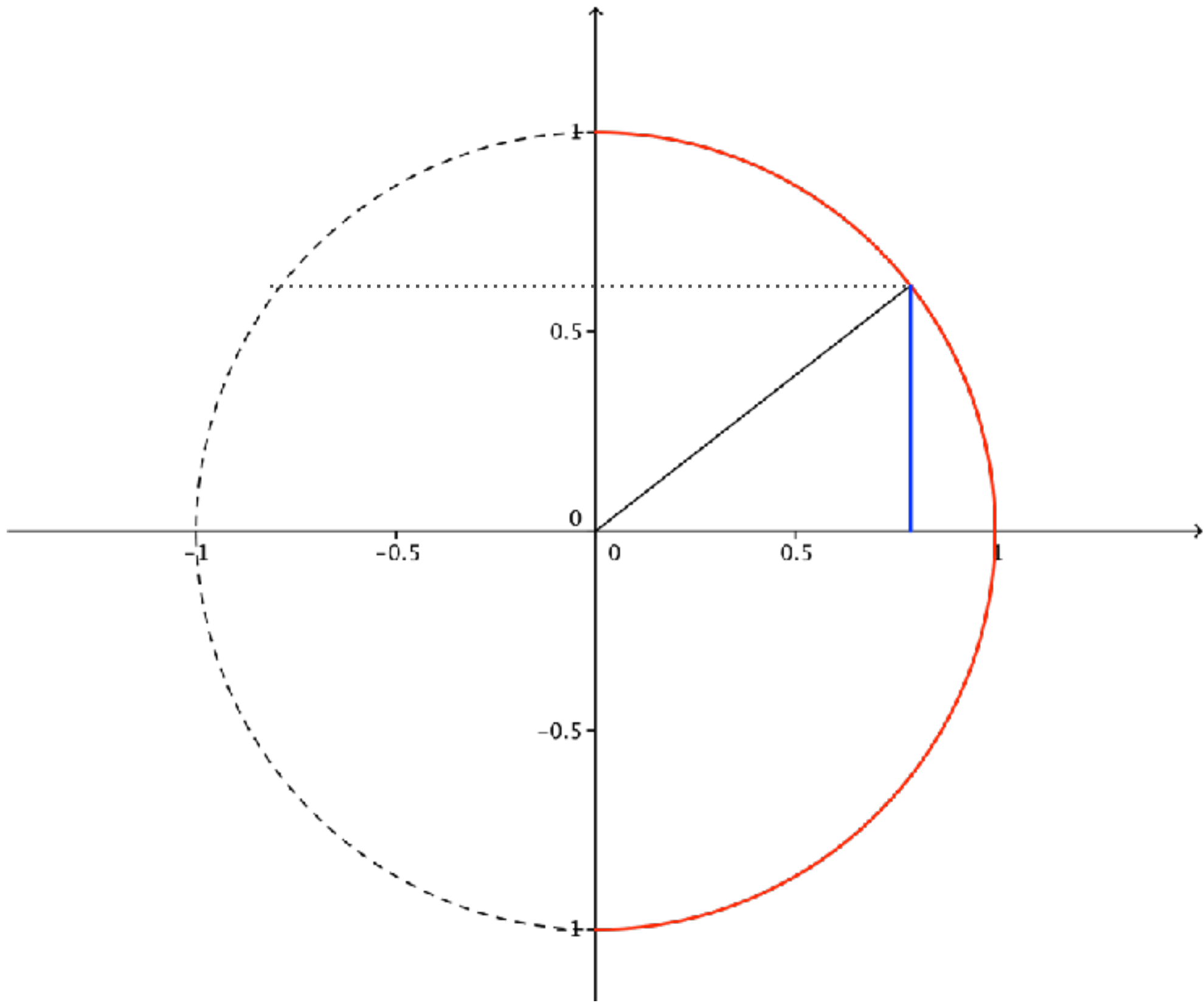
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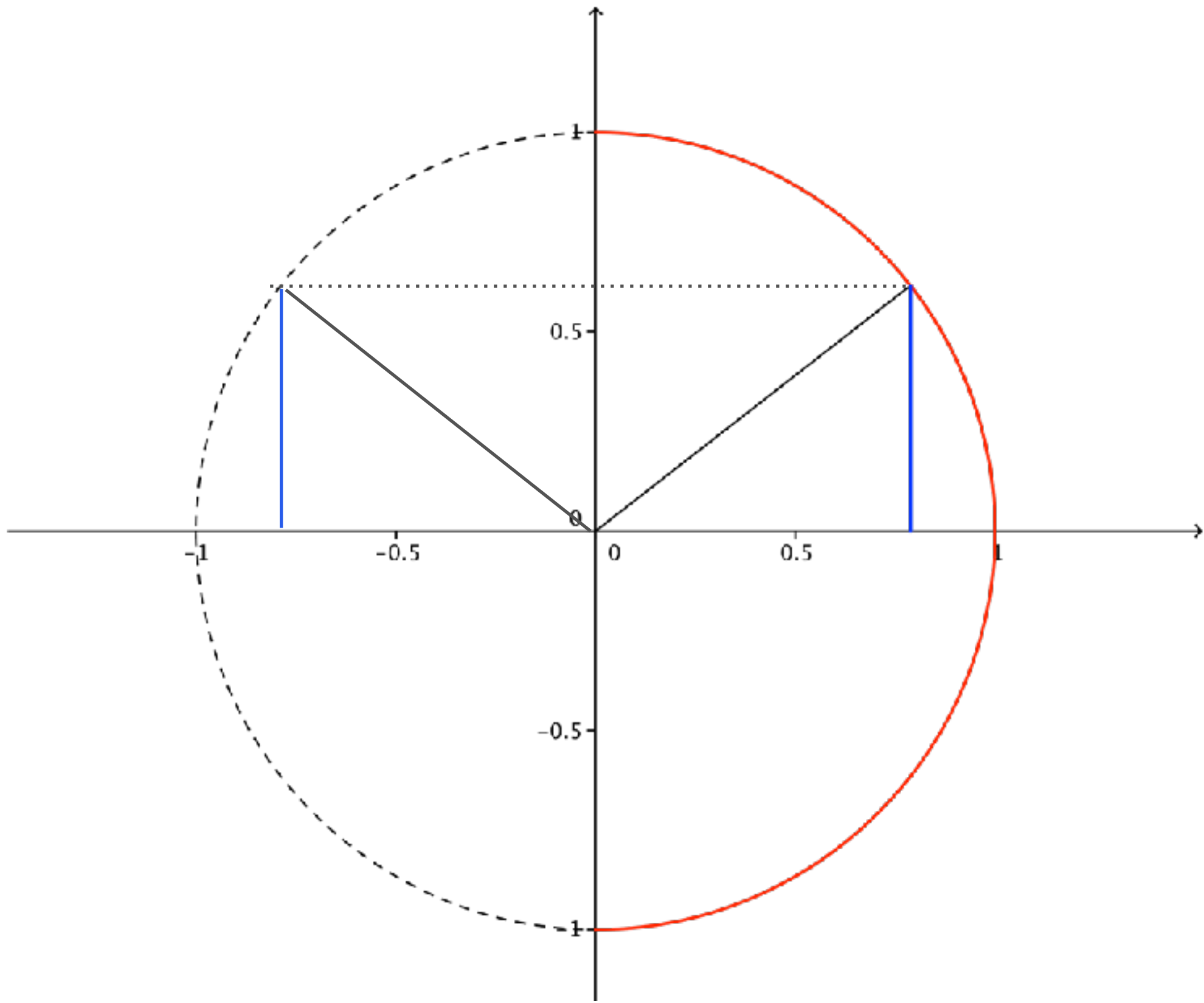
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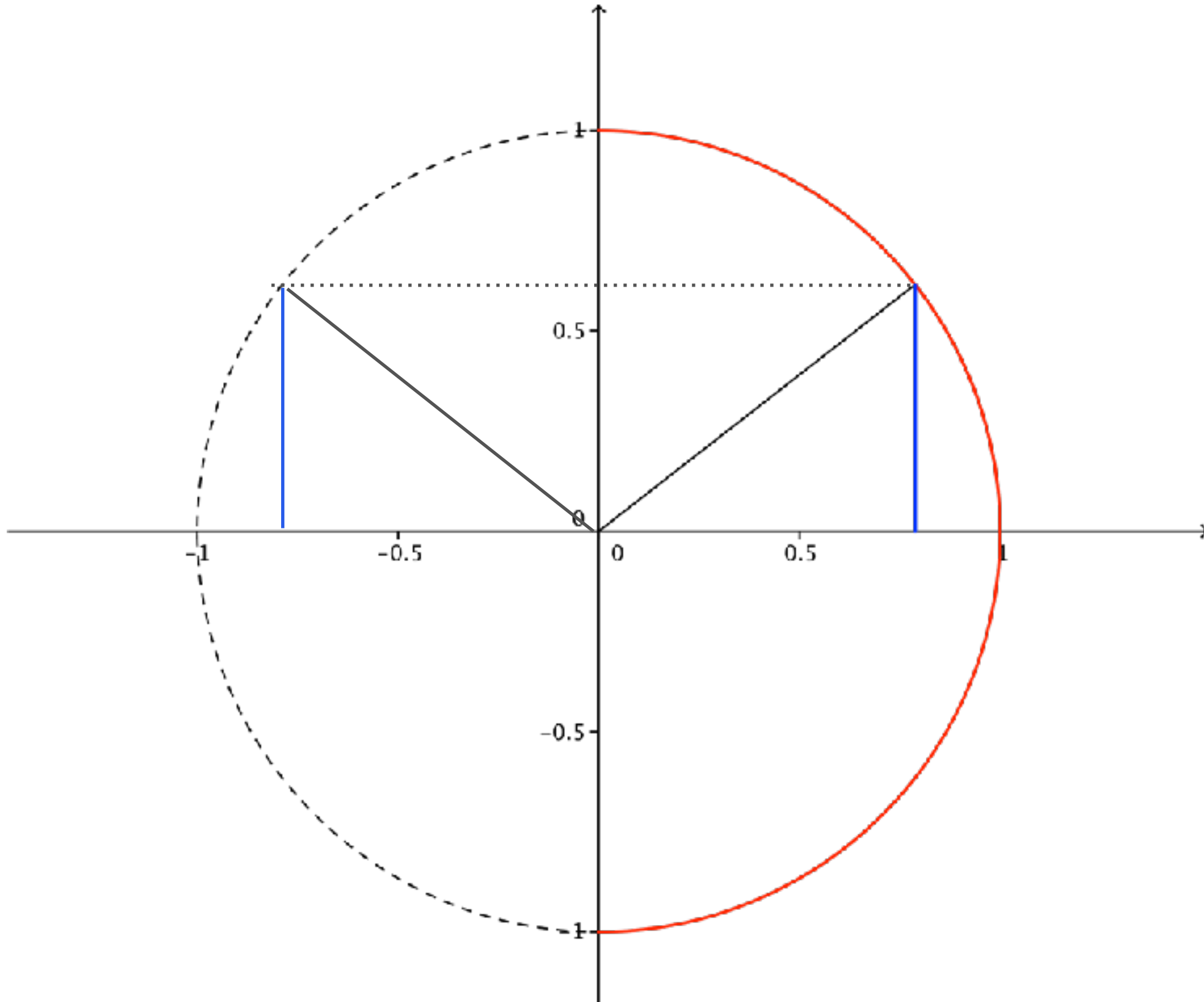
Mais on utilise
surtout ceux-là



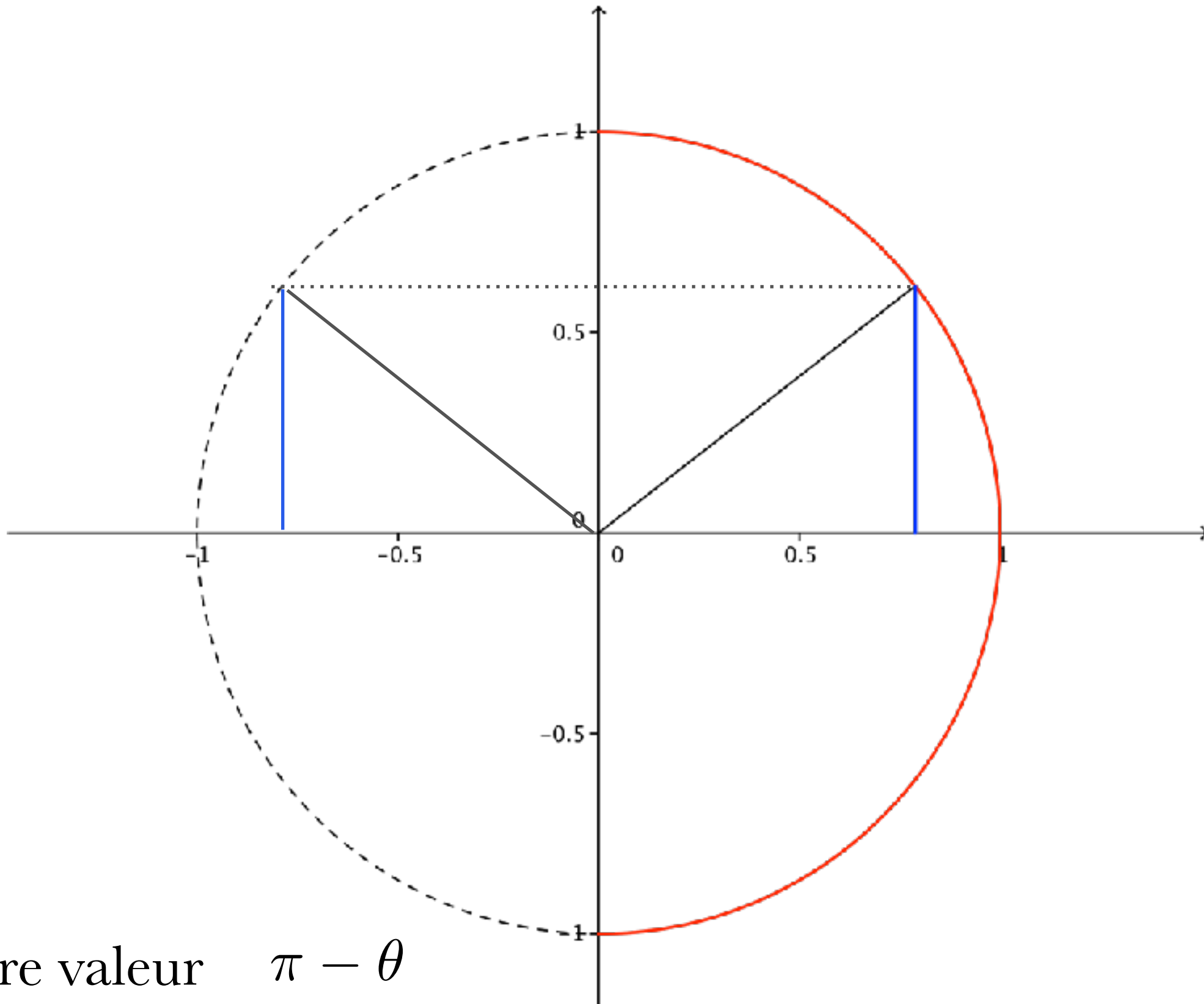




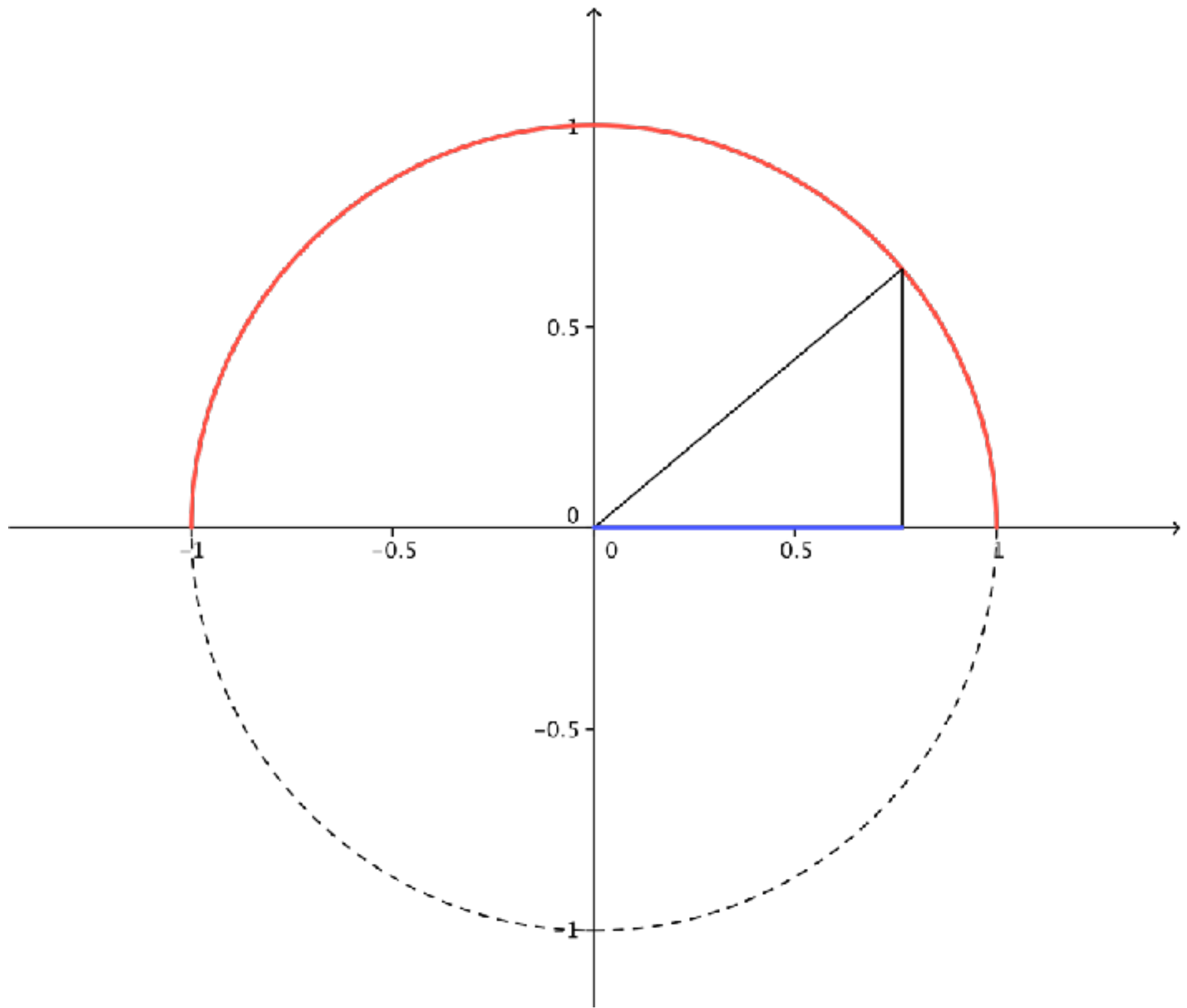
Les valeurs de $\arcsin x$ sont comprises entre $-\frac{\pi}{2}$ et $\frac{\pi}{2}$

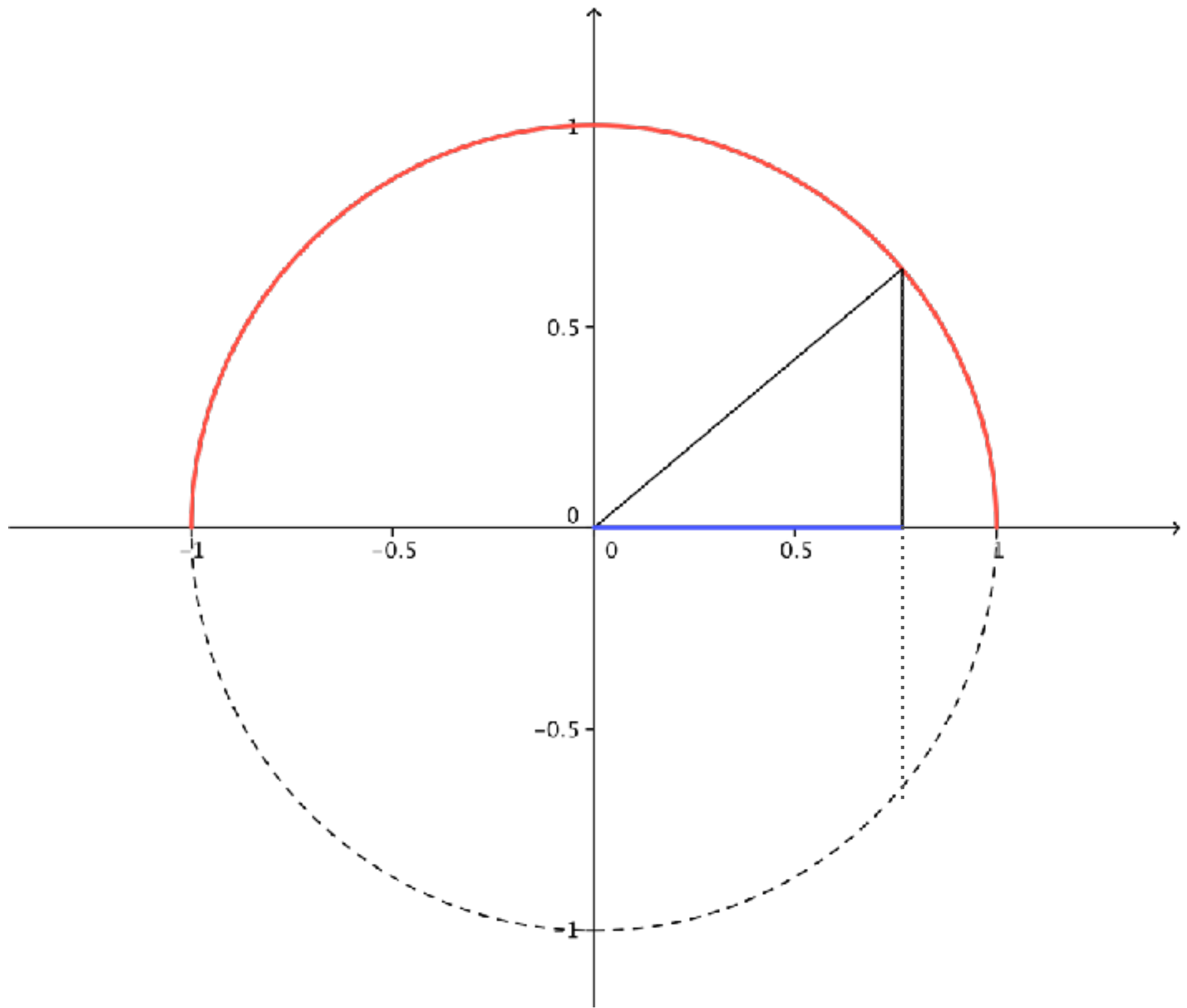


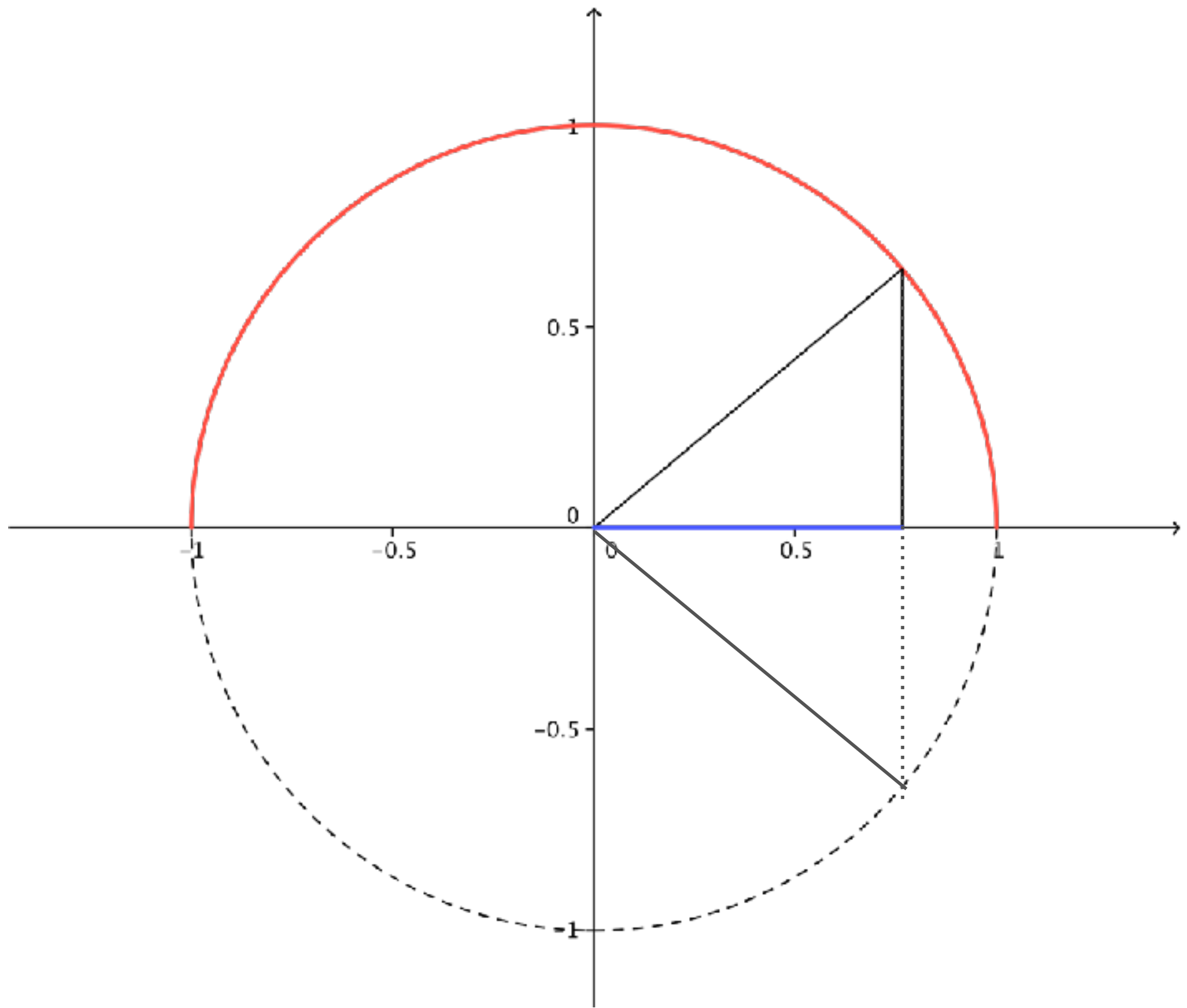
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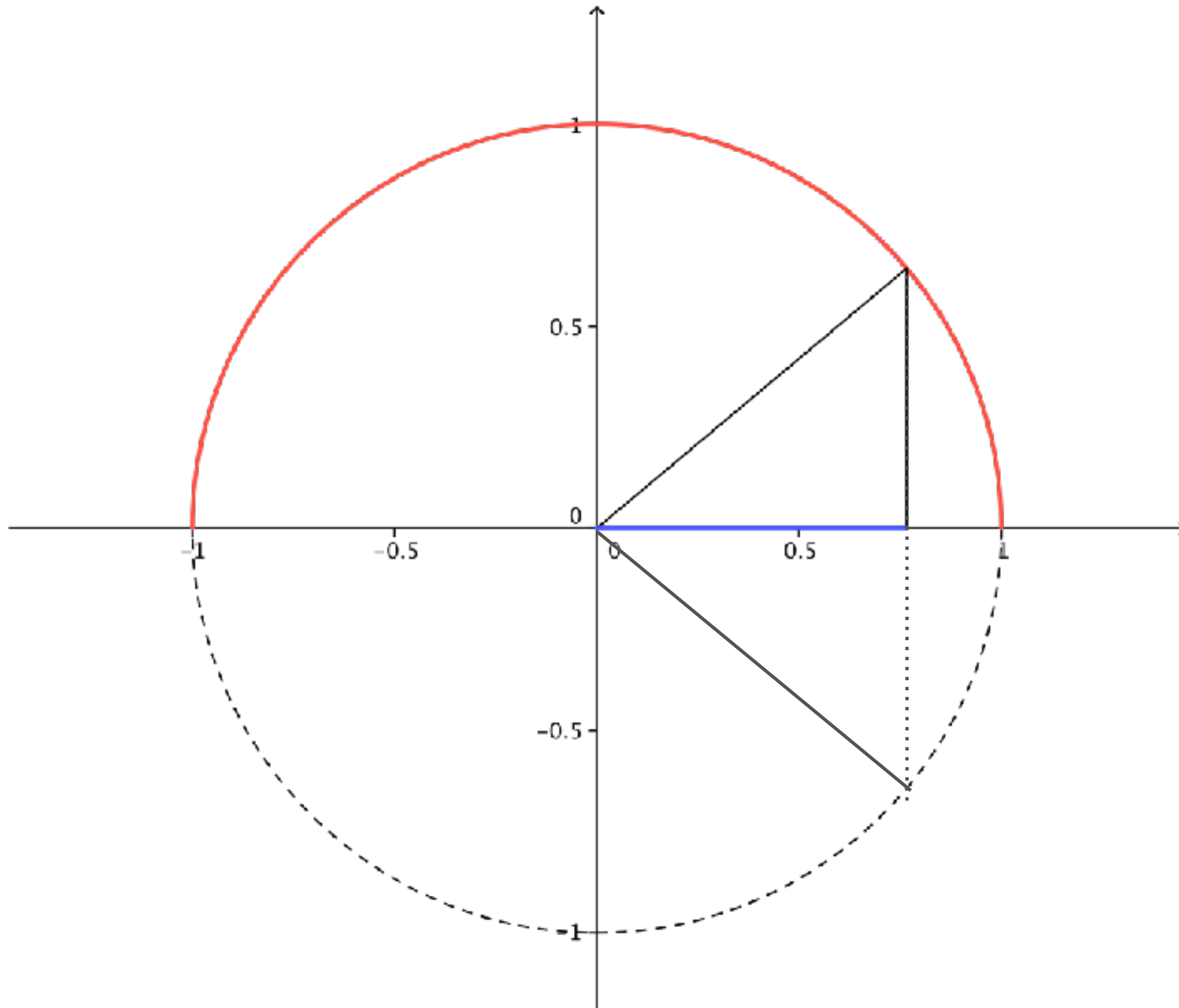
L'autre valeur $\pi - \theta$



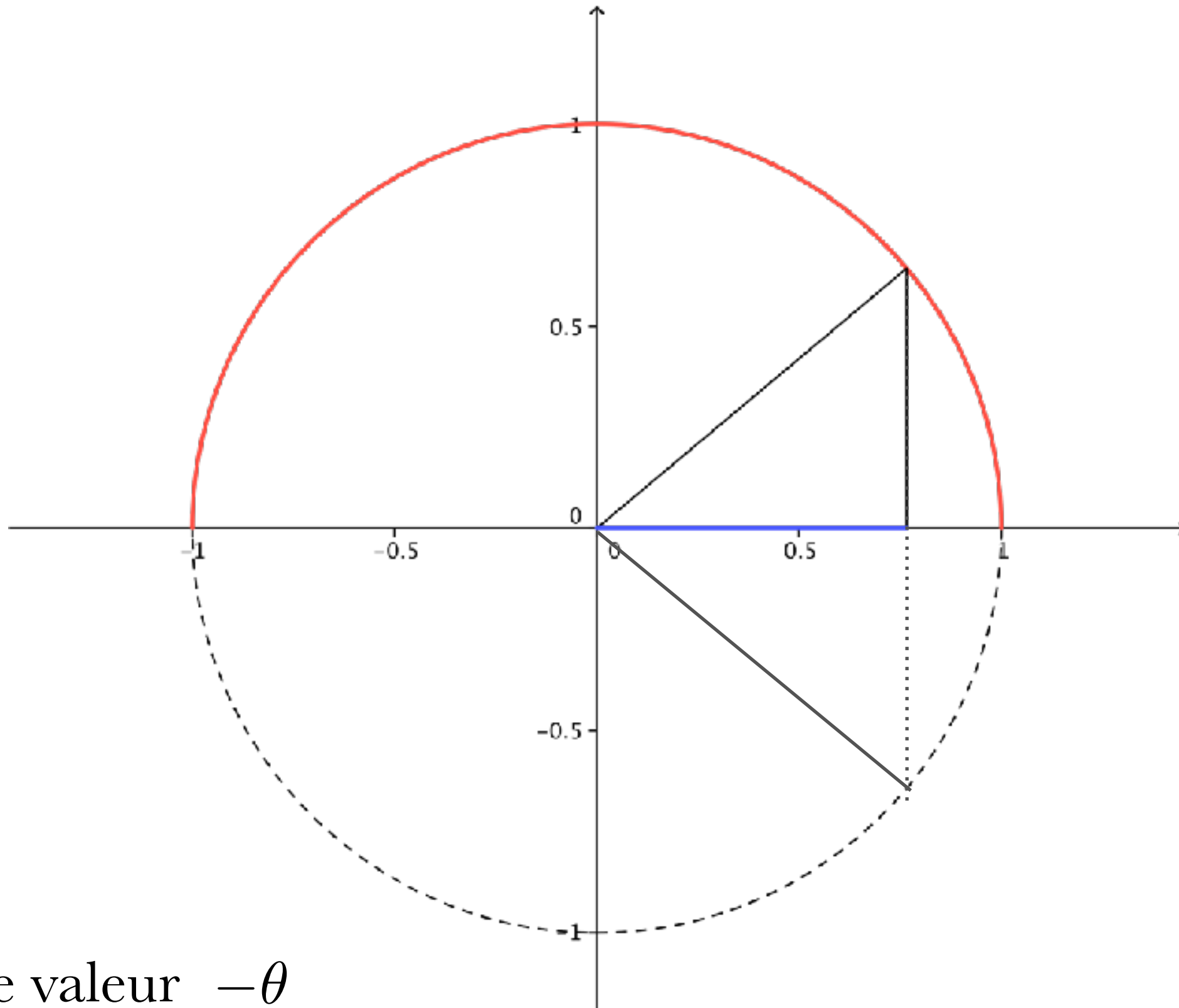




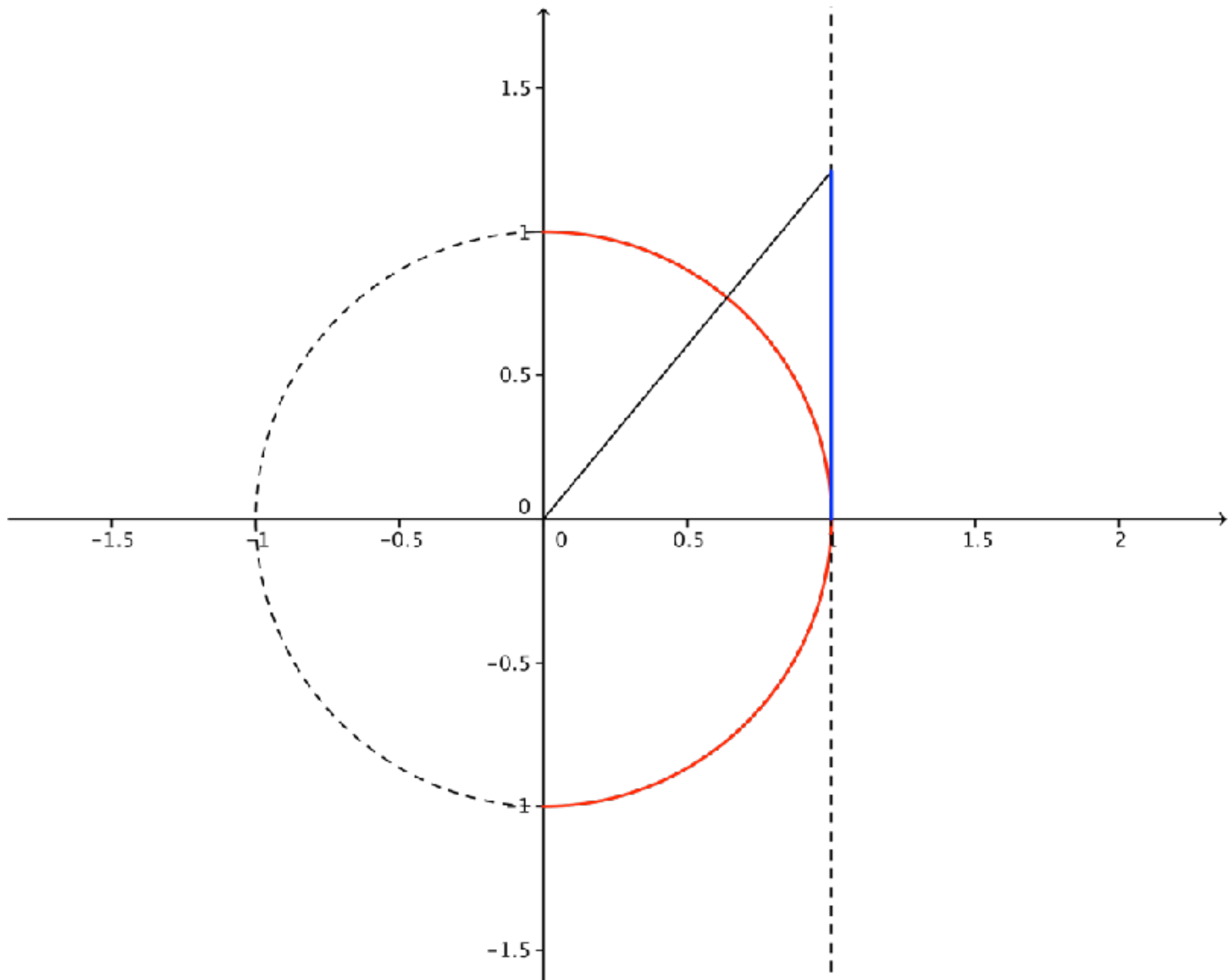
Les valeurs de $\arccos x$ sont comprises entre 0 et π

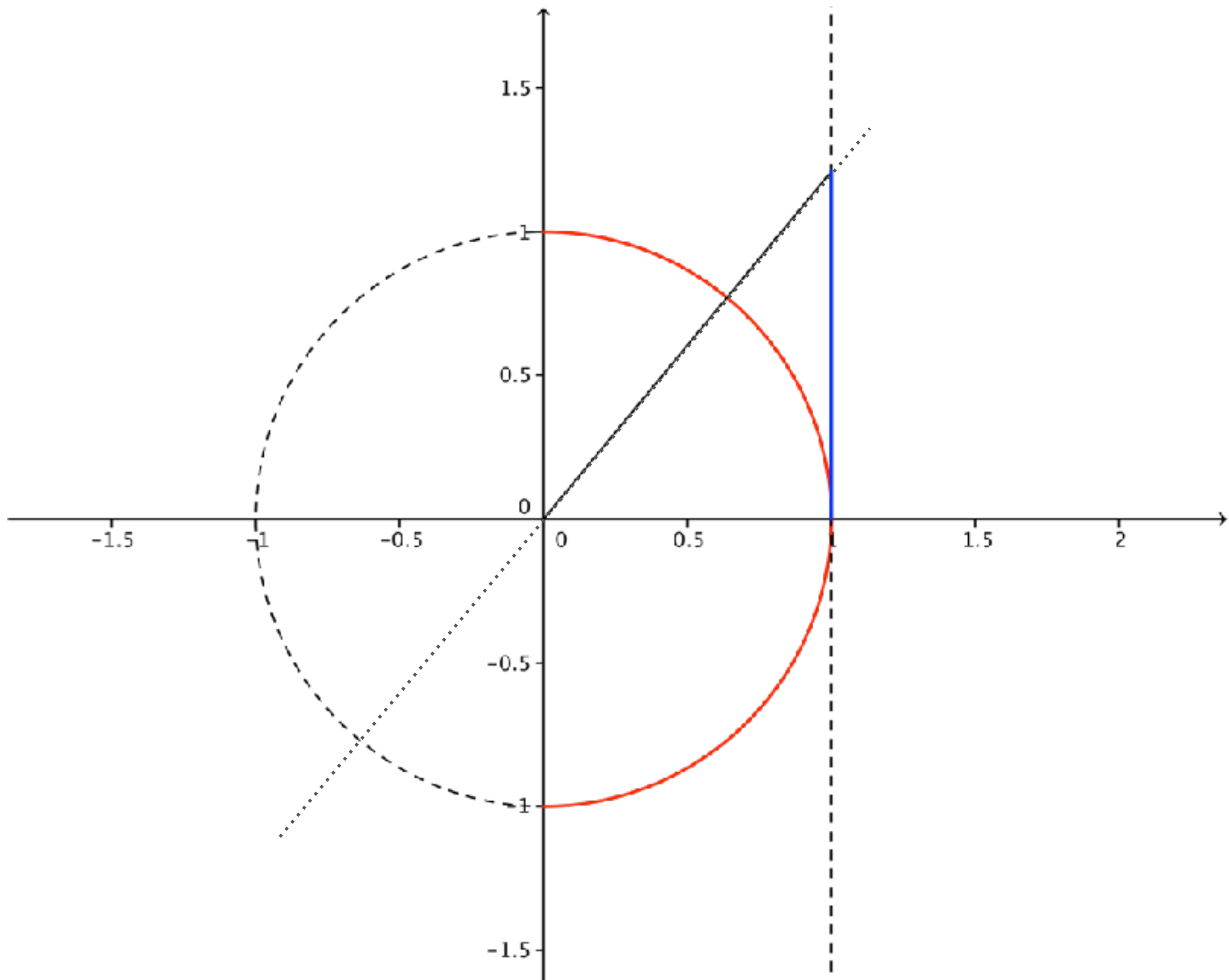


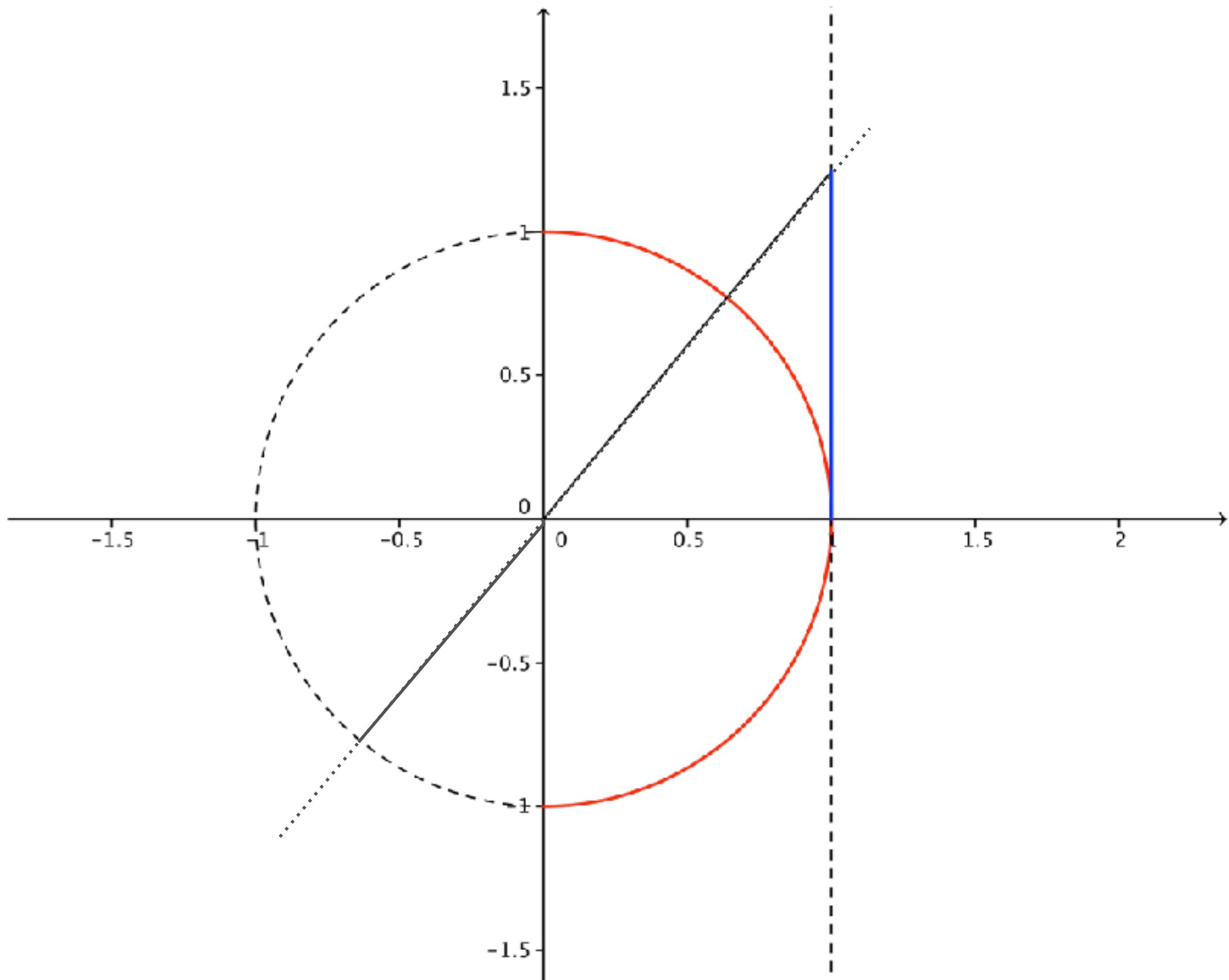
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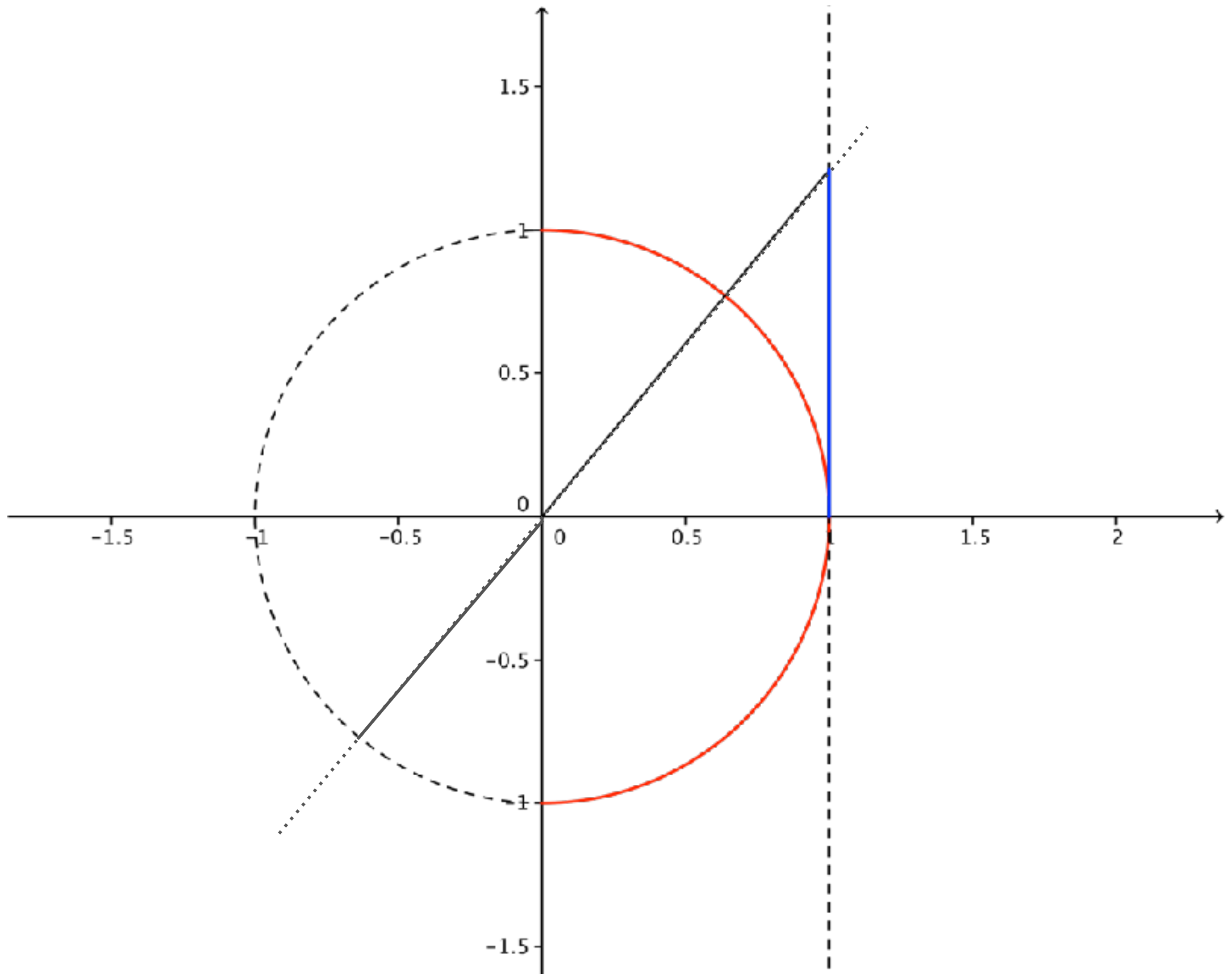
L'autre valeur $-\theta$



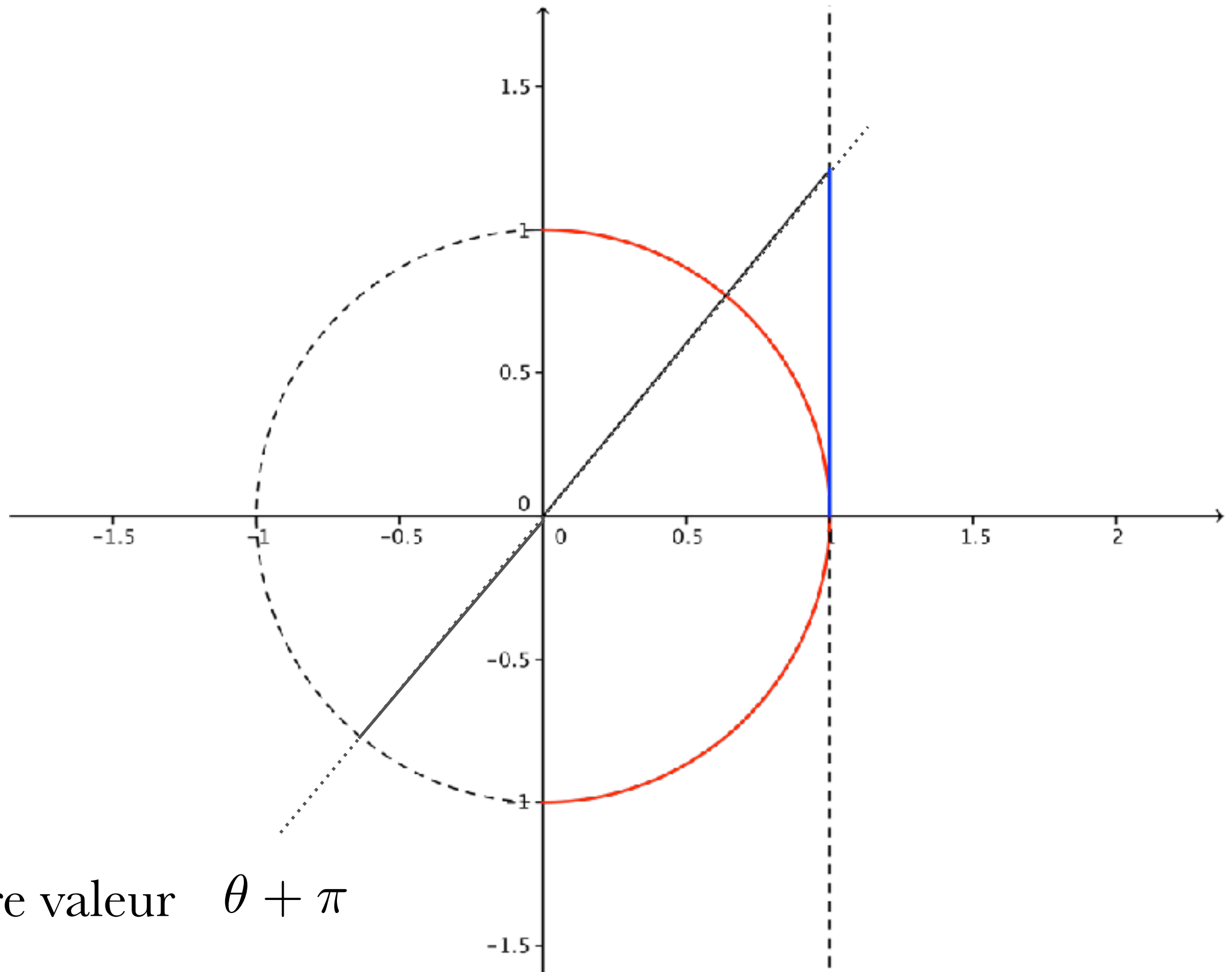




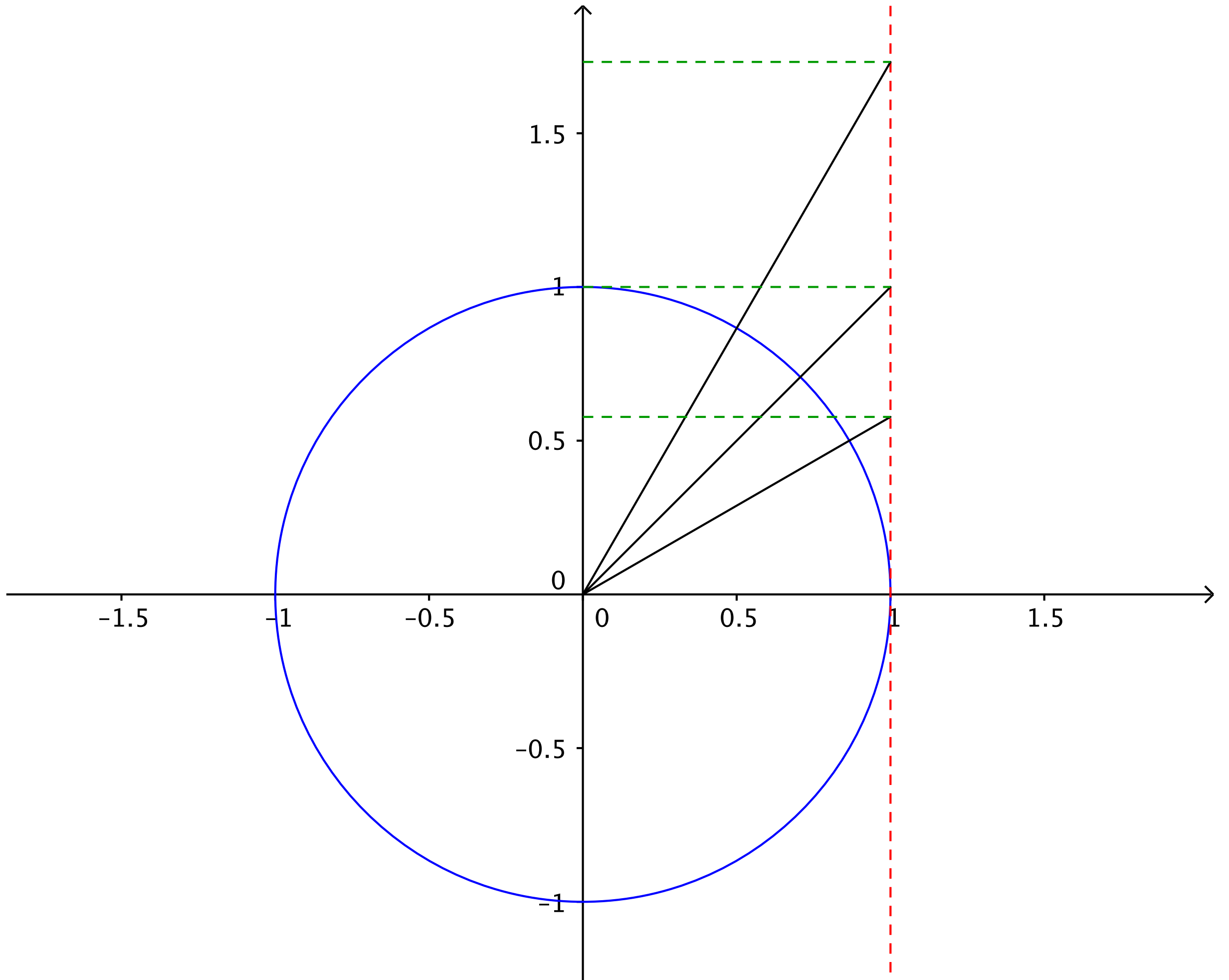
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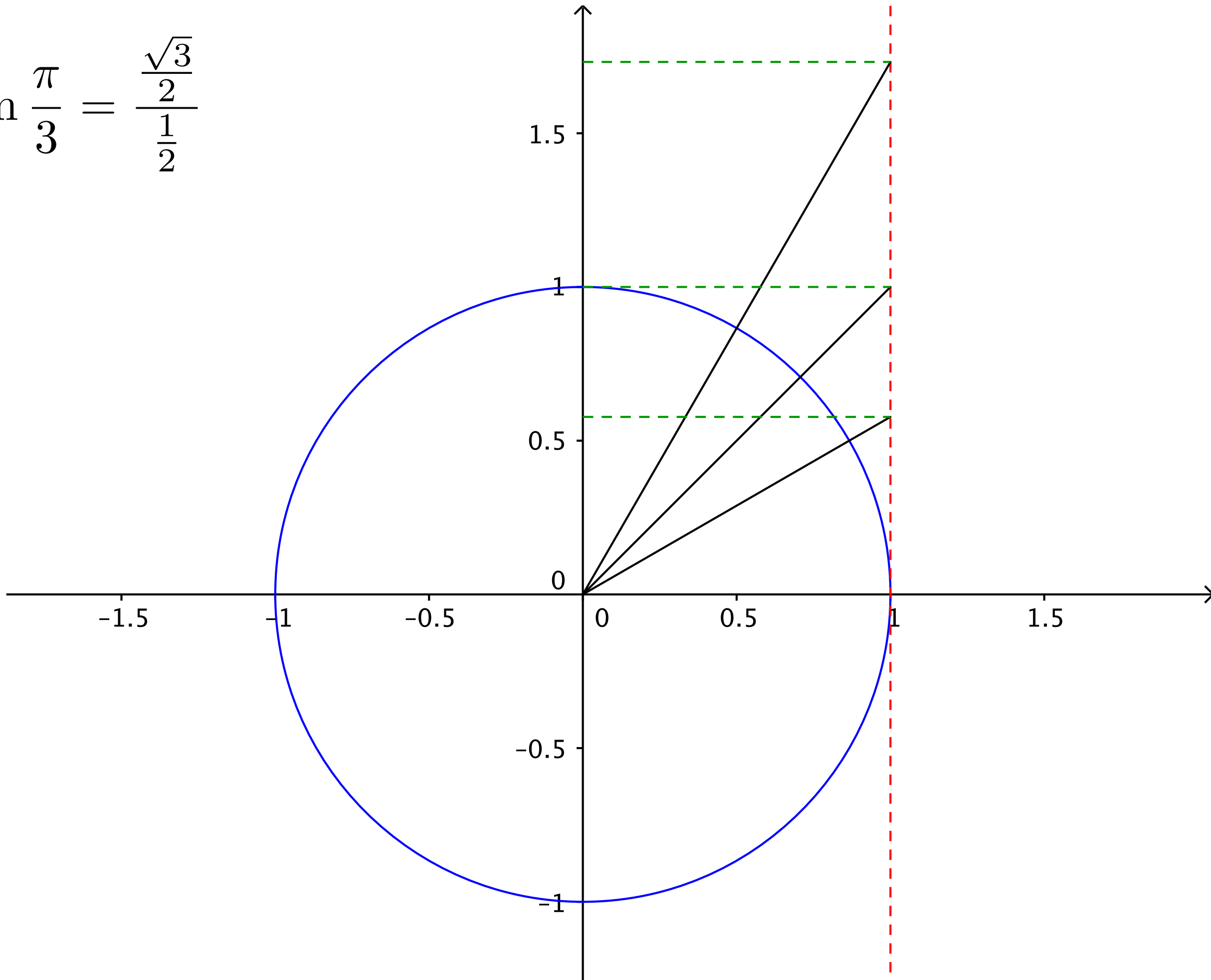
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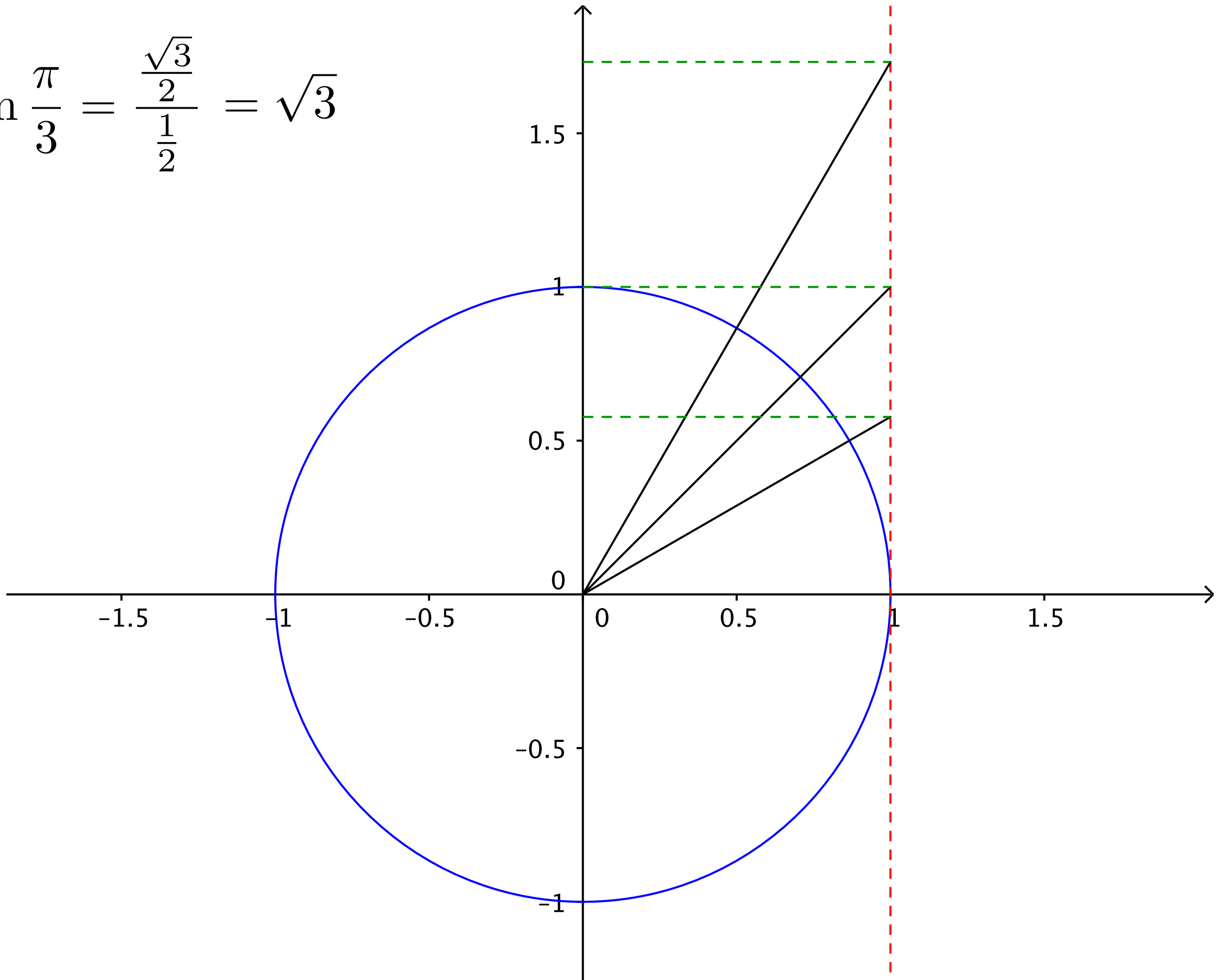
L'autre valeur $\theta + \pi$



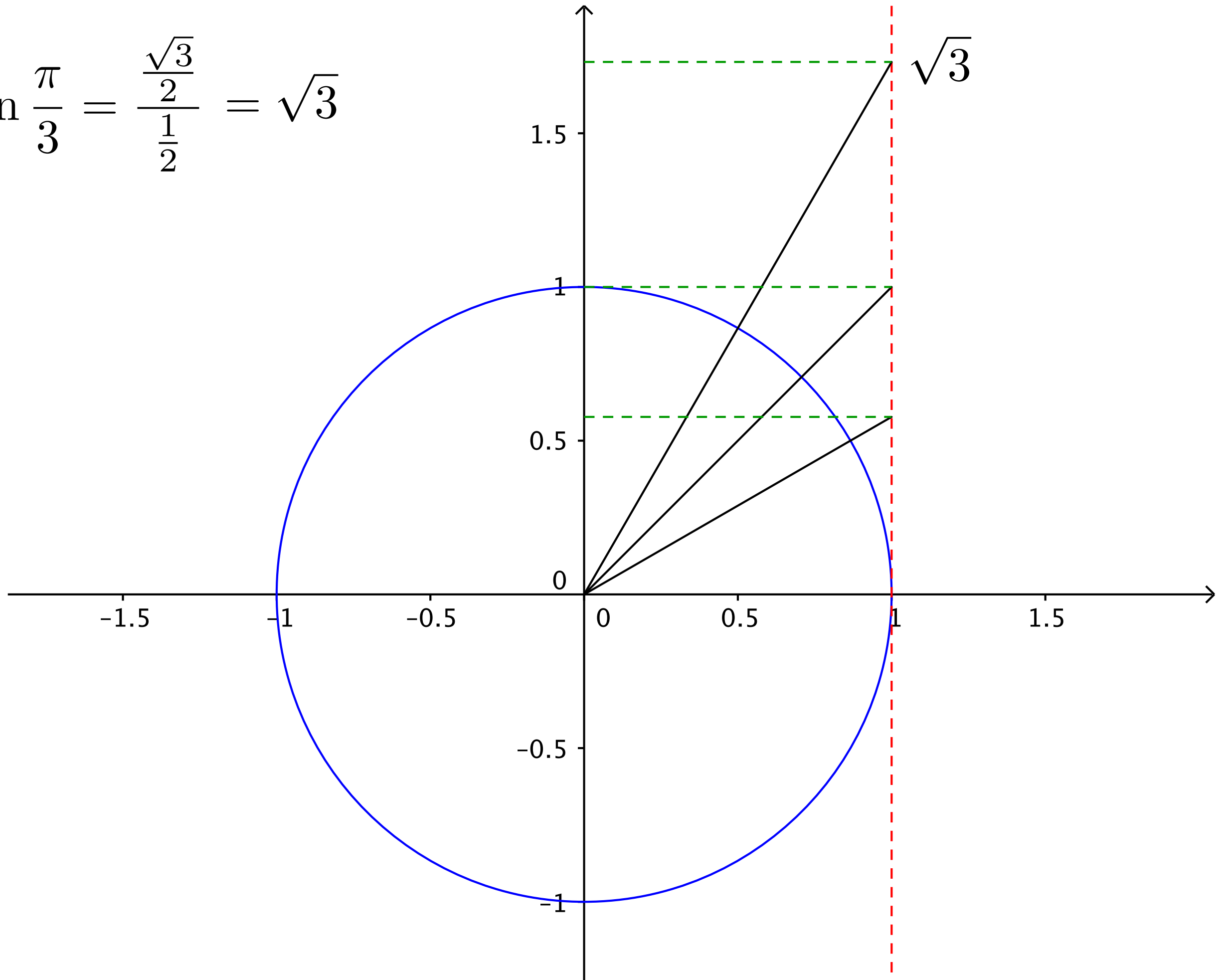
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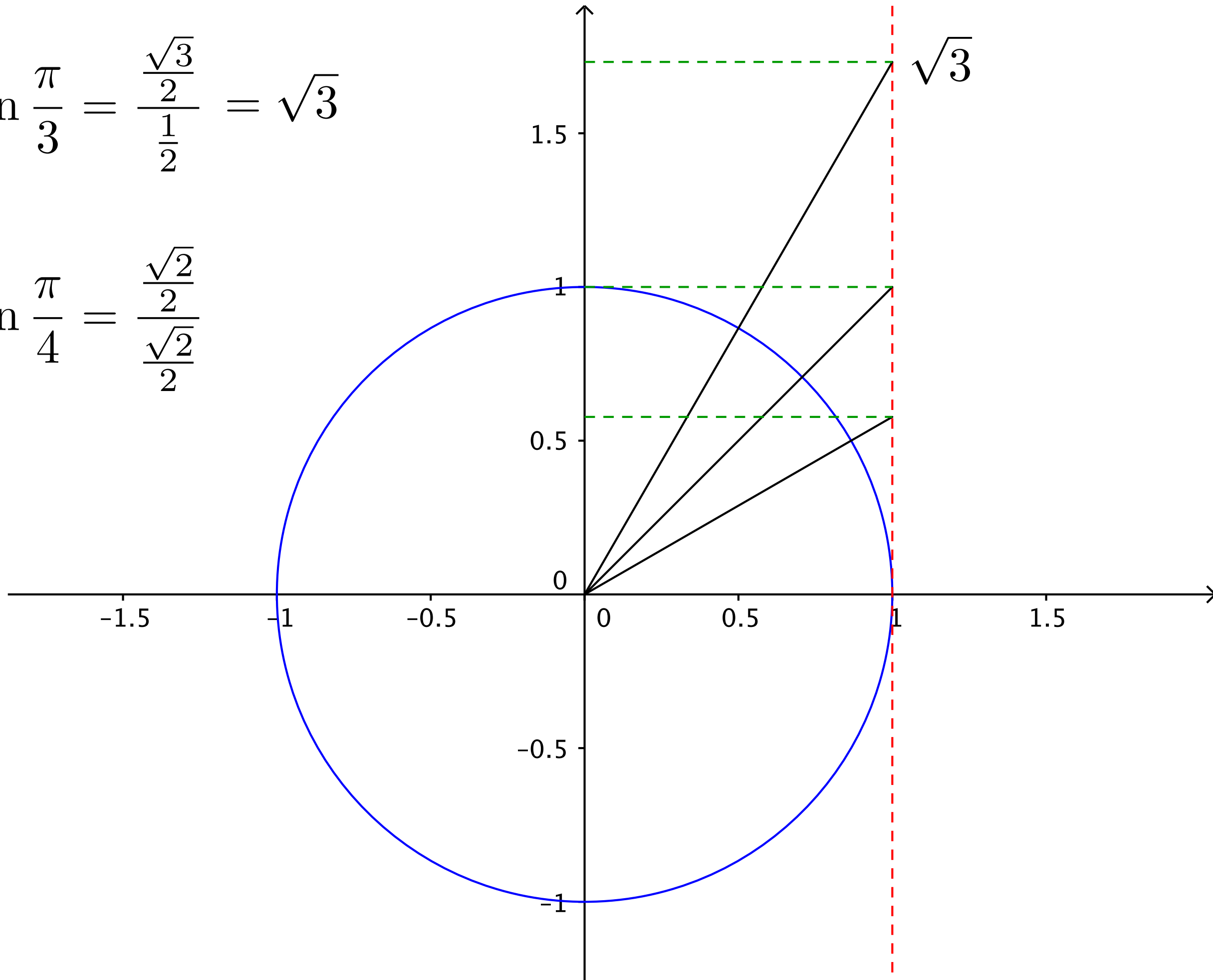


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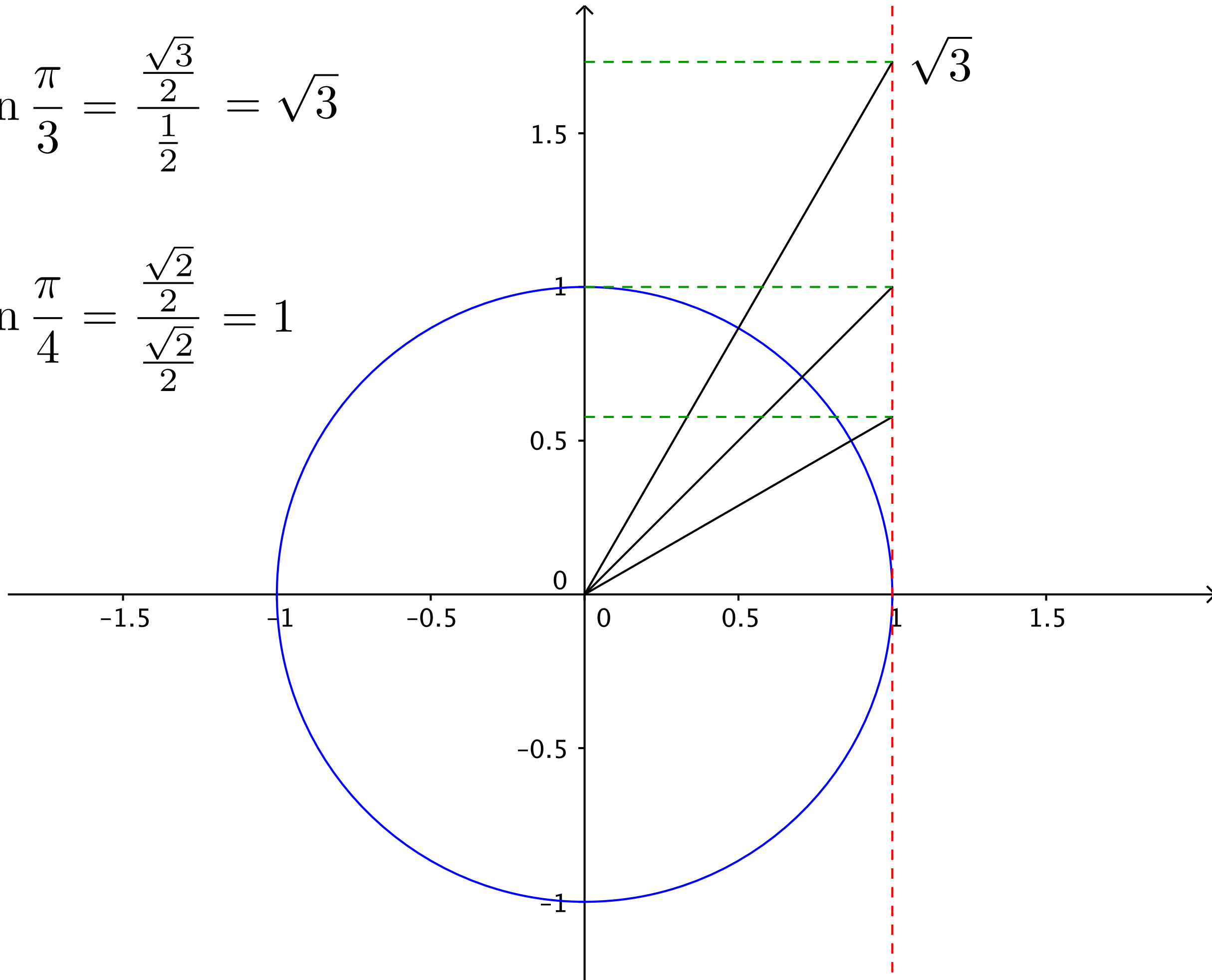
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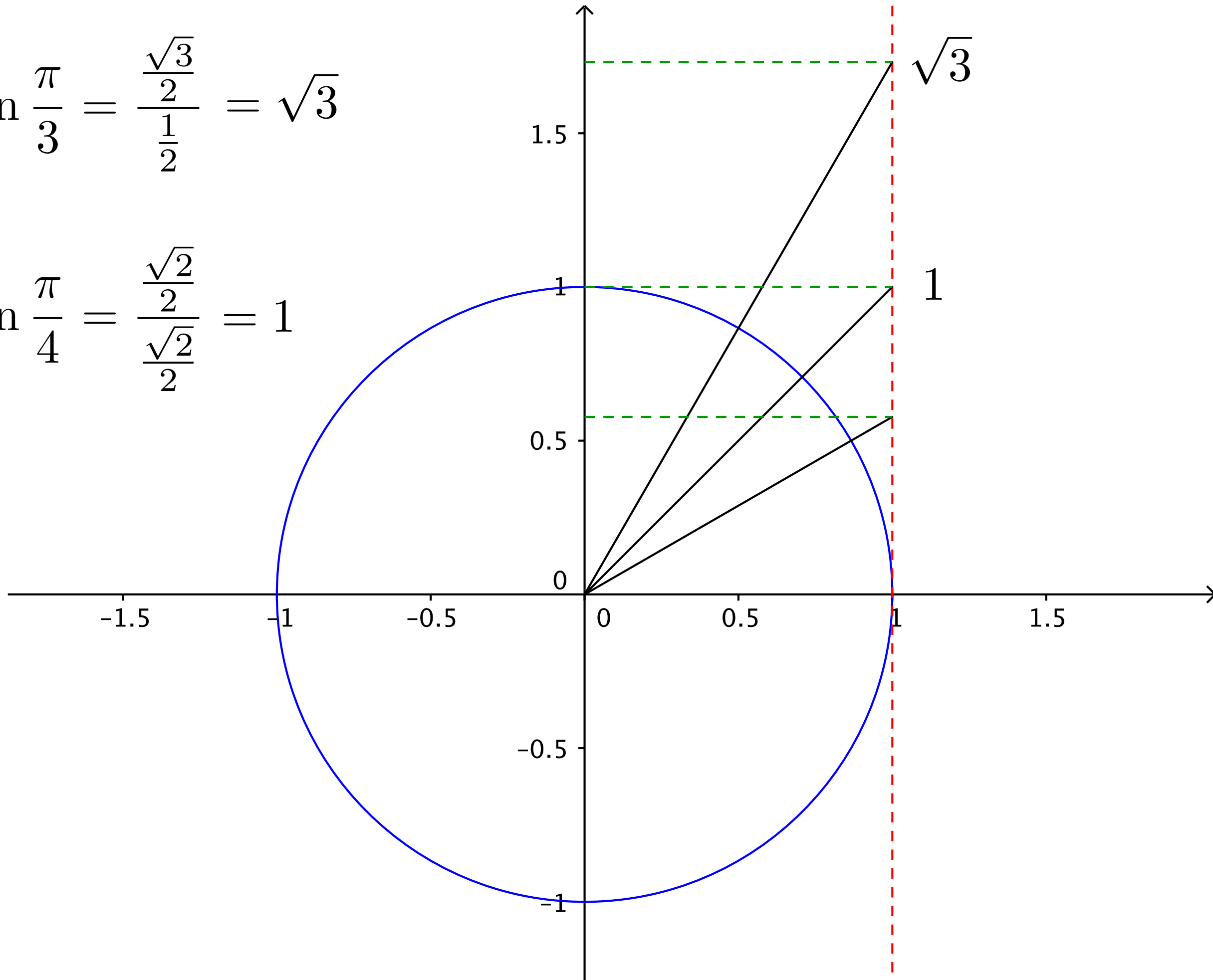
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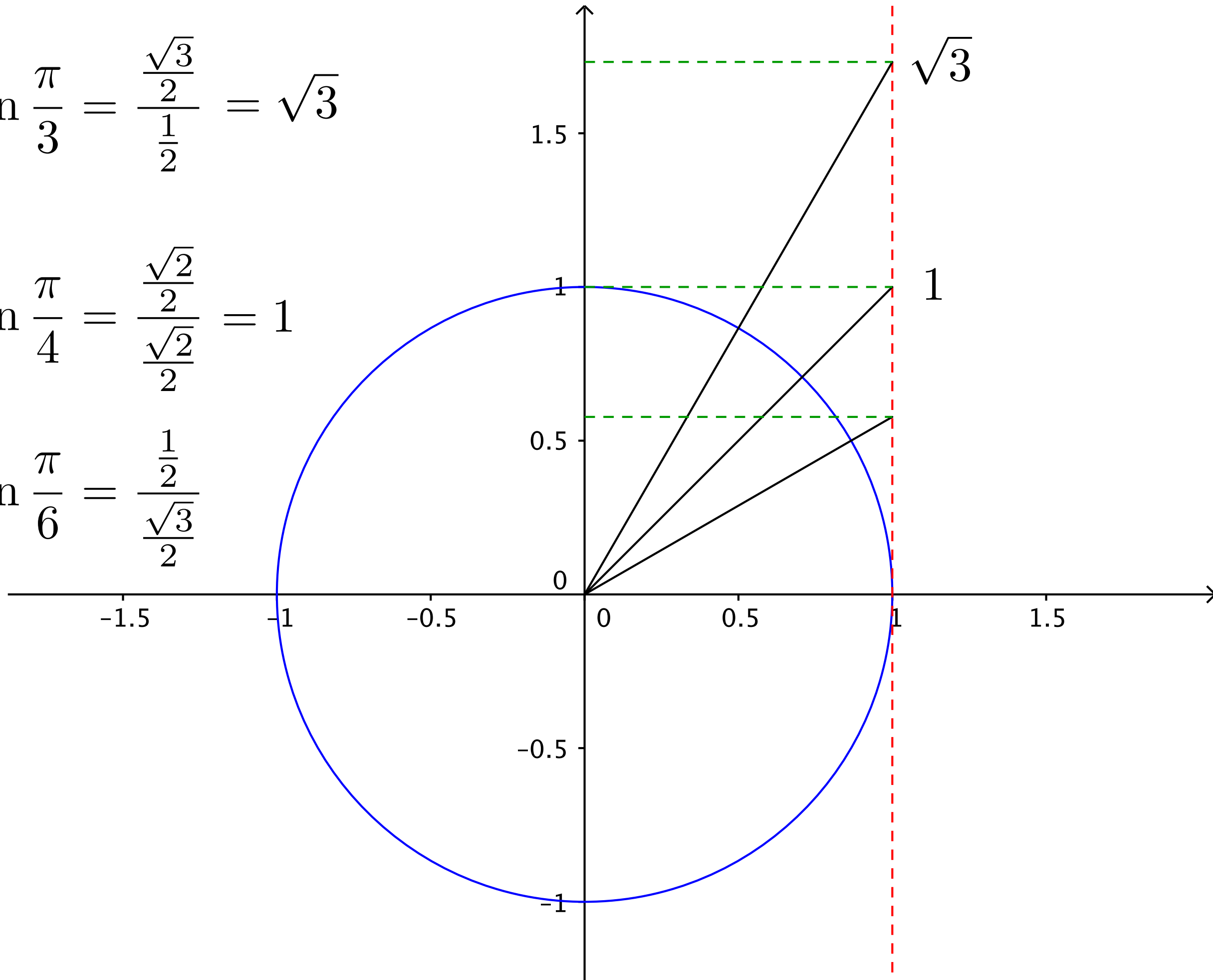
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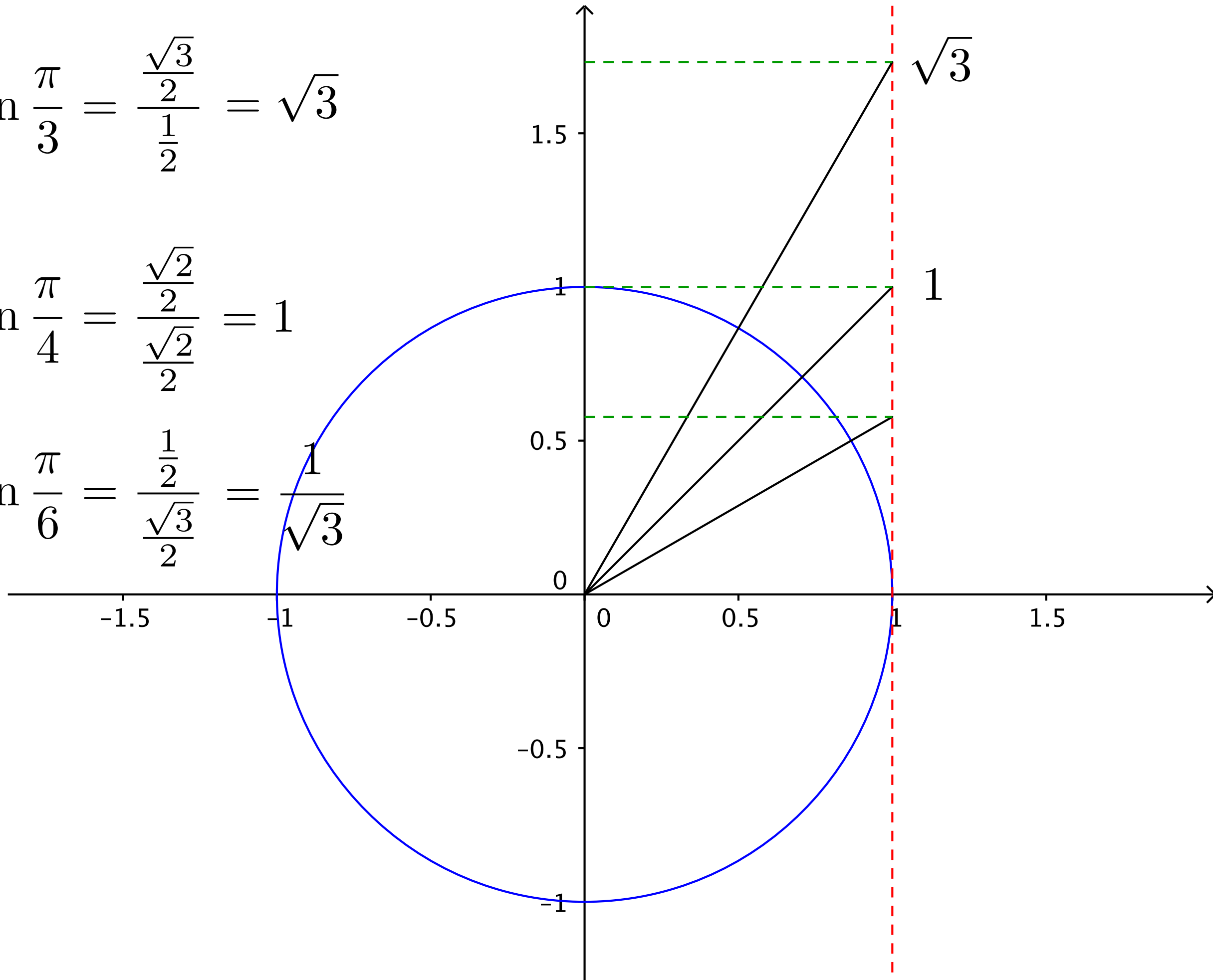
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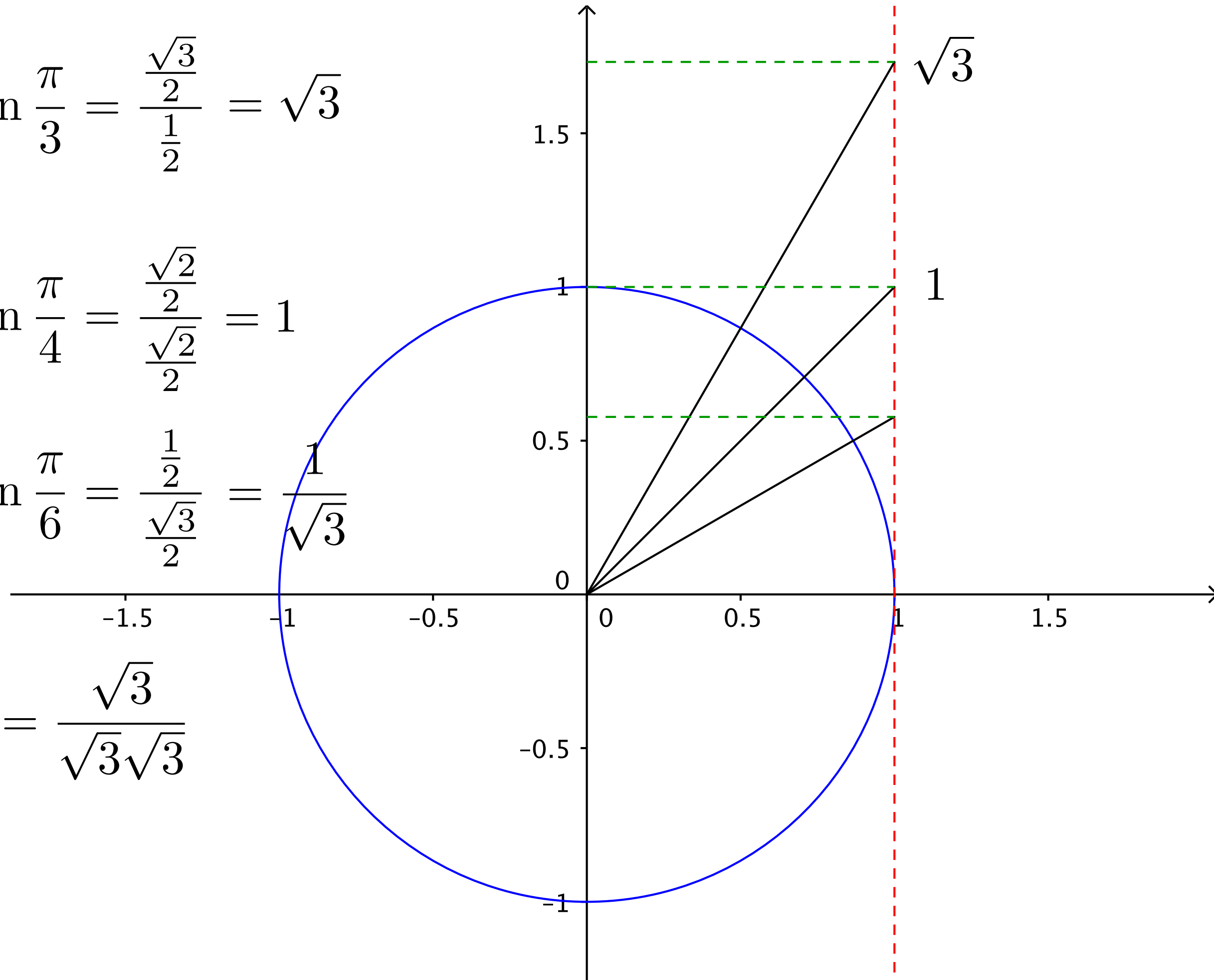


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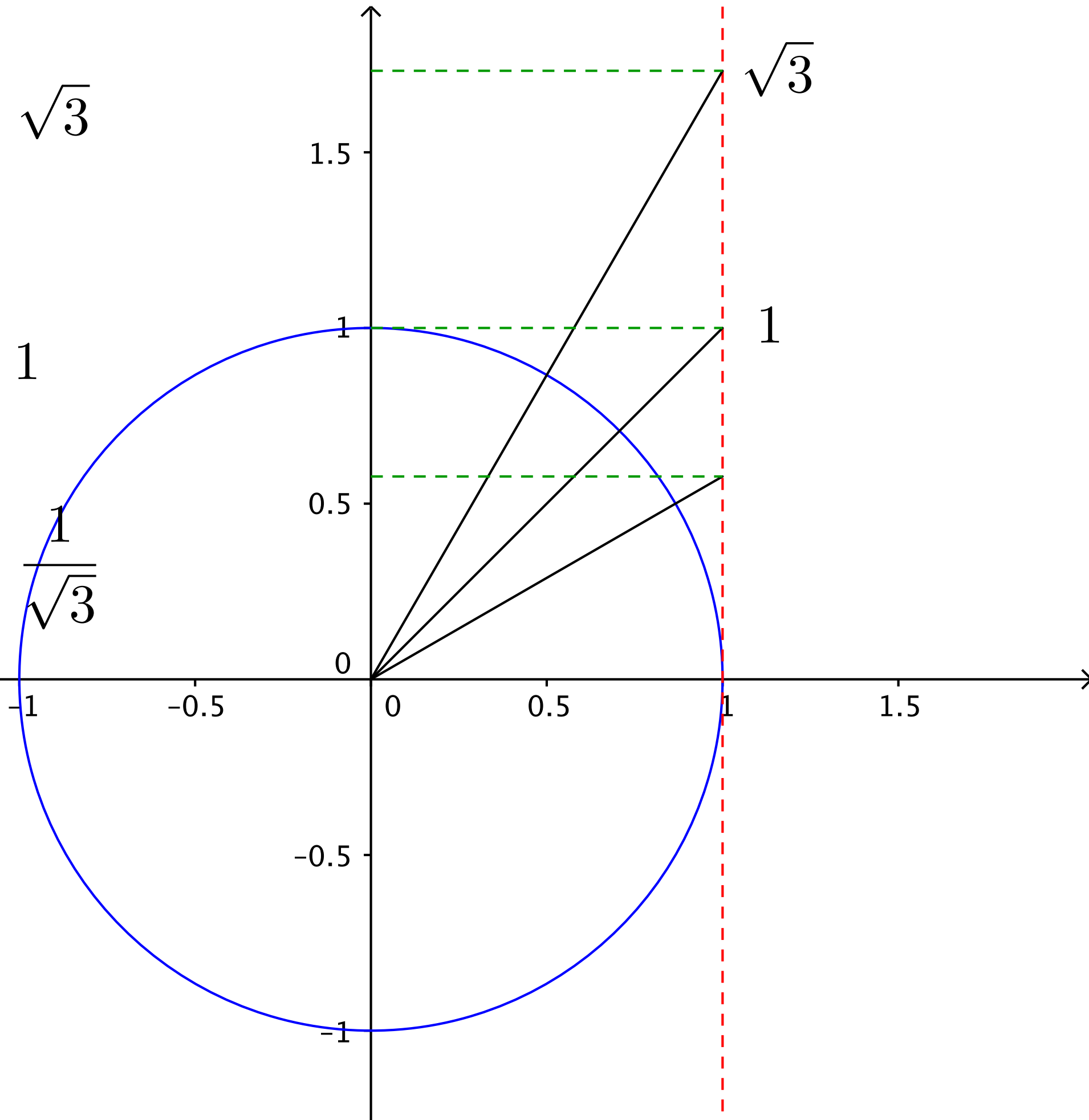
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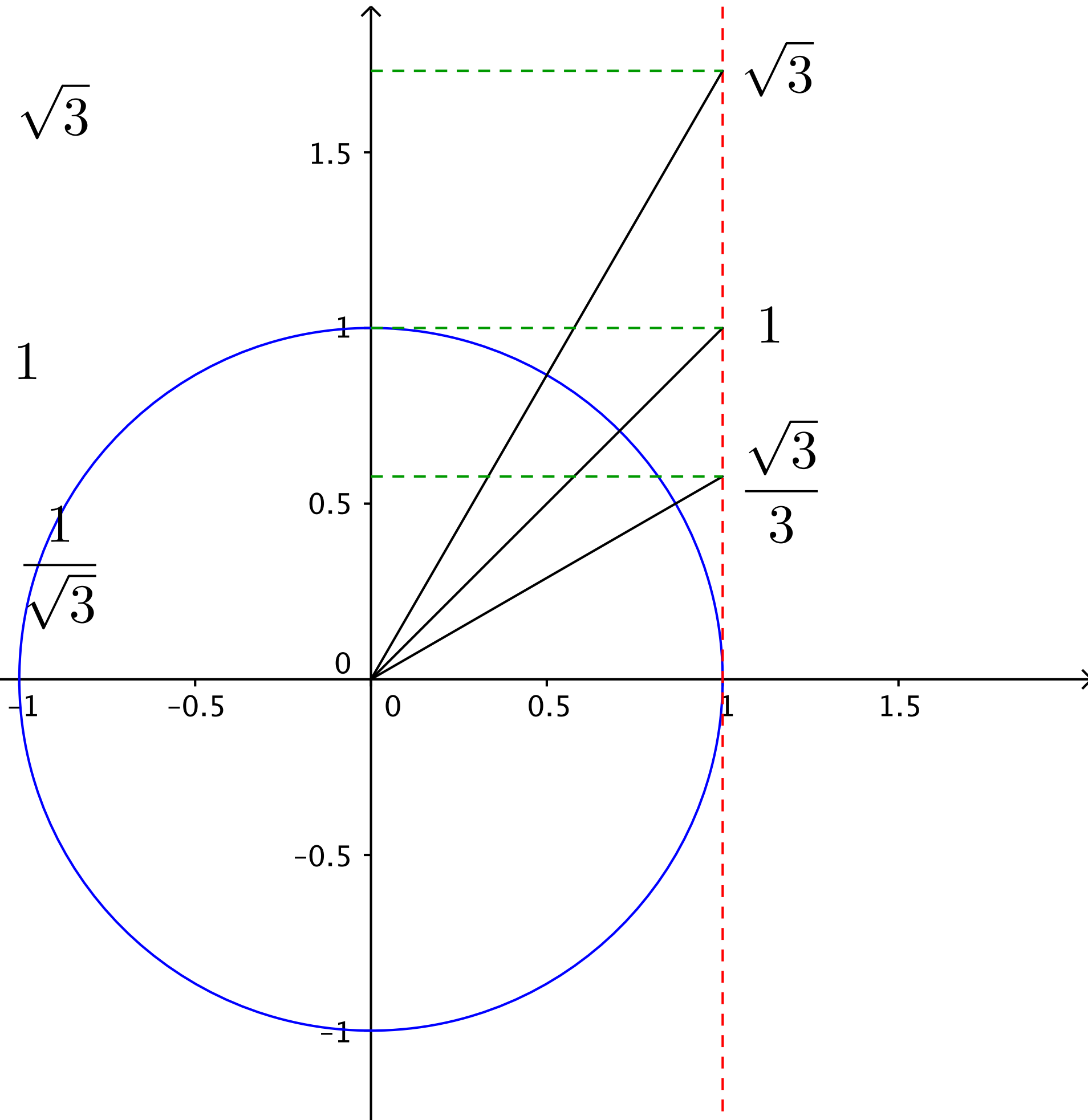
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Faites les exercices suivants

Évaluer

a) $\arccos -1$

e) $\arccos \left(-\frac{1}{2} \right)$

b) $\arcsin 0$

f) $\arctan 1$

c) $\arcsin \frac{\sqrt{2}}{2}$

g) $\operatorname{arcsec} \sqrt{2}$

d) $\arcsin \left(-\frac{\sqrt{3}}{2} \right)$

h) $\arccos \frac{\sqrt{3}}{2}$

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Donc dès qu'on a une solution, additionner un multiple de 2π ou en soustraire un nous donne aussi une solution.

Example

$$2 \sin \theta + 1 = 0$$

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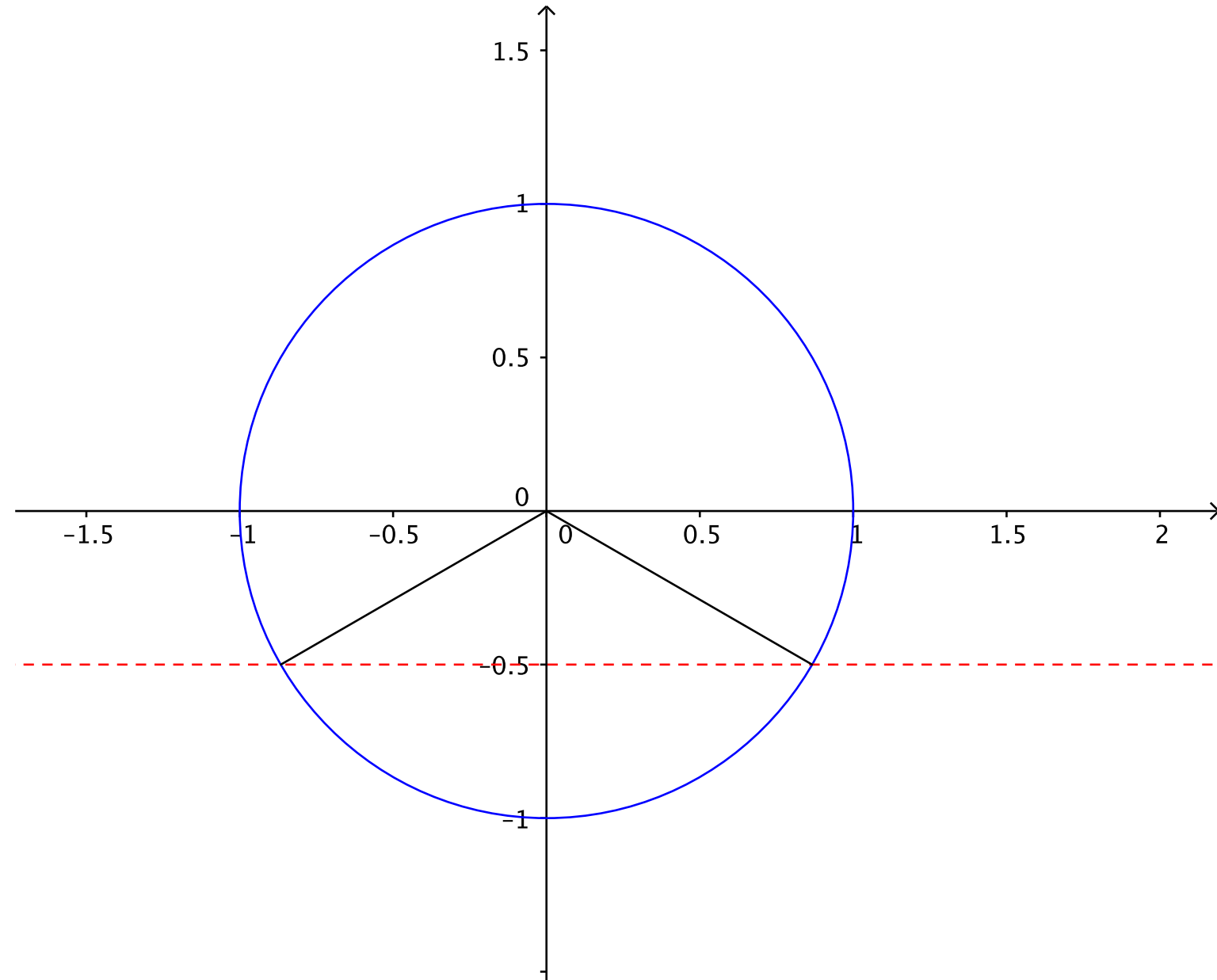
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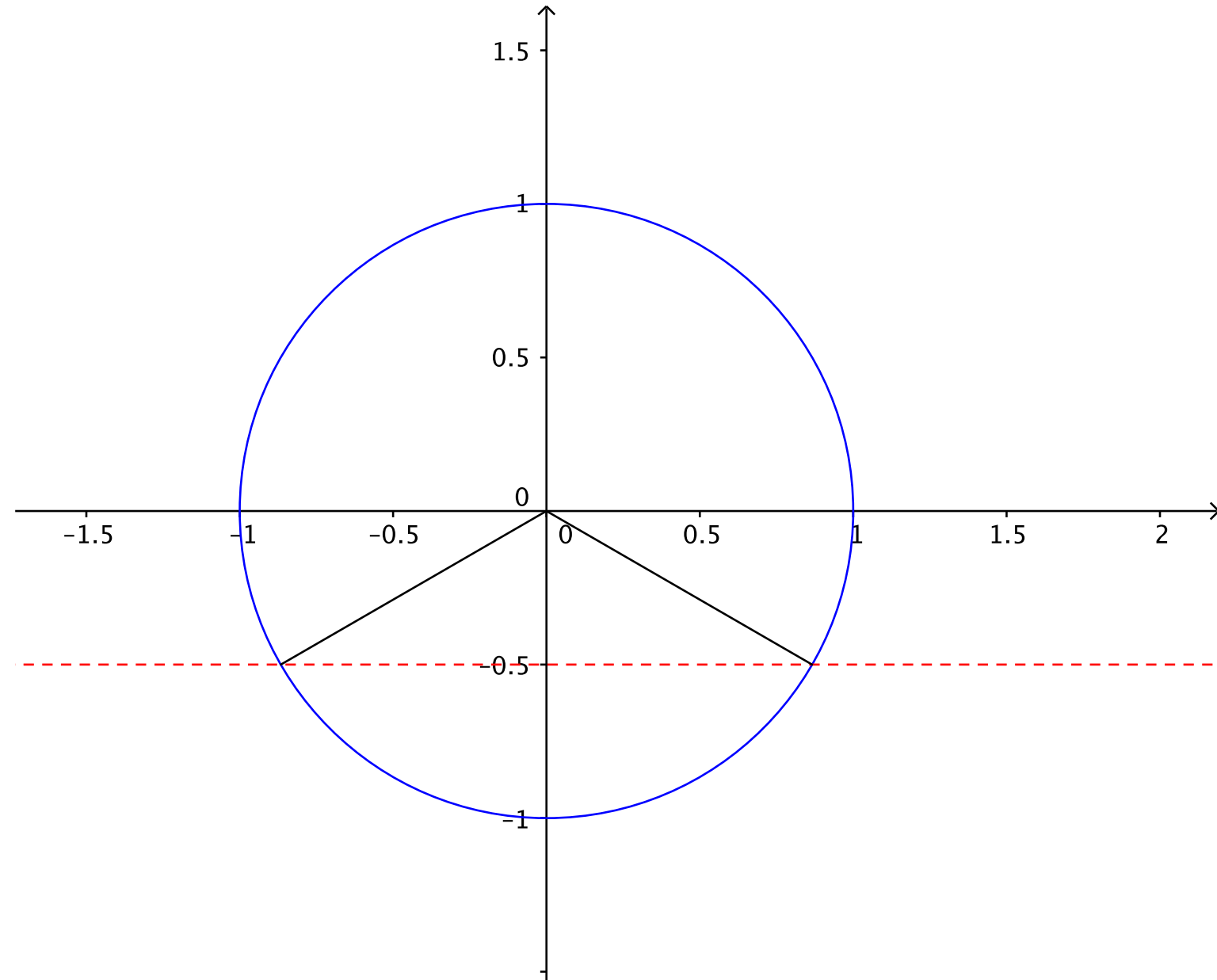


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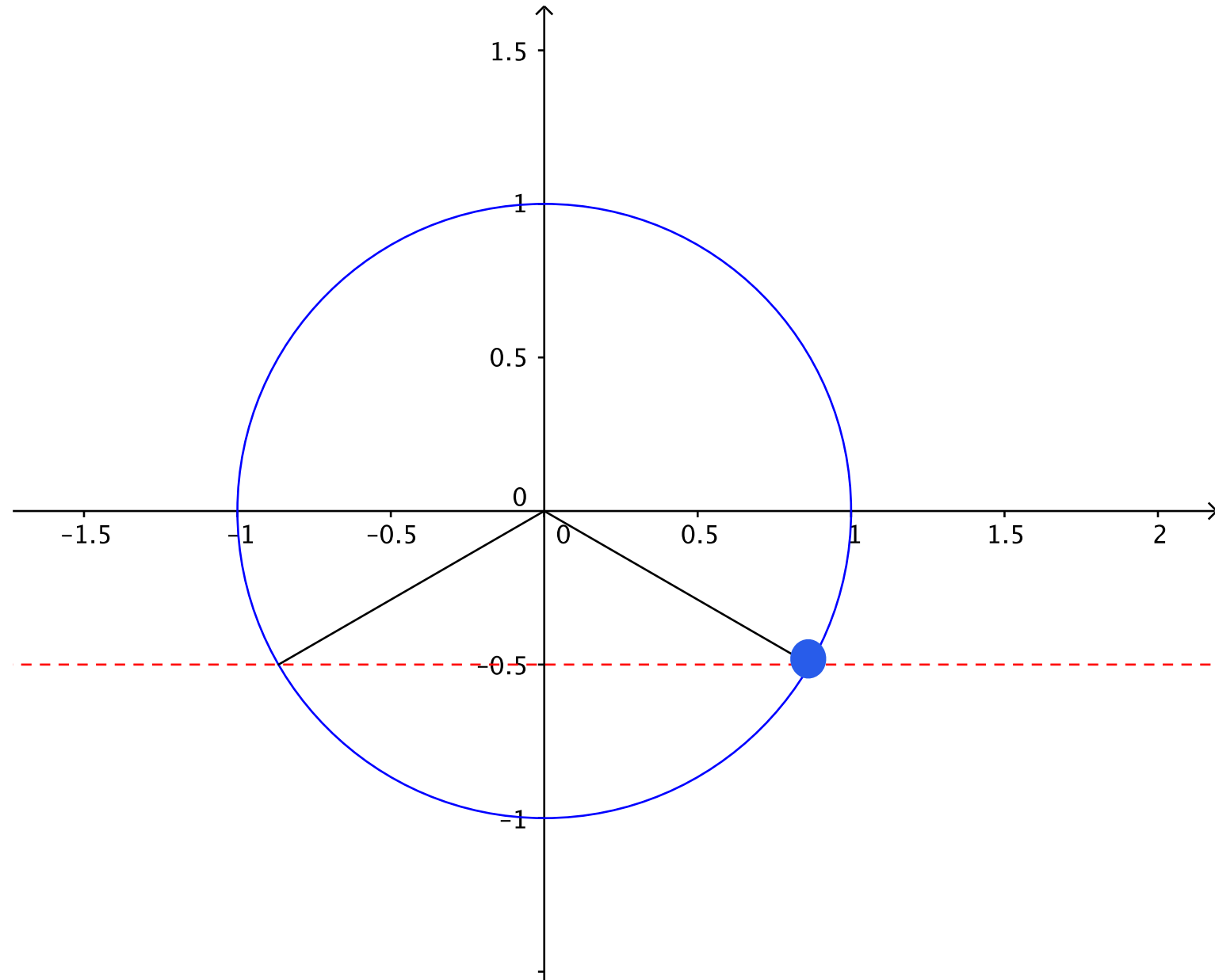
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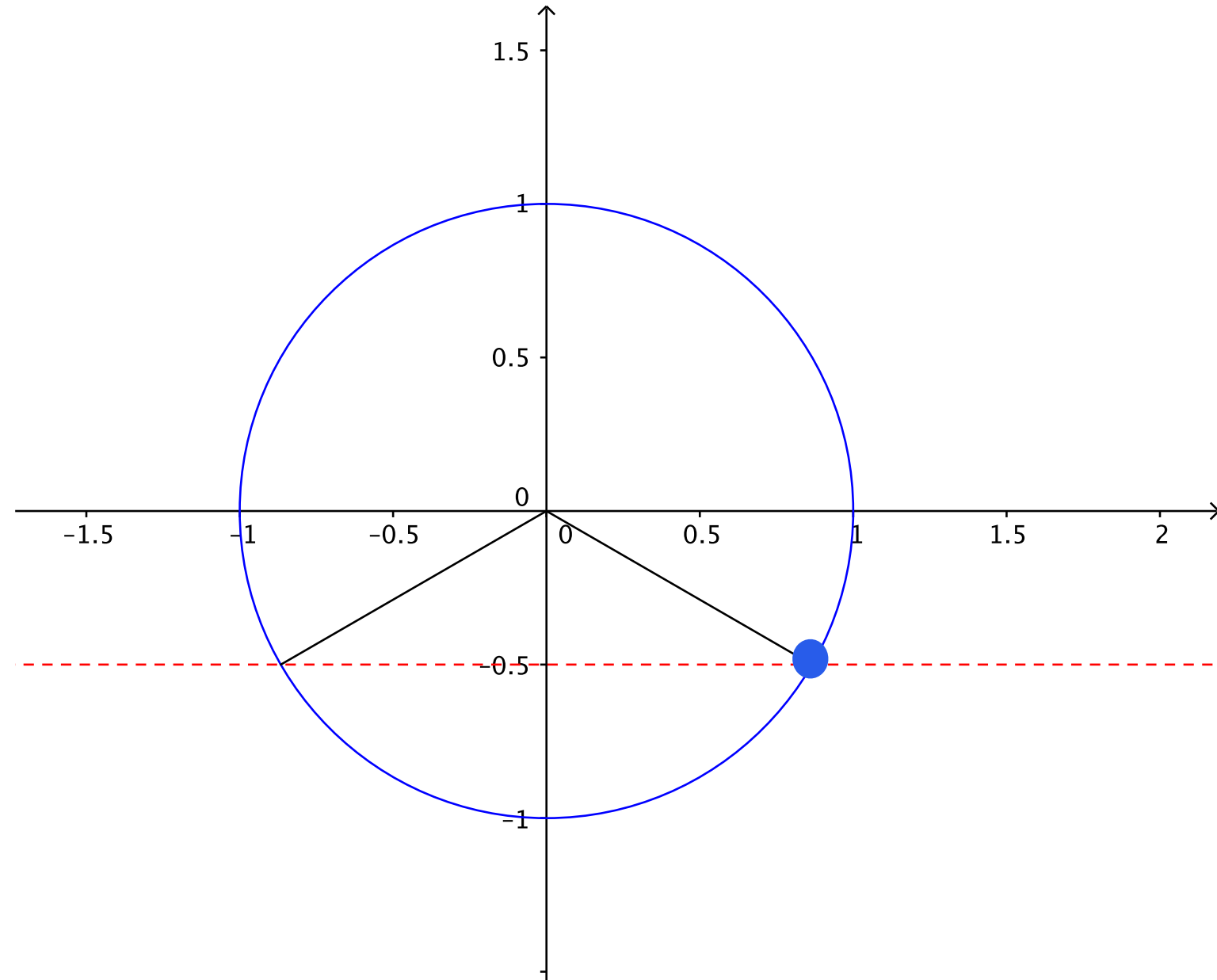
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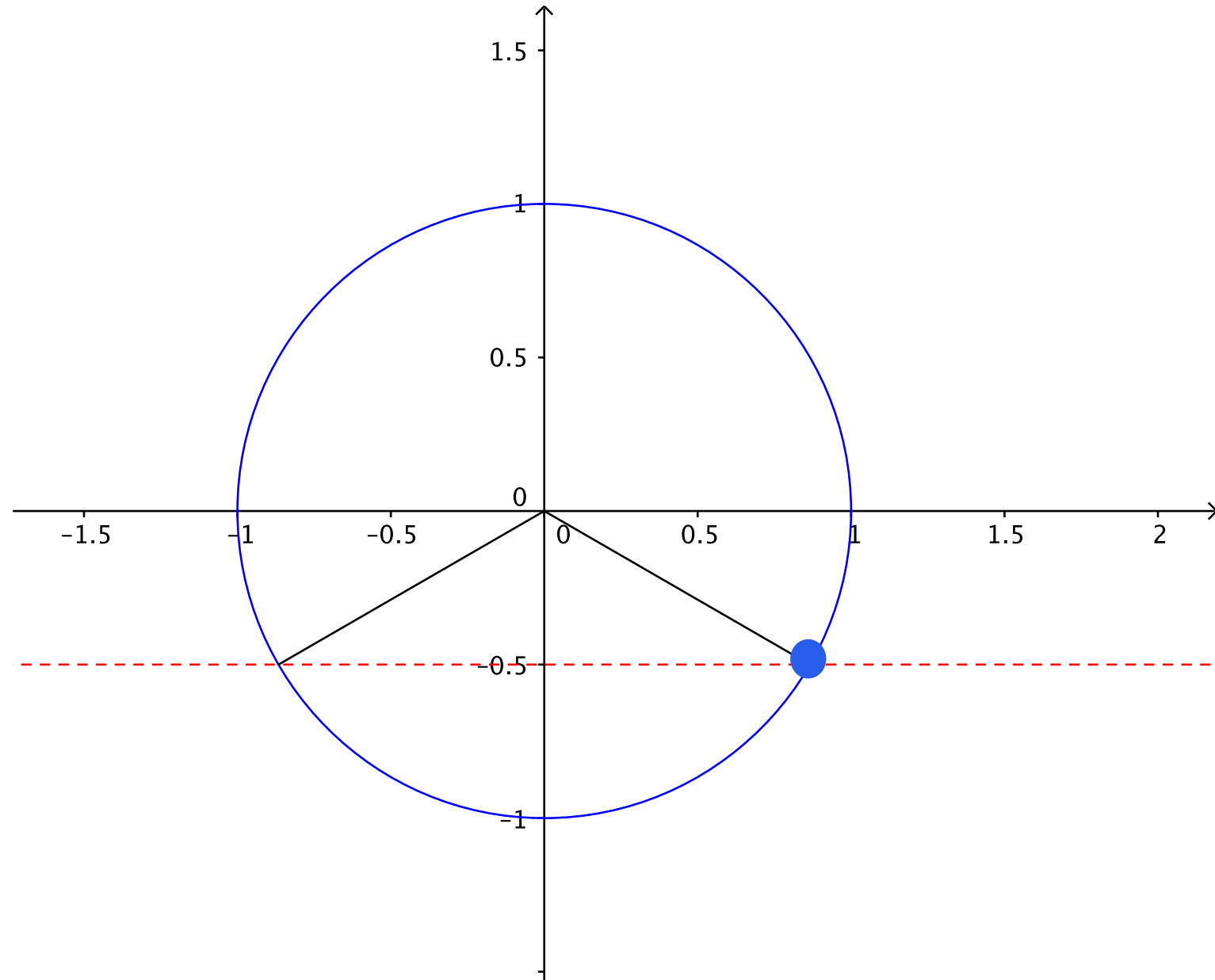
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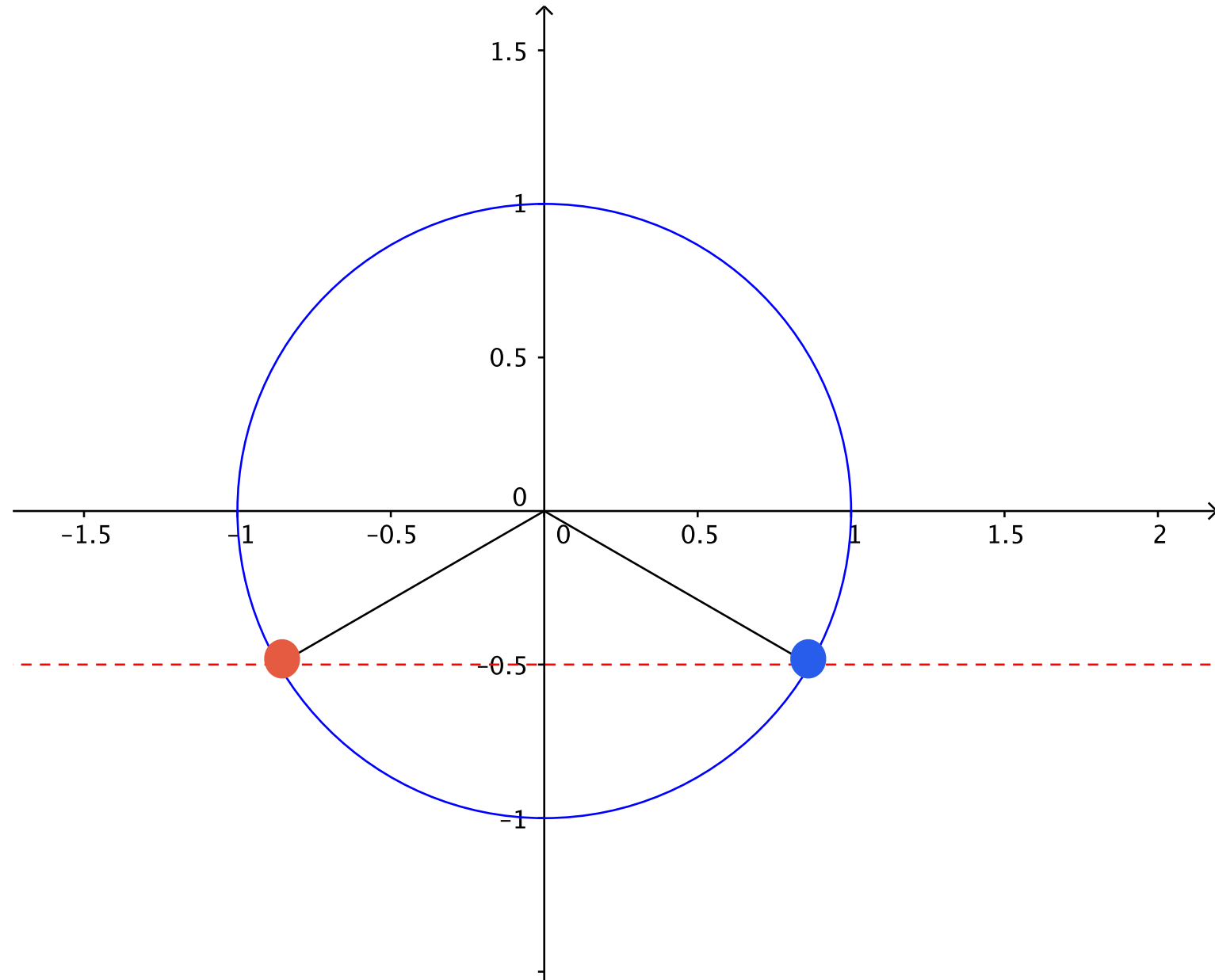
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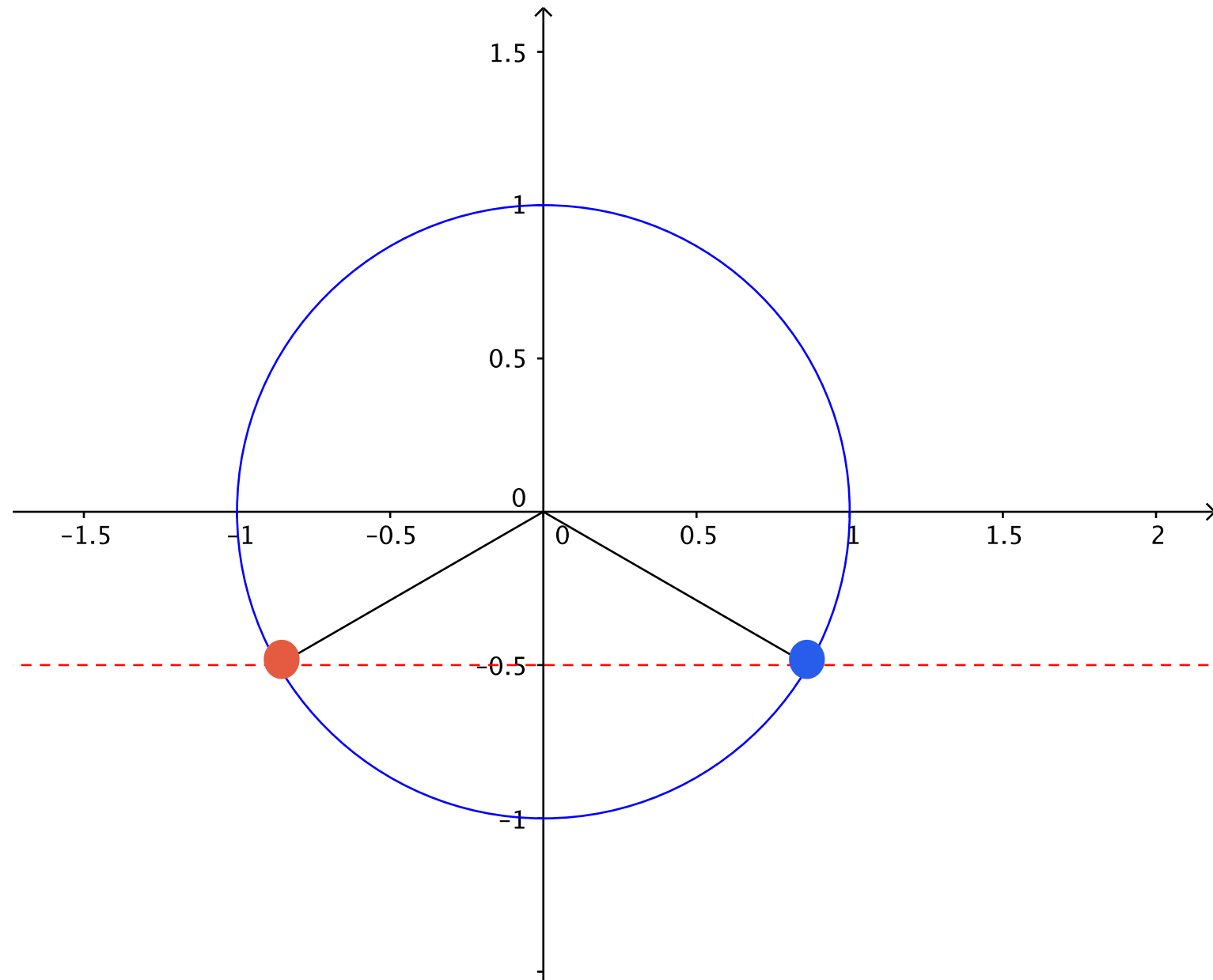
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$$\theta = -\frac{\pi}{6} + k2\pi, k \in \mathbb{Z} \quad \text{et}$$

$$\theta = \frac{7\pi}{6} + k2\pi, k \in \mathbb{Z}$$

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posons $x = \cos \theta$

$$2x^2 + x - 1 = 0$$

$$x = \frac{-1 \pm \sqrt{1 + 8}}{4}$$

Example

$$2 \cos^2 \theta + \cos \theta - 1 = 0 \quad \text{posons} \quad x = \cos \theta$$

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Example

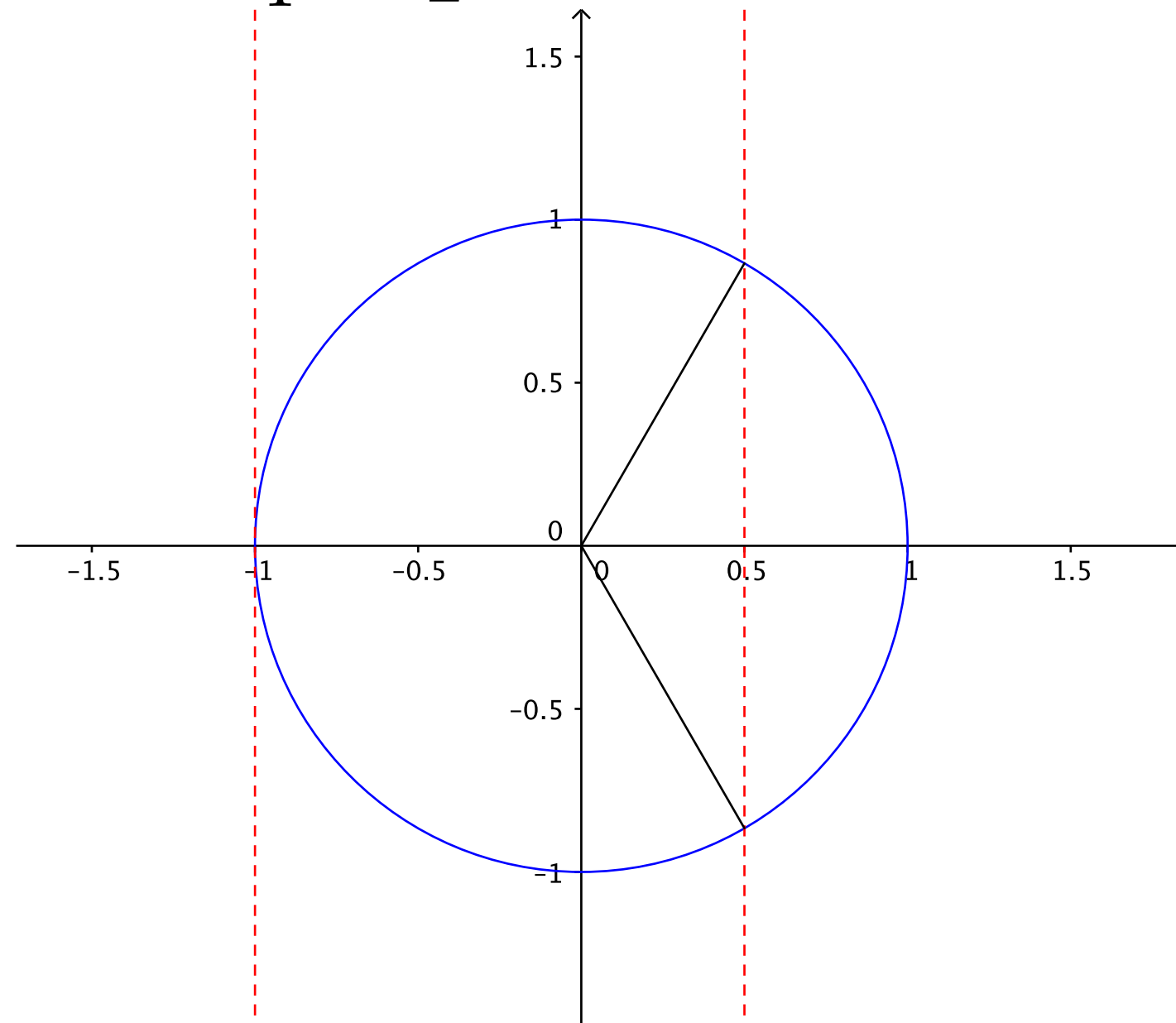
$$2 \cos^2 \theta + \cos \theta - 1 = 0 \quad \text{posons} \quad x = \cos \theta$$

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Example

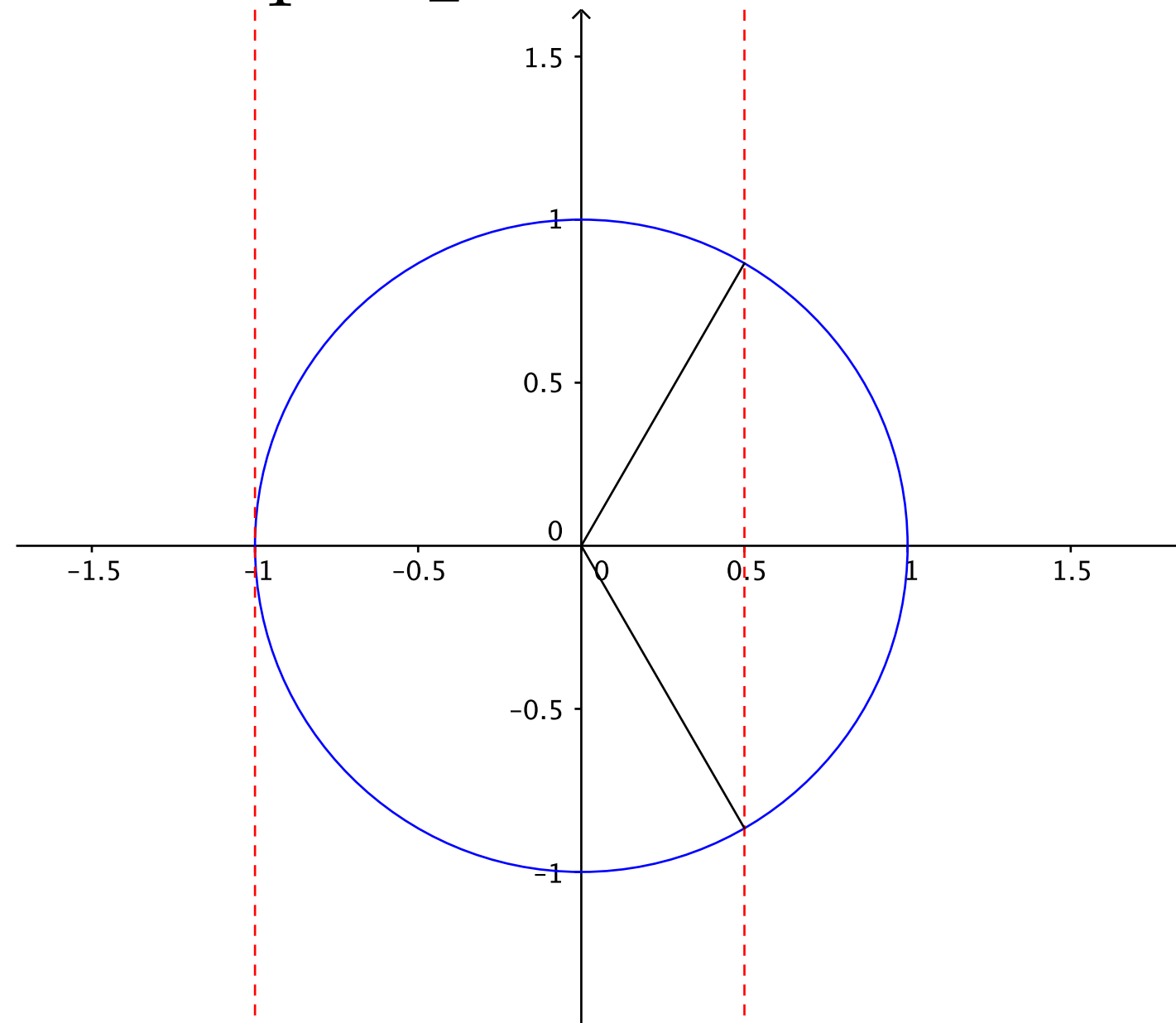
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$$x = -1 = \cos \theta$$

$$x = \frac{2}{4} = \frac{1}{2} = \cos \theta$$

$$\theta = \pi$$



Example

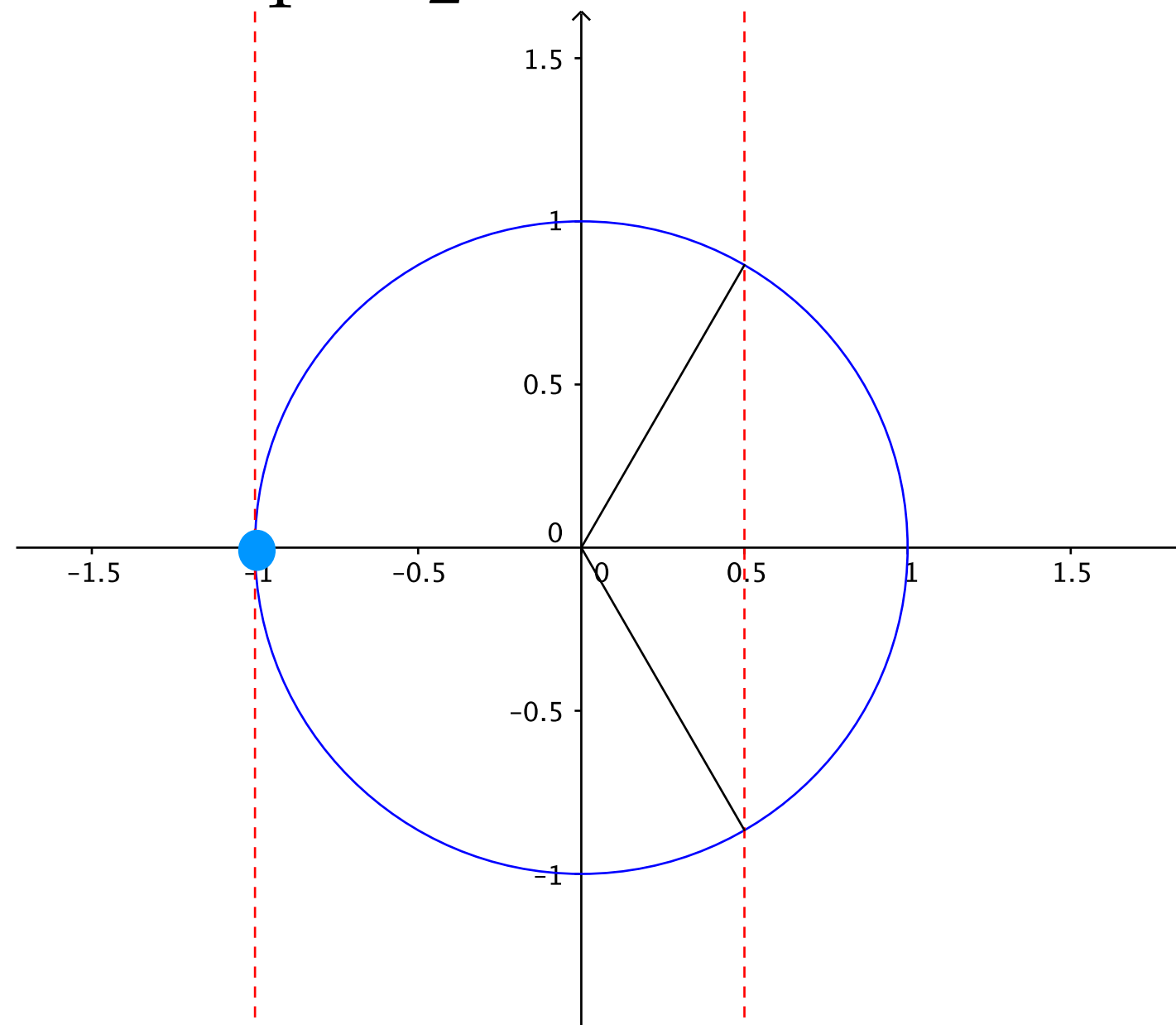
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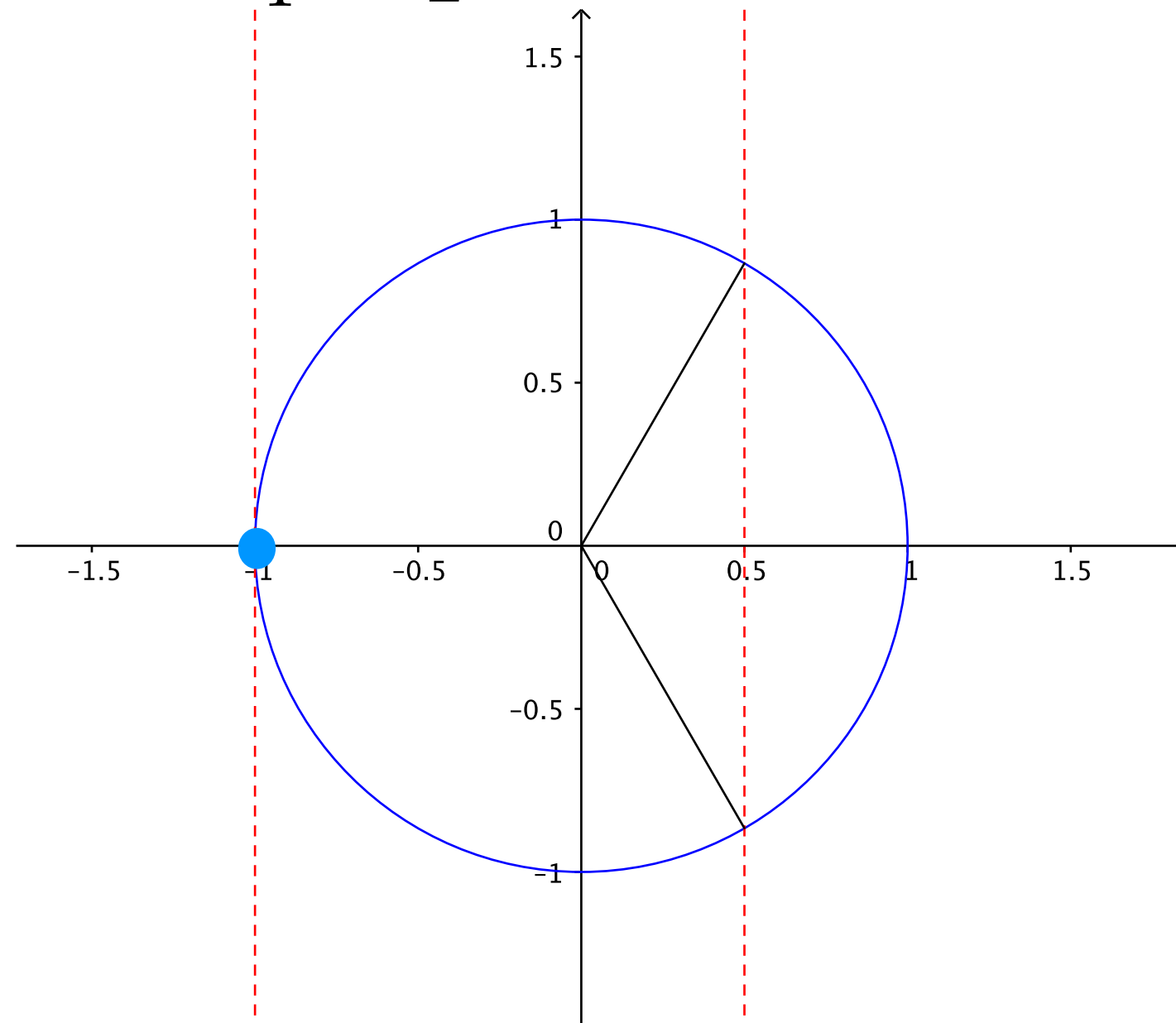
$$2x^2 + x - 1 = 0$$

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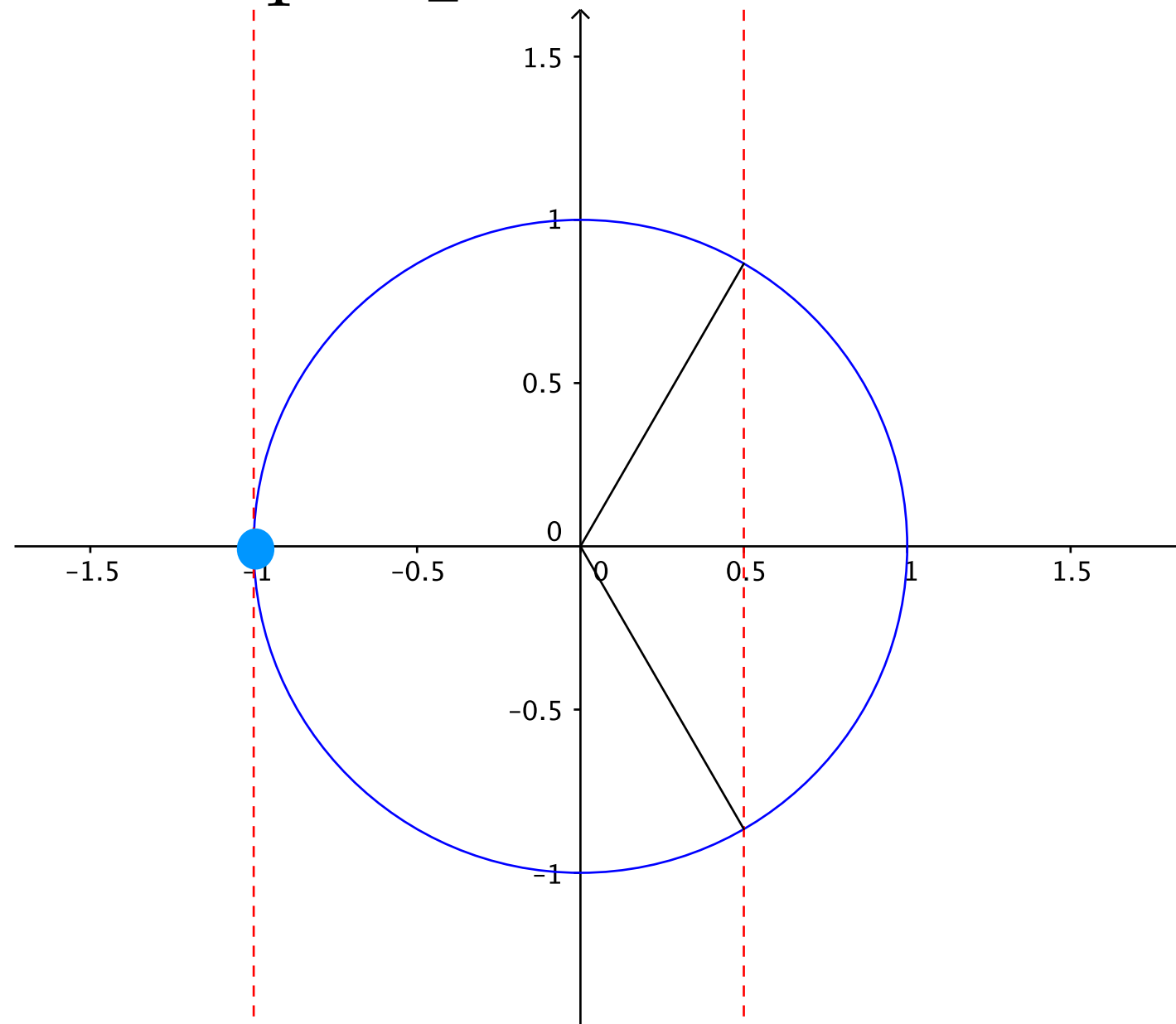
$$x = \frac{-1 \pm \sqrt{1 + 8}}{4} = \frac{-1 \pm 3}{4}$$

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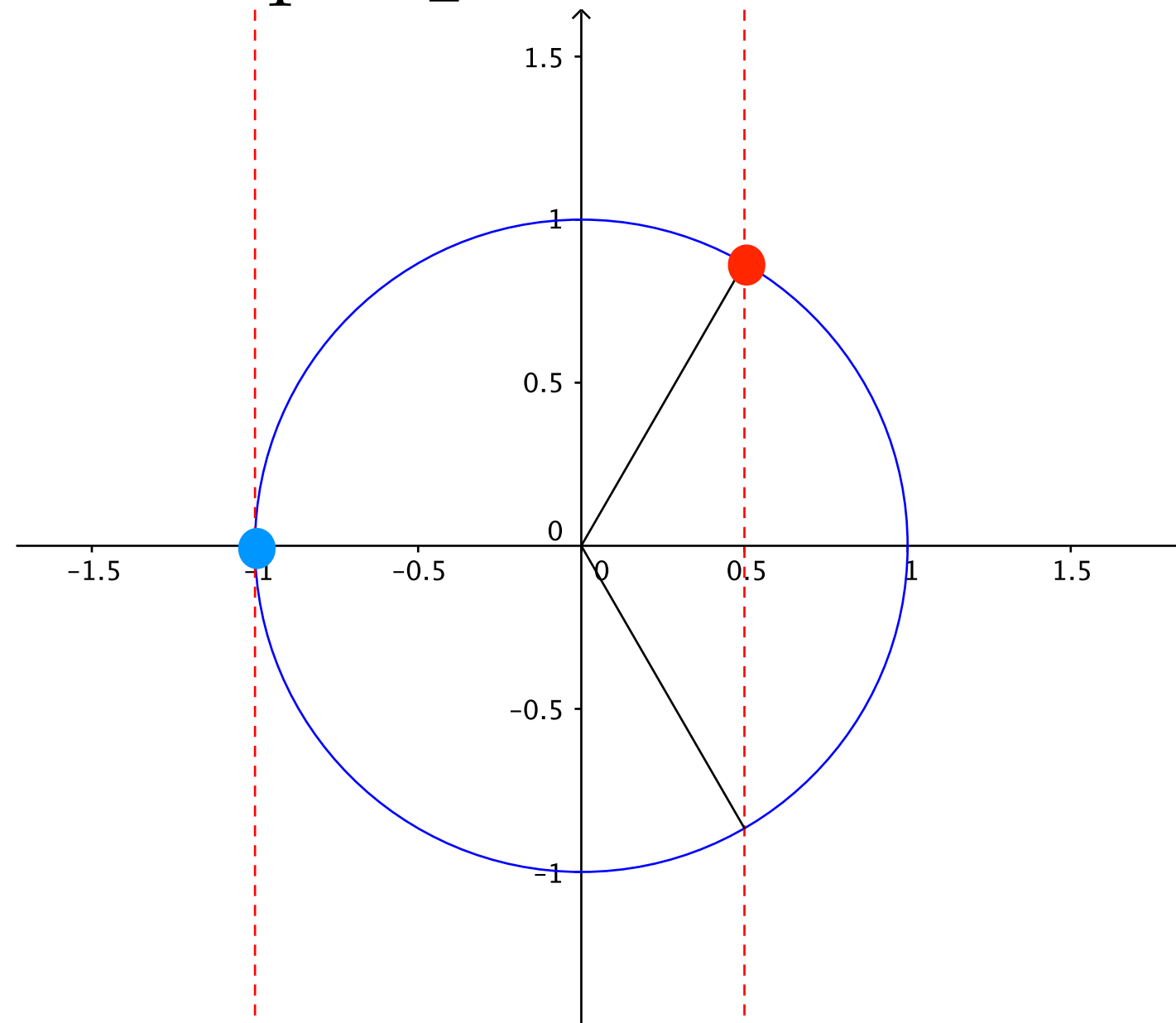
$$x = \frac{-1 \pm \sqrt{1 + 8}}{4} = \frac{-1 \pm 3}{4}$$

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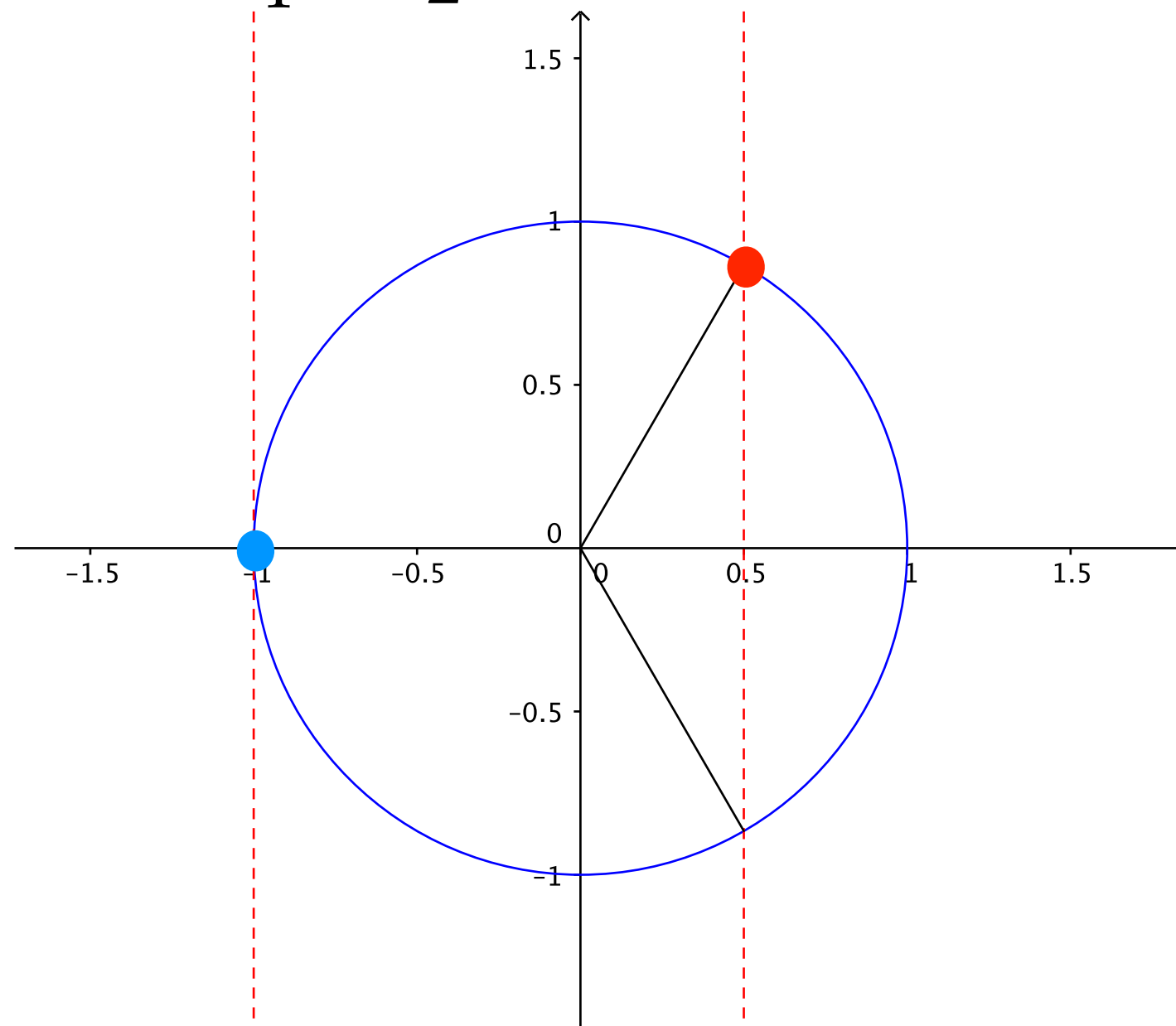
$$x = \frac{-1 \pm \sqrt{1 + 8}}{4} = \frac{-1 \pm 3}{4}$$

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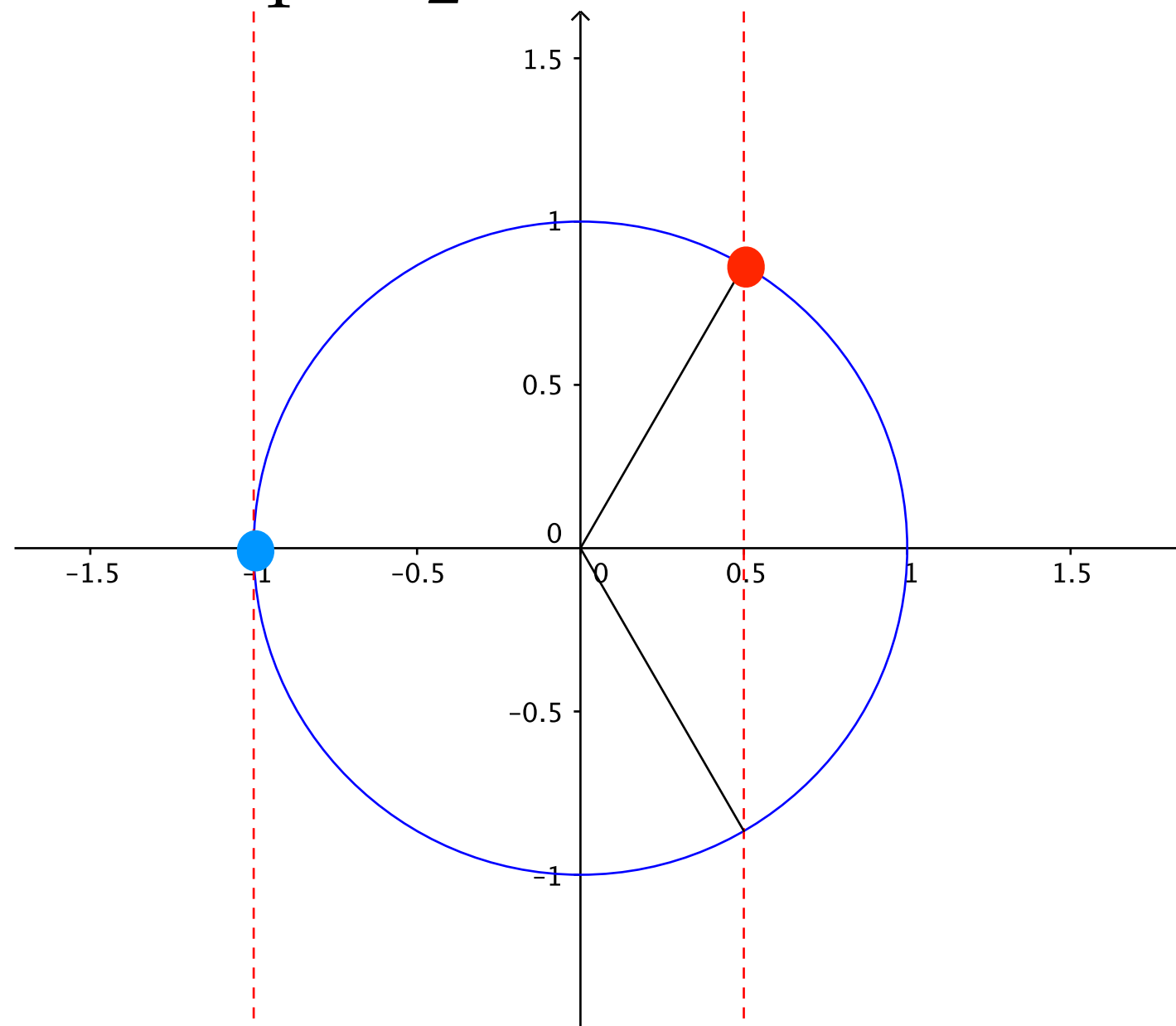
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$$\theta = \pi$$

$$\theta = \frac{\pi}{3}$$

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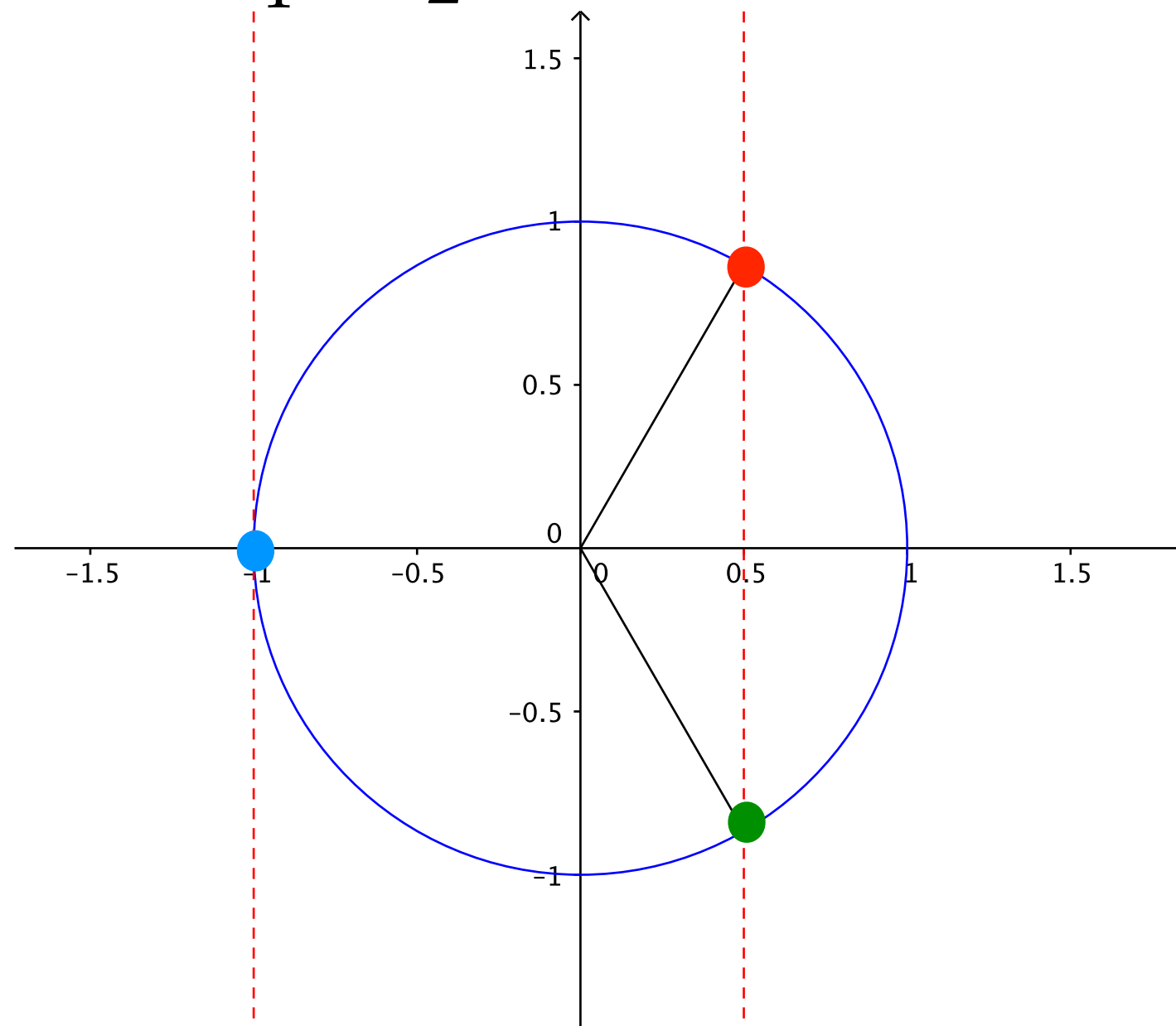
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$$\theta = \pi$$

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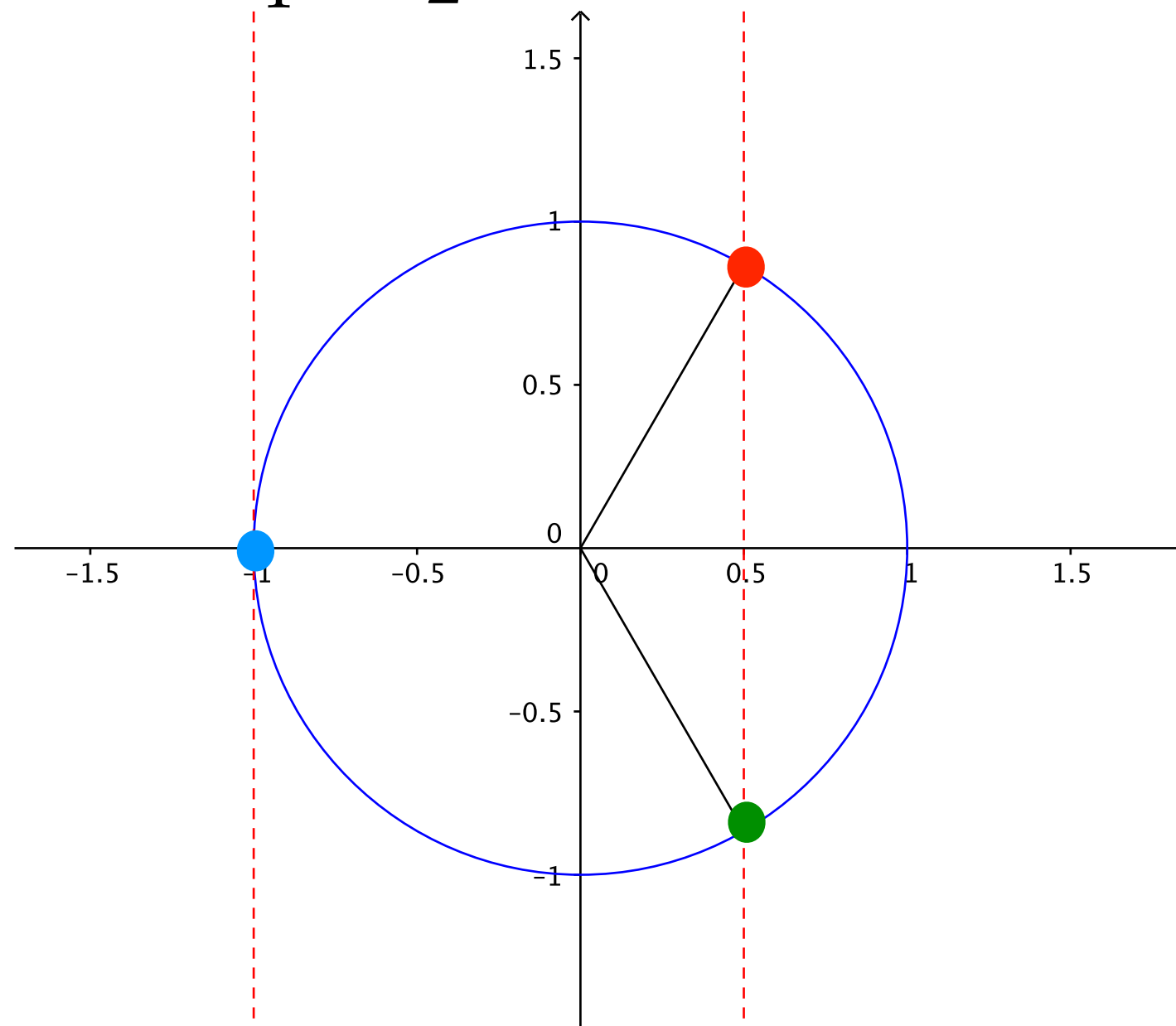
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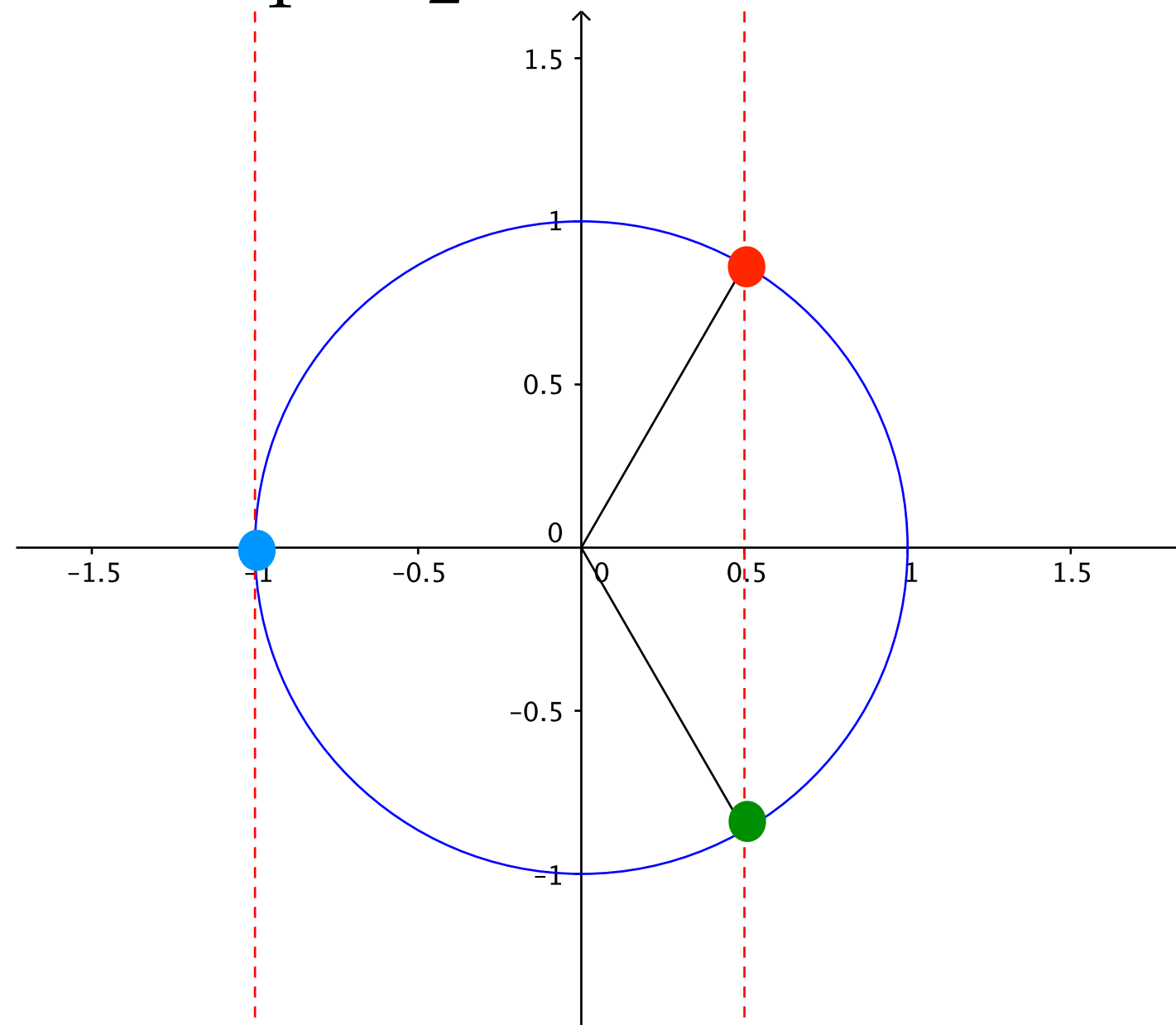
$$x = -1 = \cos \theta$$

$$x = \frac{2}{4} = \frac{1}{2} = \cos \theta$$

$$\theta = \pi + k2\pi, k \in \mathbb{Z}$$

$$\theta = \frac{\pi}{3} + k2\pi, k \in \mathbb{Z}$$

$$\theta = -\frac{\pi}{3} + k2\pi, k \in \mathbb{Z}$$



Example

$$\sec \theta + 4 \csc \theta = 5 \csc \theta$$

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$$\iff \sec \theta = \csc \theta \quad \iff \frac{1}{\cos \theta} = \frac{1}{\sin \theta}$$

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$$\iff \sec \theta = \csc \theta \iff \frac{1}{\cos \theta} = \frac{1}{\sin \theta}$$

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$$\iff \sin \theta = \cos \theta \iff \frac{\sin \theta}{\cos \theta} = 1$$

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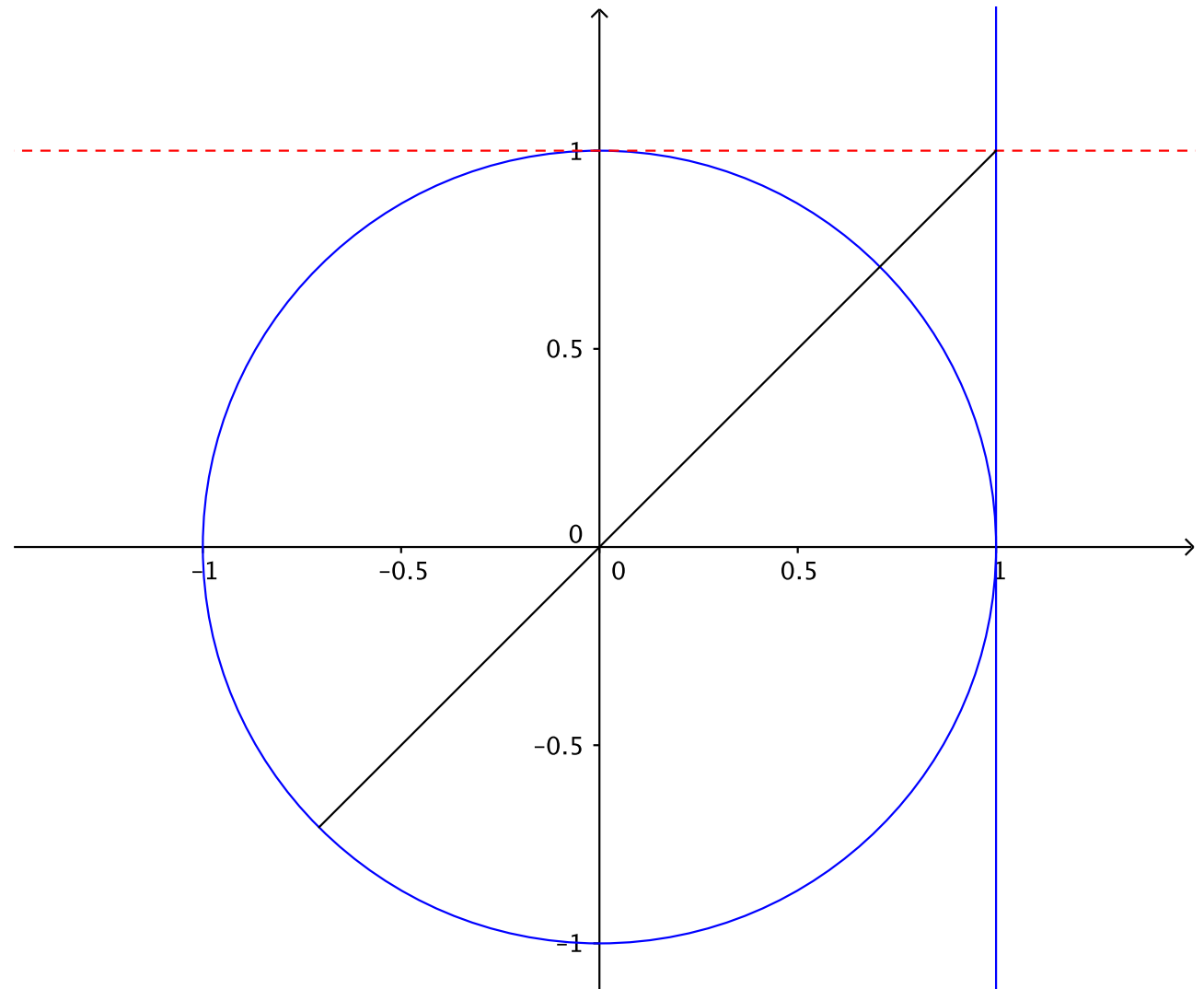
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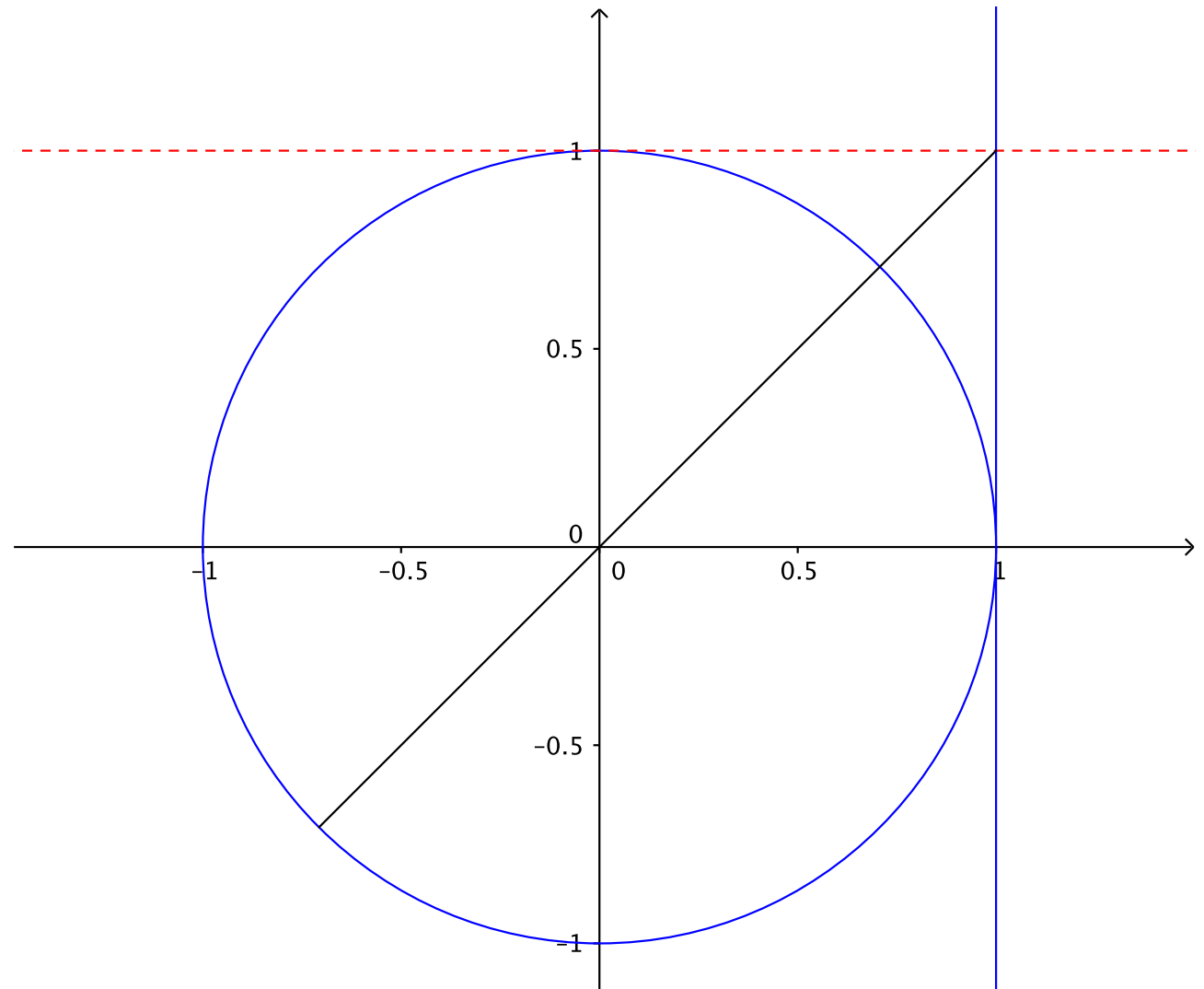
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$$\theta = \frac{\pi}{4}$$



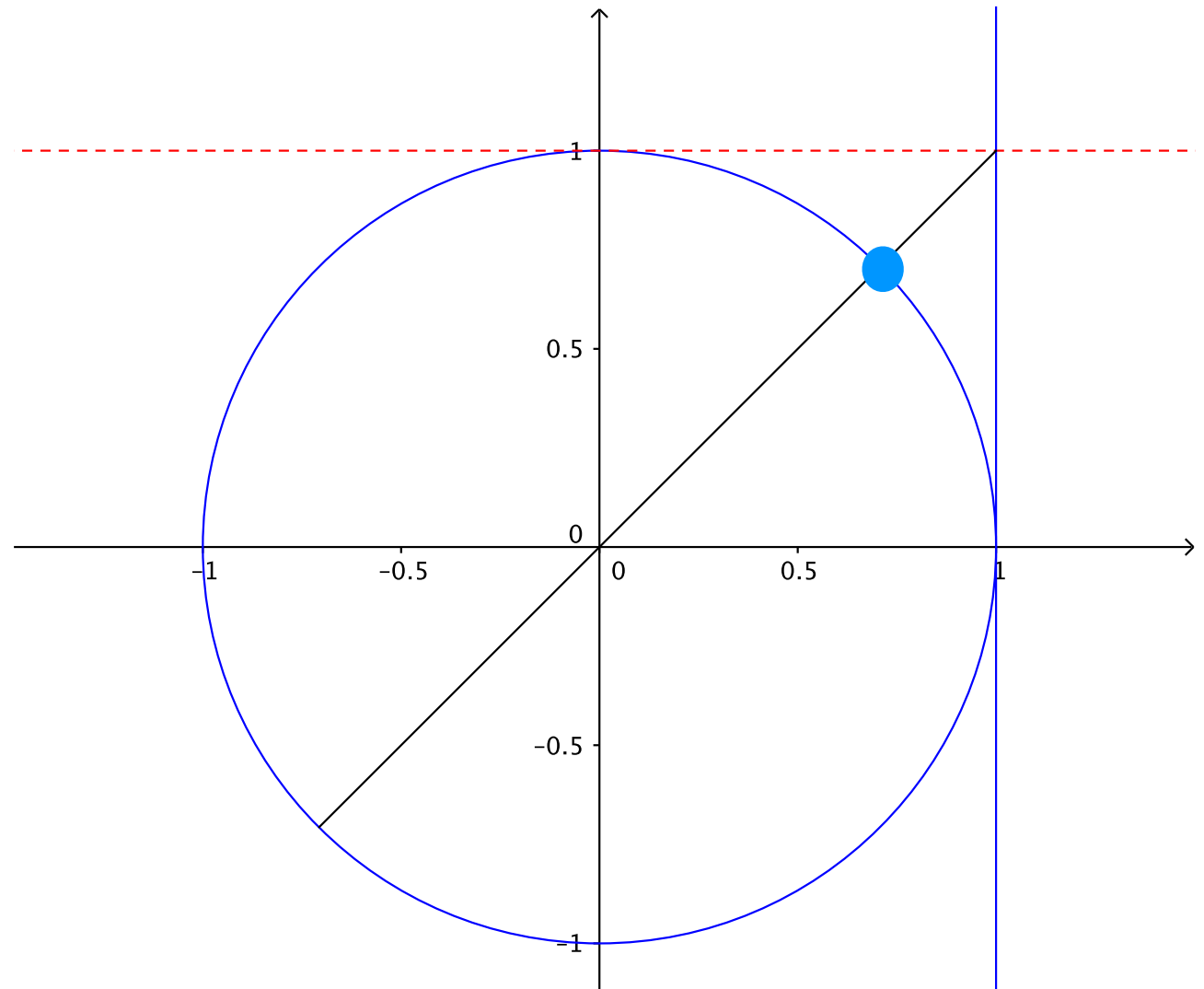
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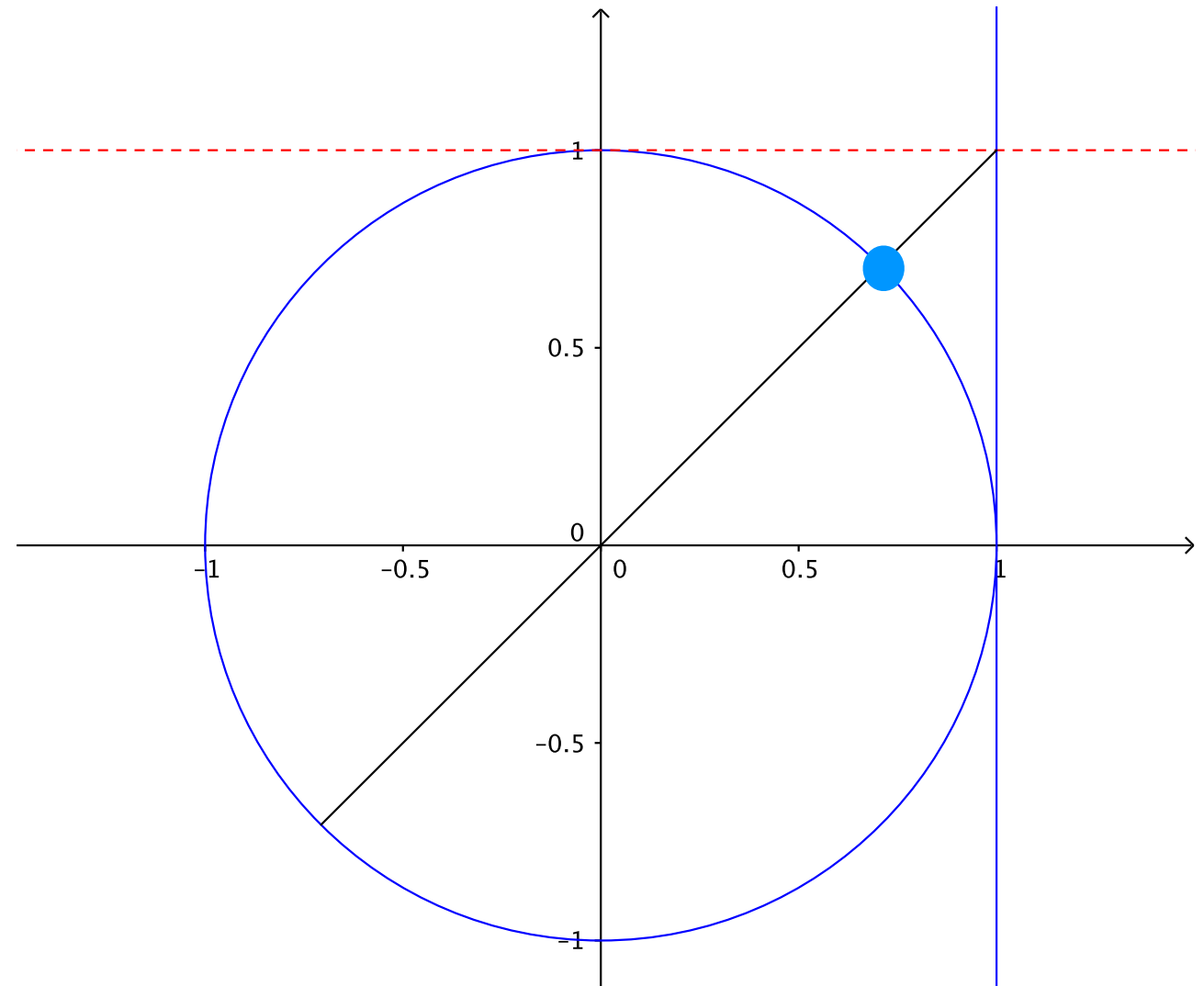
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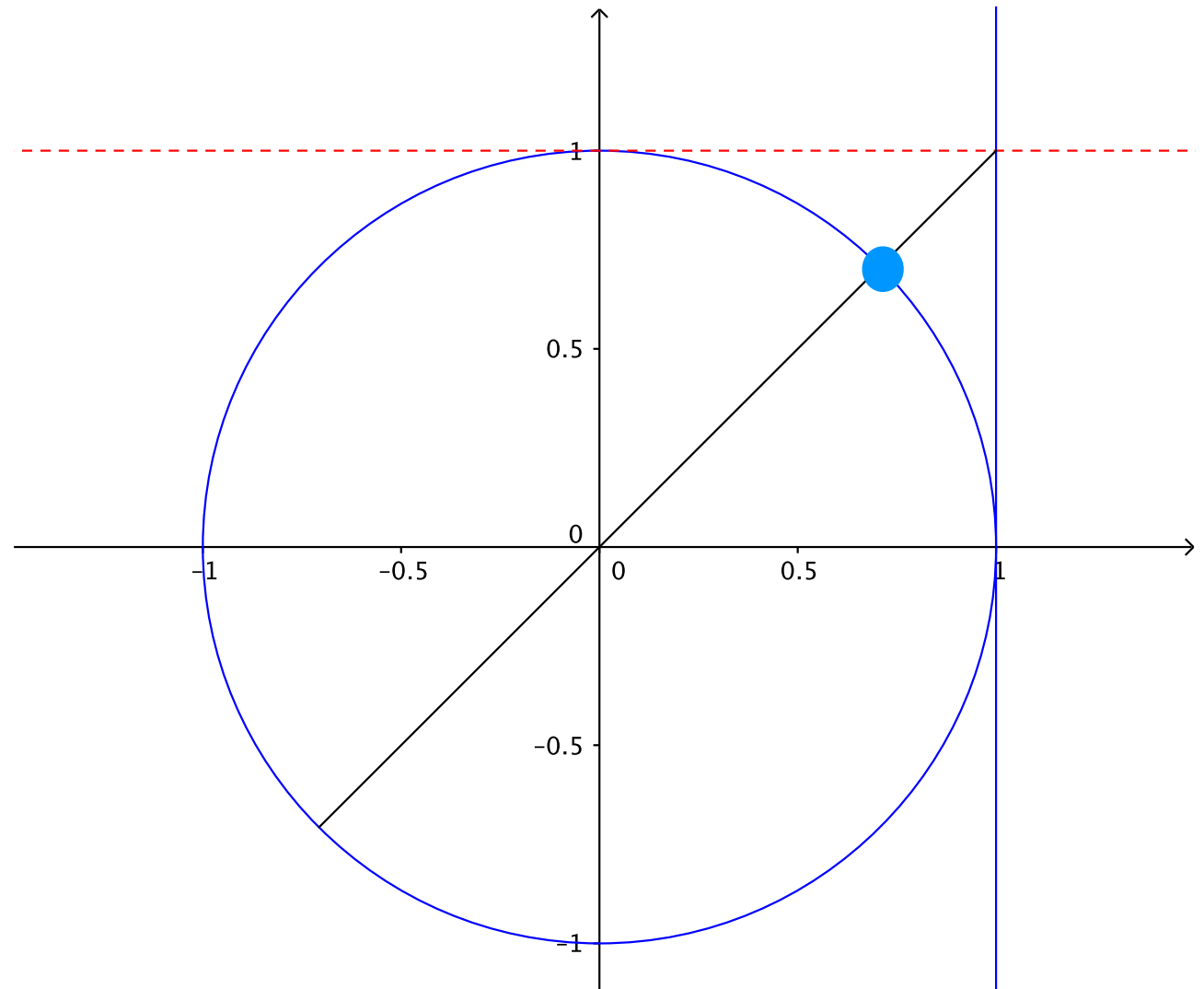
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$$\theta = \frac{5\pi}{4}$$



Example

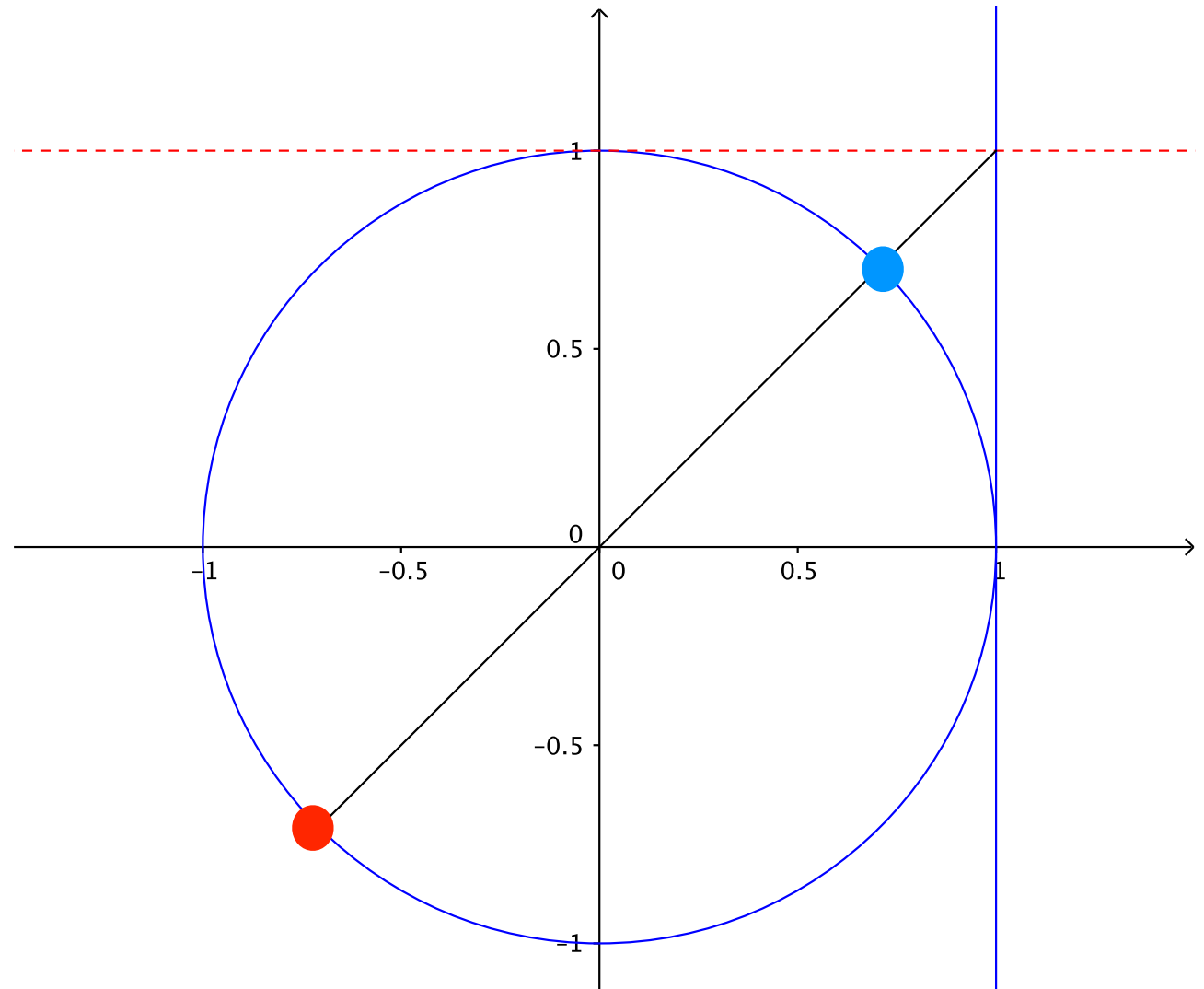
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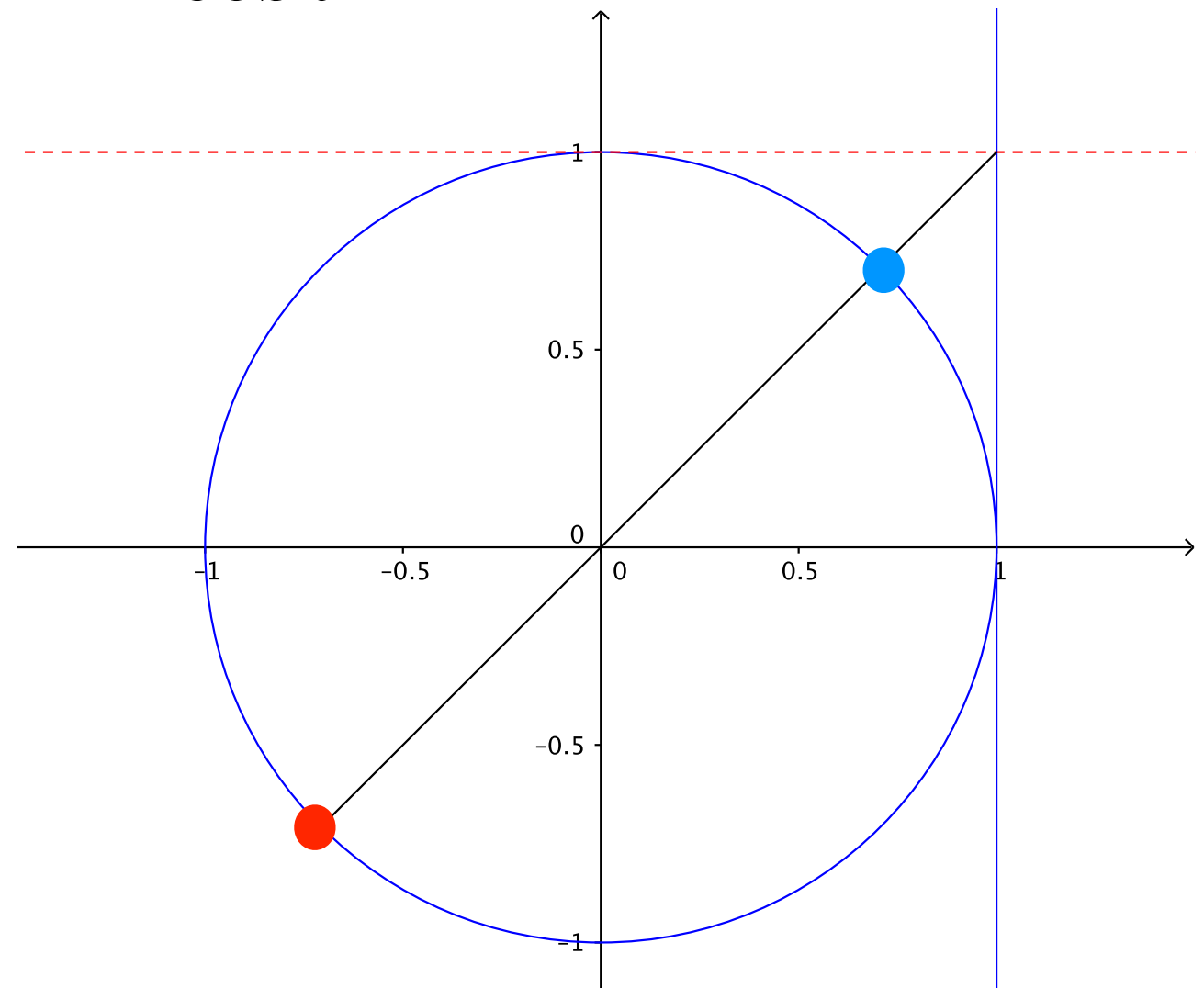
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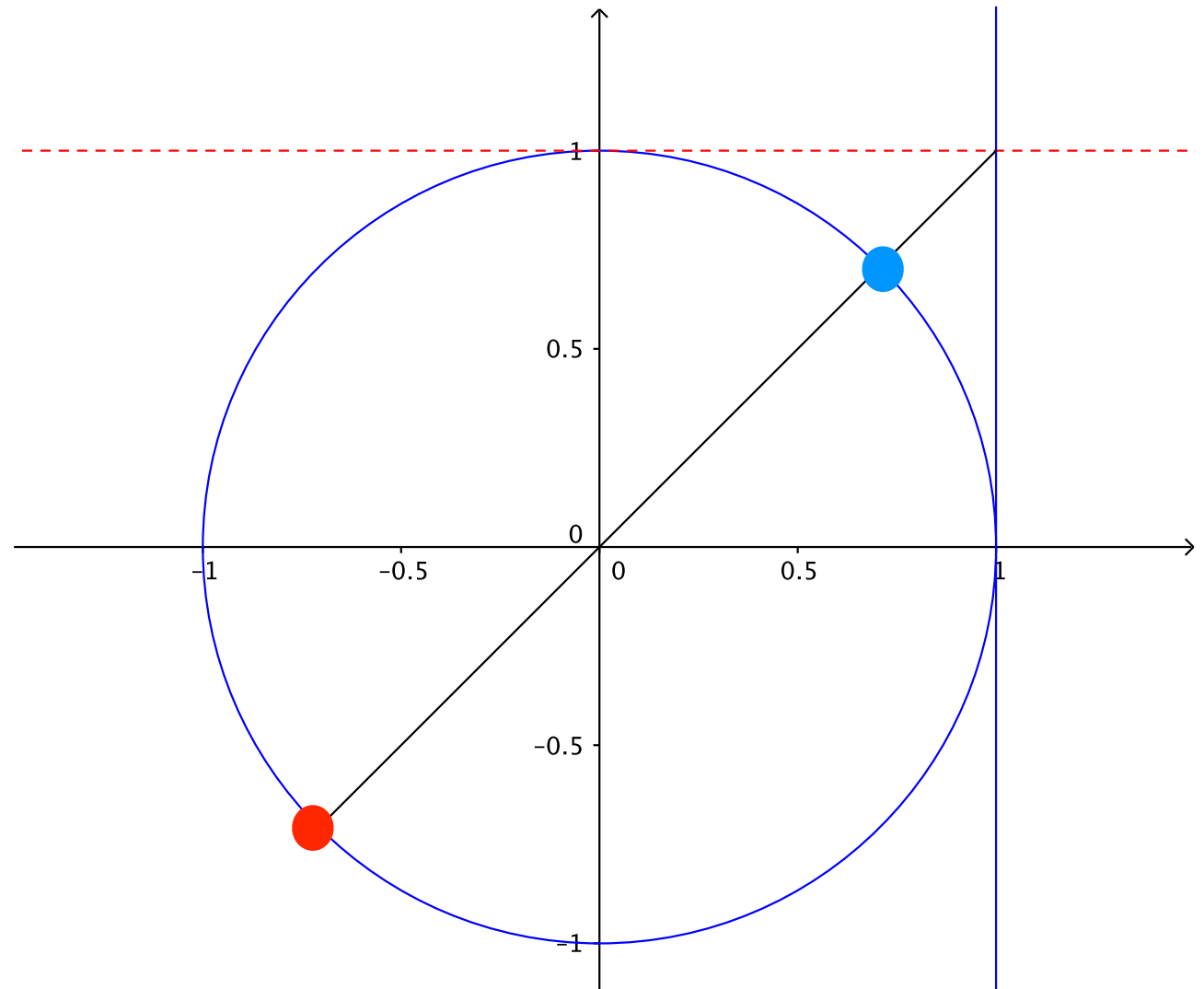
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Faites les exercices suivants

p. 517 Ex. 13.10

Devoir:

p. 521 # 17